# Dense matter EOS with GW170817

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- Zhou, et al., 1711.04312, PRD accepted
- Ai, et al., 1802.00571, ApJL under review
- Zhu, et al., 1802.05510, ApJ under review



# First Cosmic Event Observed in GRAVITATIONAL WAVES AND LIGHT

Intro of GW170817 

- EOS of NS/QS
- Summary

http://blogs.cornell.edu/arxiv/2017/10/16/gw170817/

PRL:1 Nature: 6 Science:7 ApJL:23 67 preprints:



Mooley et al., 1711.11573

# ► GW

- Neutrino: none
- **▶** γ-ray: 1.7 s
- ► X-ray: 9 days
- ► UV/Optical/IR: 2 days
- ► Radio:16 days





### Long-lived NS as remnant?

EOS

Ejecta mass

Mass ratio

Jet sructure

- **Spin period** 1.
- 2. **Magnetic field**
- 3. Ellipticity
- Δ

S.-K. Ai, H. Gao, Z.-G. Dai, X.-F. Wu, A. Li and B. Zhang, **1802.00571** #The allowed parameter space of a long-lived neutron star as the merger remnant of GW170817



TABLE I. Source properties for GW170817: we give ranges encompassing the 90% credible intervals for different assumptions of the waveform model to bound systematic uncertainty. The mass values are quoted in the frame of the source, accounting for uncertainty in the source redshift.

	Low-spin priors $( \chi  \le 0.05)$	High-spin priors $( \chi  \le 0.89)$
Primary mass $m_1$	1.36–1.60 M <sub>☉</sub>	1.36–2.26 M <sub>☉</sub>
Secondary mass $m_2$	$1.17 - 1.36 M_{\odot}$	$0.86 - 1.36 M_{\odot}$
Chirp mass $\mathcal{M}$	$1.188^{+0.004}_{-0.002} M_{\odot}$	$1.188^{+0.004}_{-0.002} M_{\odot}$
Mass ratio $m_2/m_1$	0.7–1.0	0.4–1.0
Total mass $m_{\rm tot}$	$2.74^{+0.04}_{-0.01} {M}_{\odot}$	$2.82^{+0.47}_{-0.09} {M}_{\odot}$
Radiated energy $E_{\rm rad}$	$> 0.025 M_{\odot}c^{2}$	$> 0.025 M_{\odot}c^{2}$
Luminosity distance $D_{\rm L}$	$40^{+8}_{-14}$ Mpc	$40^{+8}_{-14}$ Mpc
Viewing angle $\Theta$	$\leq 55^{\circ}$	$\leq 56^{\circ}$
Using NGC 4993 location	$\leq 28^{\circ}$	$\leq 28^{\circ}$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	$\leq 800$	$\leq 700$
Dimensionless tidal deformability $\Lambda(1.4M_{\odot})$	≤ 800	≤ 1400





TABLE I. Source properties for GW170817: we give ranges encompassing the 90% credible intervals for different assumptions of the waveform model to bound systematic uncertainty. The mass values are quoted in the frame of the source, accounting for uncertainty in the source redshift.



• Low-spin spior ( $\Lambda(1.41\text{M}_{\odot}) \leq 800$ )	3-tropes	All EoSs	$2M_{\odot}$
► NS EOS	$\gamma_1 \ M_{ m max}[M_\odot] \ R(1.4M_\odot)[ m km]$	0.2-8.5 <0.5-3.0 7.1-14.6	0.7-8.5 2.0-3.0 10.7-14.6
#Gravitational-wave constraints on the	4-tropes	All EoSs	$2M_{\odot}$
neutron-star-matter Equation of State Annala et al., <b>1711.02644</b> (17/11/7), <b>PRL</b>	$M_{ m max}[M_{\odot}]$ $R(1.4M_{\odot})[ m km]$	< 0.5 - 3.2 6.6 - 14.6	2.0-3.2 9.9-14.6

 $\Lambda < 800$ 

0.7-6.62.0-2.7 10.7-13.6

 $\Lambda < 800$ 

0.6-6.7 2.0-3.0 9.9-13.6

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#GW170817: Joint Constraint on the Neutron Star Equation of State from Multimessenger Observations Radice et al., **1711.03647, ApJL** 

#Neutron skins and neutron stars in the multi-messenger era Fattoyev, et al., **1711.06615, PRL** 

#Imprints of the nuclear symmetry energy on the tidal deformability of neutron stars Krastev & Li, **1801.04620** 

# QS EOS

#Constraints on interquark interaction parameters with GW170817 in a binary strange star scenario Zhou, Zhou & AL, 1711.04312 (17/11/12 in 4 weeks), PRD

- ► **QS** from Bodmer-Witten's conjecture
- Self-bound by strong interaction:
  - Finite surface density;
  - ► Fast increase of grav. mass with spin frenquency (40% vs. 20%,
    - e.g., AL et al. 2016 PRD 1606.02934; 2017 ApJ 1706.04720)



**Figure 3** The pressure–density relation (EOS, left) and the corresponding M-R relation (right) for some example models with different microphysics. Nucleonic (neutrons, protons): models AP3 and AP4 from Akmal & Pandharipande (1997), also used in Lattimer & Prakash (2001). Quark (u, d, s quarks): models from Li et al. (2016) and Bhattacharyya et al. (2016). Hybrid (inner core of uds quarks, outer core of nucleonic matter): models from Zdunik & Haensel (2013). Hyperon (inner core of hyperons, outer core of nucleonic matter): Model from Bednarek et al. (2012). CEFT: range of nucleonic EOS based on Chiral Effective Field Theory (CEFT) from Hebeler et al. (2013). pQCD: range of nucleonic EOS from Kurkela et al. (2014) that interpolate from CEFT at low densities and match to perturbative QCD (pQCD) calculations at higher densities than shown in this figure. All of the EOS shown are compatible with the existence of ~ 2  $M_{\odot}$  NSs.

#### Dense matter with eXTP (White paper), Sci. China in press





- MIT $\alpha_s^2$  bag model
  - ▶ interaction parametrized in  $(B_{eff}, a_4)$
  - superfluid parametrized in  $\Delta$
- ► Typical parameters  $(B_{eff}^{1/4}, a_4)$ = (145, 0.61)
- BQS merger justified.



 $\Omega_{\text{free}} = \sum_{i} \Omega_{i}^{0} + \frac{3}{4\pi^{2}} (1 - a_{4}) \left(\frac{\mu_{b}}{3}\right)^{4} + B_{\text{eff}}$ 

 $\Omega_{\rm CFL} = \Omega_{\rm free} - \frac{3}{\pi^2} \Delta^2 \mu_b^2$ 

	$a_4$	$B_{\mathrm{eff}}^{1/4} \left[ \mathrm{MeV} \right]$	$R[\mathrm{km}]$	M/R	$k_2$	Λ
	0.61	133	12.046	0.17166	0.19973	893.4
Normal QS	0.61	136	11.662	0.17731	0.18865	717.7
	0.61	138	11.415	0.18115	0.18133	619.7
	0.72	138	11.453	0.18055	0.18262	634.5
	0.83	138	11.482	0.18008	0.18367	646.6

- ► Finite strange quark mass (m<sub>s</sub>) soften EOS;
- Perturbative QCD correction (a<sub>4</sub>) soften EOS;
- Effective bag constant (B<sub>eff</sub>)
   dominates the EOS stiffness;
- Strong  $\Lambda(1.4)$ -vs- $M_{TOV}$  correlation:

$$\Lambda(1.4) = 510.058 \times \left(\frac{M_{\rm TOV}}{2.01 \, M_{\odot}}\right)^{5.4}$$



- ► NEW parameter ranges from GW170817:  $B_{\text{eff}}^{1/4} \in (134.1, 141.4) \text{ MeV}$
- ► Weak a<sub>4</sub> softening;
- QM stability window:
  - 2-flavor quark matter cannot be more stable than Fe nuclei;

 $a_4 \in (0.56, 0.91)$ 

3-flavor quark matter is more stable than Fe nuclei.



## Superfluid QS

- ► Gap parameter *∆* very uncertain: (0,100/150 MeV);
- a<sub>4</sub>=1: Two-solar mass constraint bounds the lower limit of at the order of 50MeV;
- ► a<sub>4</sub>=0.61: No new lower limit is found for both the low-spin prior and the high-spin prior.



Move to NS... <sup>13</sup>

## NS structure



Dark matter-mixed
► Li\*, Liu, Gubler, Xu, 2015
Astropart. phys.

► Li\*, Huang, Xu, 2012 Astropart. phys.

- Nucleons
  - ► Zhu, Li\*, 2018 PRC
  - ► Li\*, Dong, Wang, Xu, 2016 ApJS
  - ► Li\*, Zhang, Zhang, Gao, Qi, Liu, 2016 PRD
  - ► Li\*, Hu, Shang, Zuo, 2016 PRC
  - ► Li\*, Liu, 2013 A&A

#### Excited nucleons (Δ-isobars)

► Zhu, Li\*, Hu, Sagawa, 2016 PRC

#### Kaon condensation

- ► Li\*, Zhou, Burgio, Schulze, 2010 PRC
- ► Li\*, Burgio, Lombardo, Zuo, 2006 PRC
- ► Zuo\*, Li, Li, Lombardo, 2004 PRC
- ▶ Free quarks→ Hybrid star (混杂星)
  - ► Li\*, Peng, Zuo, 2015 PRC
  - ▶ Peng\*, Li, Lombardo, 2008 PRC
- ▶ Hyperons ( $\Lambda^0$ ,  $\Sigma^{0,\pm}$ ,  $\Xi^{0,-}$ )→ Hyperon star (超子星)
  - ► Li\*, Hiyama, Zhou, Sagawa, 2013 PRC
  - ▶ Hu, Li\*, Toki, Zuo, 2014 PRC
  - ▶ Burgio\*, Schulze, Li, 2011 PRC

- Any strangeness phase transition leads to
- softer EOS (lower  $M_{TOV}$ ) (Hyperon puzzle);
- Nucleonic EOS sufficiently stiff, or only weak soften (late appearance) of
- Delta/hyperon/Kaon/quark;
- Universal baryonic repulsive three-body
- force, or stiff quark core;
- Study of hyperon interaction
   (NY,YY,NNY,NYY,YYY) through
   hyperonnuclei/scattering experiments
   VERY IMPORTANT.



Hyperon interaction (NY,YY,NNY,NYY,YYY) through hyperonnuclei/scattering experiments are VERY IMPORTANT 1/2

- Microscopic scheme, e.g., BHF;
- Nijmegen soft-core NY potentials (NSC89/ESC08...) model, fitted to the available experimental NY scattering data;
- Presently, 4233 NN data, 52 NY data, weak ΛΛ attraction (Nagara event, Takahashi et al., PRL 2001)

With these potentials, the various G-matrices are evaluated by solving numerically the Bethe-Goldstone equation, which can be written in operator form as

$$G_{ab}[W] = V_{ab} + \sum_{c} \sum_{p,p'} V_{ac} |pp'\rangle \frac{Q_c}{W - E_c + i\varepsilon} \langle pp' | G_{cb}[W],$$
(6)

where the indices a, b, c indicate pairs of baryons, and the Pauli operator  $Q_c$  and energy  $E_c$  characterize the propagation of intermediate baryon pairs. The pair energy in a given channel  $c = (B_1B_2)$  is

$$E_{(B_1B_2)} = T_{B_1}(k_{B_1}) + T_{B_2}(k_{B_2}) + U_{B_1}(k_{B_1}) + U_{B_2}(k_{B_2}),$$
(7)

with  $T_B(k) = m_B + k^2/2m_B$ , where the various s.p. potentials are given by

$$U_B(k) = \sum_{B'=n,p,\Lambda,\Sigma^-} U_B^{(B')}(k) \tag{8}$$

and are determined self-consistently from the G-matrices,

$$U_B^{(B')}(k) = \sum_{k' < k_F^{(B')}} \operatorname{Re} \langle kk' | G_{(BB')(BB')}[E_{(BB')}(k,k')] | kk' \rangle_A.$$

The coupled eqs. (6)–(9) define the BHF scheme with the

e.g., Burgio, Schulze, **AL**, 1101.0726 PRC 2011

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(9)

- Hyperon interaction (NY,YY,NNY,NYY,YYY) through hyperonnuclei/scattering experiments are VERY IMPORTANT 2/2
  - Phenomenological scheme, e.g., RMF/QMF;
  - Meson coupling constant (σωρ...)



$$\mathcal{L} = \overline{\psi} \bigg[ i\gamma_{\mu} \partial^{\mu} - M_{N}^{*} - g_{\omega} \omega \gamma^{0} - g_{\rho} \rho \tau_{3} \gamma^{0} - e \frac{(1 + \tau_{3})}{2} A \gamma^{0} \bigg] \psi$$

F

$$+ \psi_{A} [i\gamma_{\mu}\partial^{\mu} - M_{A}^{*} - g_{\omega}^{A}\omega\gamma^{\sigma}]\psi_{A} - \frac{1}{2}(\nabla\sigma)^{2} - \frac{1}{2}m_{\sigma}^{2}\sigma^{2} - \frac{1}{4}g_{3}\sigma^{4} + \frac{1}{2}(\nabla\omega)^{2} + \frac{1}{2}m_{\omega}^{2}\omega^{2} + \frac{1}{4}c_{3}\omega^{4} \cdot + \frac{1}{2}(\nabla\rho)^{2} + \frac{1}{2}m_{\rho}^{2}\rho^{2} + \frac{1}{2}(\nabla A)^{2}$$

e.g., J. N. Hu, **AL**, H. Shen and H. Toki, 1310.3602 PTEP 2014

01.

- ► Ignore strangeness for the moment
- ► EOS uncertain most in asymmetric part: *L*-vs-*Λ*?



- Isobaric analog states (IAS) and from IAS and neutron skins (IAS+skin) (Danielewicz & Lee 2014);
- □ Electric dipole polarizability in <sup>208</sup>Pb ( $\boldsymbol{a}_{D}$ ) (*Zhang & Chen 2015*).









- Collective flow in **HIC** (Danielewicz et al. 2002);
- Transport in **HIC** (*Tsang et al. 2009*)
- ★ PSR J1614-2230 (Demorest et al. 2010; Fonseca et al. 2016);
- ★ PSR J0348+0432 (Antoniadis et al. 2013).



Many-body model

Green's Function Monte Carlo Chiral Perturbation Theory (ChPT) Variational Many-Body (VMB) V<sub>lowk</sub> + Renormalization Group Brueckner-Hartree-Fock (BHF) Dirac-Brueckner-Hartree-Fock (DBHF)

Quark mean-field (QMF)

Quark Meson Coupling (QMC)

Relativistic mean-field (RMF)

Skyrme energy density functional



Unless you are using unified NS EOS... (e.g., AL et al. 2016 PRD, ApJS)

## ► Rotation



## □ Static (TOV)

$$\frac{dP(r)}{dr} = -\frac{GM(r)\varepsilon(r)}{r^2} \frac{\left[1 + \frac{P(r)}{\varepsilon(r)}\right] \left[1 + \frac{4\pi r^3 P(r)}{M(r)}\right]}{1 - \frac{2GM(r)}{r}}, \quad (1)$$
$$\frac{dM(r)}{dr} = 4\pi r^2 \varepsilon(r), \quad (2)$$

**Slow rotation**  $\Omega \ll \Omega_{\text{max}} \approx \sqrt{GM/R^3}$ 

Spherical-symmetry metric + Axis-symmetry perturbation

Vela pulsar @ *AL, Dong, Wang, Xu,* 2016 *ApJS* 1512.00340

 NS/QS structures are unique to the underlying EoS. Fast rotation

Relativistic stars in general relativity from *rns* code (*www/gravity.phys.uwm.edu/rns*),

Komatsu H, Eriguchi Y and Hachisu I 1989 Mon. Not. R. Astron. Soc. 237 355 Cook G B, Shapiro S L and Teukolsky S A 1994 ApJ 422 227 Stergioulas N and Friedman J L 1995 ApJ 444 306

*AL, Zhang, Zhang, Gao, Qi, Liu,* 2016 PRD, 1606.02934

► NS EOS model from the quark level within QMF ( $m_q \sim 300$ MeV)

#### Step 1: Single nucleon

$$\begin{bmatrix} \gamma^{0}(\epsilon_{q} - g_{\omega q}\omega - \tau_{3q}g_{\rho q}\rho) - \vec{\gamma} \cdot \vec{p} - (m_{q} - g_{\sigma q}\sigma) - U(r) \end{bmatrix} \psi_{q}(\vec{r}) = 0$$
$$U(r) = \frac{1}{2}(1 + \gamma^{0})(ar^{2} + V_{0}) \qquad V_{0} = -62.257187 \text{ MeV} = M_{N} = 939 \text{ MeV}$$
$$a = 0.534296 \text{ fm}^{-3} \qquad M_{N} = 0.87 \text{ fm}.$$

#### Step 2: Nucleon many-body system

$$\mathcal{L} = \overline{\psi} \left( i\gamma_{\mu} \partial^{\mu} - M_{N}^{*} - g_{\omega N} \omega \gamma^{0} - g_{\rho N} \rho \tau_{3} \gamma^{0} \right) \psi - \frac{1}{2} (\nabla \sigma)^{2} - \frac{1}{2} m_{\sigma}^{2} \sigma^{2} - \frac{1}{3} g_{2} \sigma^{3} - \frac{1}{4} g_{3} \sigma^{4} + \frac{1}{2} (\nabla \rho)^{2} + \frac{1}{2} m_{\rho}^{2} \rho^{2} + \frac{1}{2} (\nabla \omega)^{2} + \frac{1}{2} m_{\omega}^{2} \omega^{2} + \frac{1}{2} g_{\rho N}^{2} \rho^{2} \Lambda_{v} g_{\omega N}^{2} \omega^{2},$$

	$L \; [MeV]$	$g_{\sigma q}$	$g_\omega$	$\upsilon q$	$g_{ ho q}$	$g_2  [\mathrm{fm}^{-1}]$	$g_3$	$\Lambda_v$
	20	3.8620366	2.917	4838	6.9588083	14.6179599	9 -66.3442468	1.1080665
	40	3.8620366	2.917	4838	5.4129448	14.6179599	9 -66.3442468	0.7693664
	60	3.8620366	2.917	4838	4.5830609	14.6179599	9 -66.3442468	0.4306662
	80	3.8620366	2.917	4838	4.0459574	14.6179599	9 -66.3442468	0.0919661
(			$ ho_0$	E/A		$E_{\rm sym}$	L	$M_N^*/M_N$
		_[fr	$n^{-3}]$	[MeV]	[MeV]	[MeV]	[MeV]	/
		<b>-</b> <u>-</u>	).16	-16	240	31	20/40/60/80	0.77
						Li	& Han (201	<b>3</b> ) <sup>23</sup>

- ► All smaller than 800 limit of GW170817;
- Larger *L*, larger *R*, **NOT** monotonic dependence of  $\Lambda$ .



- ► Tidal deformability:  $\Lambda = \frac{2}{3}k_2(M/R)^{-5}$
- describes the amount of induced mass quadrupole moment when reacting to a certain external tidal field.
- ► Tidal 2<sup>nd</sup> Love number  $k_2$ :  $Q_{ij} = -k_2 \frac{2R^5}{3G} E_{ij}$ measures how easily the bulk of the matter in a star is deformed by an external tidal field.
- ► Larger *L* leads to smaller  $k_2$ , for a star with certain amount of mass/ compactness.







$$\Lambda = \frac{2}{3}k_2(M/R)^{-5}$$

∧ is normalized with a factor of R<sup>5</sup>, from k<sub>2</sub>
 ▶ Differences in radius scatter the dependence on L.

Employing very well-constrained chirp mass of GW170817;

$$\mathcal{M} = (m_1 m_2)^{3/5} (m_1 + m_2)^{-1/5} = 1.188^{+0.004}_{-0.002} M_{\odot}$$

Combined dimensionless tidal deformability (Directly measured!)

$$\tilde{\Lambda} = \frac{16}{13} \frac{(m_1 + 12m_2)m_1^4 \Lambda_1 + (m_2 + 12m_1)m_2^4 \Lambda_2}{(m_1 + m_2)^5}$$

► Violation of monotonic dependence: Maybe dangerous to probe R/L via Λ.



To better understand the nonmonotonic behaviour





	QMF18	DDRHF	$DDRHF\Delta$	$NL3\omega\rho$	DDME2	DD2	Sly9	BCPM	-
$M_{\rm TOV} \ [M_{\odot}]$	2.08	2.50	2.24	2.75	2.48	2.42	2.16	1.98	-
$L  [{ m MeV}]$	40	82.99	82.99	55.5	51.2	55.0	54.9	52.96	_
R(1.4) [km]	11.77	13.74	13.67	13.75	13.21	13.16	12.46	11.72	<13.6 km
M/R(1.4)	0.1756	0.1505	0.1512	0.1503	0.1566	0.1571	0.1660	0.1765	(Annala et al.,)
$\Lambda(1.4)$	344	865	828	925	681	674	446	294	_

Table 4. Radius, compactness and tidal deformability for a  $1.4 M_{\odot}$  star are provided for various advanced NS EOSs, together with their maximum static gravitational mass  $M_{\text{TOV}}$  and the symmetry energy slope L.



Details in Zhu, Zhou & AL 1802.05510

Table 3. NS EOS for the QMF18 model newly introduced in this work.

$\epsilon  [{\rm g}  {\rm cm}^{-3}]$	$P [\mathrm{erg} \ \mathrm{cm}^{-3}]$	$\rho_N \; [\mathrm{fm}^{-3}]$
$0.13855E{+}15$	0.79586E + 33	0.082
$0.14365E{+}15$	0.85234E + 33	0.085
$0.15216E{+}15$	0.95144E + 33	0.090
$0.16920 \text{E}{+}15$	0.11706E + 34	0.100
$0.18626E{+}15$	0.14226E + 34	0.110
0.20336E + 15	0.17145E + 34	0.120
0.22047E + 15	0.20433E + 34	0.130
0.27203E + 15	0.33950E + 34	0.160
0.32393E + 15	0.55426E + 34	0.190
0.37631E + 15	0.87679E + 34	0.220
0.42926E + 15	0.13315E + 35	0.250
0.48293E + 15	0.19385E + 35	0.280
0.53741E + 15	0.27149E + 35	0.310
0.59282E + 15	0.36752E + 35	0.340
0.64927E + 15	0.48329E + 35	0.370
0.70686E + 15	0.62008E + 35	0.400
$0.76568E{+}15$	0.77912E + 35	0.430
$0.82583E{+}15$	0.96151E + 35	0.460
0.88738E + 15	0.11682E + 36	0.490
$0.95043E{+}15$	0.13999E + 36	0.520
$0.10150 \mathrm{E}{+16}$	0.16569E + 36	0.550
$0.10813E{+}16$	0.19389E + 36	0.580
$0.11492E{+}16$	0.22449E + 36	0.610
$0.12189E{+}16$	0.25733E + 36	0.640
$0.12904E{+}16$	0.29223E + 36	0.670
0.13636E + 16	0.32903E + 36	0.700
0.14896E + 16	0.39423E + 36	0.750
0.16207E + 16	0.46399E + 36	0.800
$0.17568E{+}16$	0.53809E + 36	0.850
$0.18978E{+}16$	0.61645E + 36	0.900
0.20438E + 16	0.69900E + 36	0.950
0.21948E + 16	0.78573E + 36	1.000
0.25116E + 16	0.97160E + 36	1.100
$0.28480 \text{E}{+}16$	0.11739E + 37	1.200
0.32039E + 16	0.13926E + 37	1.300

#### "QMF18" Welcome to use!

# First Cosmic Event Observed in Gravitational Waves and Light

In this talk

- QS merger scenario for GW demonstrated;
- New interquark parameter range found;
- New NS EOS "QMF18" proposed.



# Hurry for more calculations before O5! Thank you for listening. Ang

