



# System Size and Beam Energy Effects on Probing the Nuclear Symmetry Energy with Pion Ratio

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# Outline

Brief Introduction on nuclear symmetry energy

>  $\pi^{-}/\pi^{+}$  probe to  $E_{sym}(\rho)$  at high densities

Main results and discussions

Conclusion and further experiments





# EOS of Asymmetric Nuclear Matter and Symmetry Energy

# $E(\rho,\delta) = \frac{E(\rho,0) + E_{sym}(\rho)\delta^2 + O(\delta^4), \quad \delta = (\rho_n - \rho_p)/\rho$

$$E_{\rm sym}(\rho) \equiv \frac{1}{2} \frac{\partial^2 E(\rho, \delta)}{\partial \delta^2}$$

Most progress has been made to constrain the behavior of density dependence of symmetry energy at sub-saturation densities while little is know at supra-saturation densities!







A Conservative Conclusion about Symmetry Energy at Sub-saturation Densities

- Isospin diffusion experiment at MSU
- ✓ Neutron skin in <sup>208</sup>Pb from hadronic probes
- Isoscaling in heavy-ion reactions
- Isospin dependence of giant monopole resonance

$$31.6(\rho / \rho_0)^{0.69} \leq E_{sym}(\rho) \leq 31.6(\rho / \rho_0)^{1.05}$$

B.A. Li, L.W. Chen and C.M. Ko, Phys. Rep. 464 (2008) 113





# A Promising Probe at Super-saturation Densities $\pi^{-}/\pi^{+}$ ratio

## **Isobaric Model**

 $\pi^{-}/\pi^{+} = (5N^{2}+NZ)/(5Z^{2}+NZ) \approx (N/Z)^{2}_{dens}$ 

 $\Delta$  (1232) resonance model in first chance NN scattering (neglect re-scattering and re-absorption)

## **Thermal Model**

$$\frac{\pi^-}{\pi^+} \propto \exp[2(\mu_n - \mu_p)/kT]$$

 $\mu_{n} - \mu_{p} = (V_{asy}^{n} - V_{asy}^{p})\delta - V_{Coul} + kT\{\ln\frac{\rho_{n}}{\rho_{p}} + \sum_{m}\frac{m+1}{m}b_{m}(\frac{1}{2}\lambda_{T}^{3})^{m}(\rho_{n}^{m} - \rho_{p}^{m})\}$ 





# An Isospin and Momentum Dependent Transport Model

## **IBUU04**

The isospin and momentumdependent mean- field potential (MDI) is followed by:

$$U(\rho, \delta, \mathbf{p}, \tau) = A_u(x) \frac{\rho_{\tau'}}{\rho_0} + A_l(x) \frac{\rho_{\tau}}{\rho_0} + B\left(\frac{\rho}{\rho_0}\right)^{\sigma} (1 - x\delta^2) - 8x\tau \frac{B}{\sigma + 1} \frac{\rho^{\sigma - 1}}{\rho_0^{\sigma}} \delta\rho_{\tau'} + \frac{2C_{\tau,\tau}}{\rho_0} \int d^3 \mathbf{p}' \frac{f_{\tau}(\mathbf{r}, \mathbf{p}')}{1 + (\mathbf{p} - \mathbf{p}')^2 / \Lambda^2} + \frac{2C_{\tau,\tau'}}{\rho_0} \int d^3 \mathbf{p}' \frac{f_{\tau'}(\mathbf{r}, \mathbf{p}')}{1 + (\mathbf{p} - \mathbf{p}')^2 / \Lambda^2}.$$
 (1)

C. B. Das, S. Das Gupta, C. Gale, B. A. Li PRC67(2003) 034611

The parameter x above is introduced to mimic the density dependence of symmetry energy.







# $\pi^{-}/\pi^{+}$ Probe the Behavior of Symmetry Energy at Supra-saturation Densities







 $\pi^{-}/\pi^{+}$  Probe the Behavior of Symmetry Energy at Supra-saturation Densities







A rather soft nuclear symmetry energy is more favored to FOPI data!!!

Z.G. Xiao, B.A. Li, L.W. Chen, G.C. Yong and M. Zhang, Phys. Rev. Lett. 102 (2009) 062502





## Probing the Behavior of Symmetry Energy with the Same Neutron/proton Ratio but Different Masses



$$\mathbf{R} = (\pi^{-}/\pi^{+})_{x=1} / (\pi^{-}/\pi^{+})_{x=0}$$

- 1. The  $\pi^{-}/\pi^{+}$  ratio increases with decreasing the beam energy and exceeds the isobar model prediction.
- 2. The sensitivity R decreases as the beam energy increases.
- **3.** The sensitivity R increases from light to heavy system at a fixed beam energy.





#### Probing the Behavior of Symmetry Energy with the Same Neutron/proton Ratio but Different Masses

The sensitivity **R** is related to the degree of *isospin fractionation* !

**Definition**: the participant region is more neutron-rich (poor) if the value of the symmetry energy at high densities is lower (higher).

 ✓ Lower beam energy and lager system size can result in a higher central density, a much longer duration of the reaction thus a larger isospin fractionation.

Therefore, results suggest that heavy systems with larger N/Z are preferential to constrain the behavior of symmetry energy at supra-saturation densities with pion ratio near the threshold of pion production in experiment.





#### Quantitative Relation between Degree of Isospin Fractionation and Sensitivity



To the first order of approximation, we define the quality  $R_{\pi}$  -  $R_{isob}$  to describe the degree of isospin fractionation.





## **Conclusion and Further Experiment**

Heavy colliding systems are recommended in experiment to probe the behavior of symmetry energy at supra-saturation densities with the beam energy near the threshold of pion production.

External Target Facility at HIRFL-CSR in China provide good opportunities to study EOS of asymmetric nuclear matter at sub-GeV energy regime.





# External Target Facility — Phase I - II Complex at HIRFL-CSR



#### **POSSIBLE PHYSICS**

**RIB** Physics  $\sqrt{\text{EOS}}$  of Asymmetric Nuclear Matter High Baryon Density Matter

