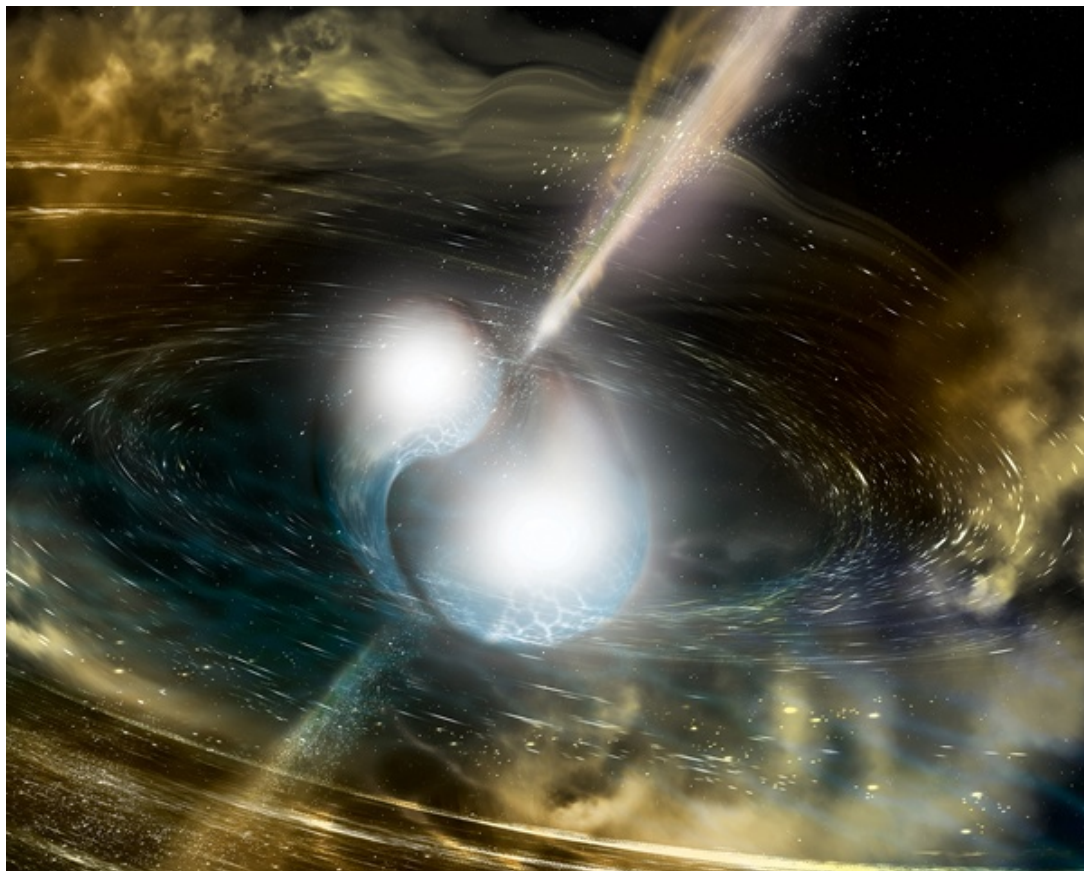


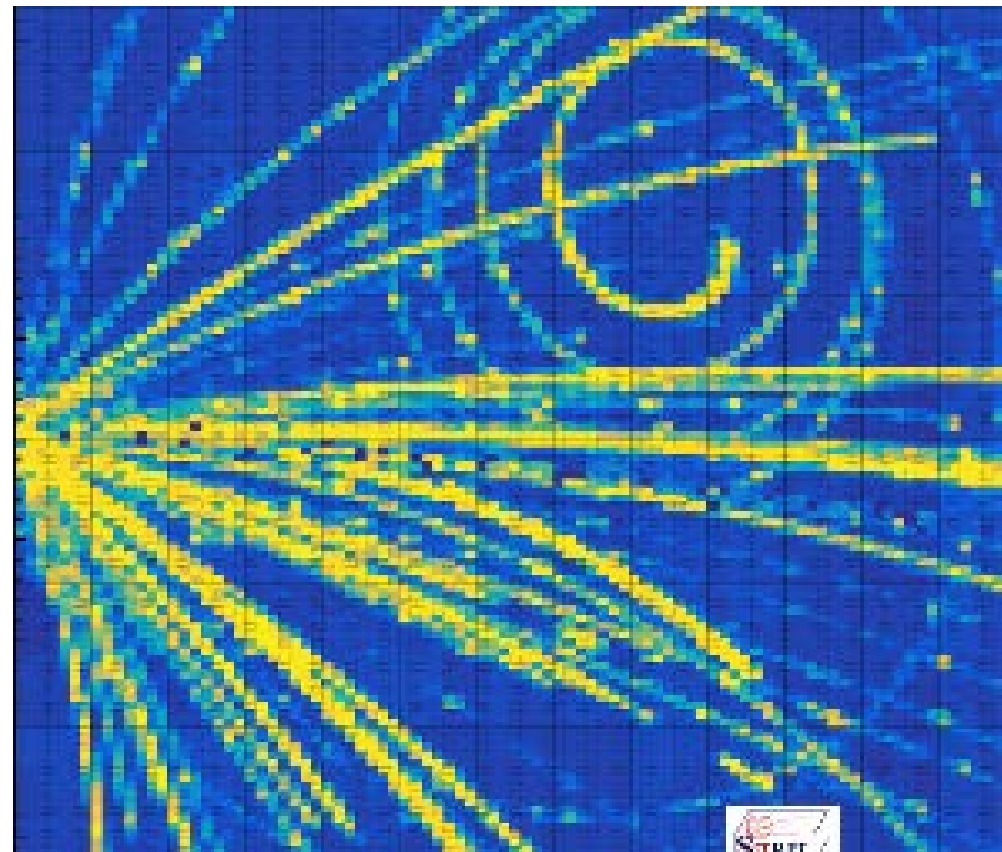
# Laboratory Probes of the Neutron-Matter Equation of State

LIGO Detects a Neutron Star Merger



Betty Tsang, NSCL  
Michigan State University

$^{132}\text{Sn} + ^{124}\text{Sn}$  @  $E/A = 270$  MeV

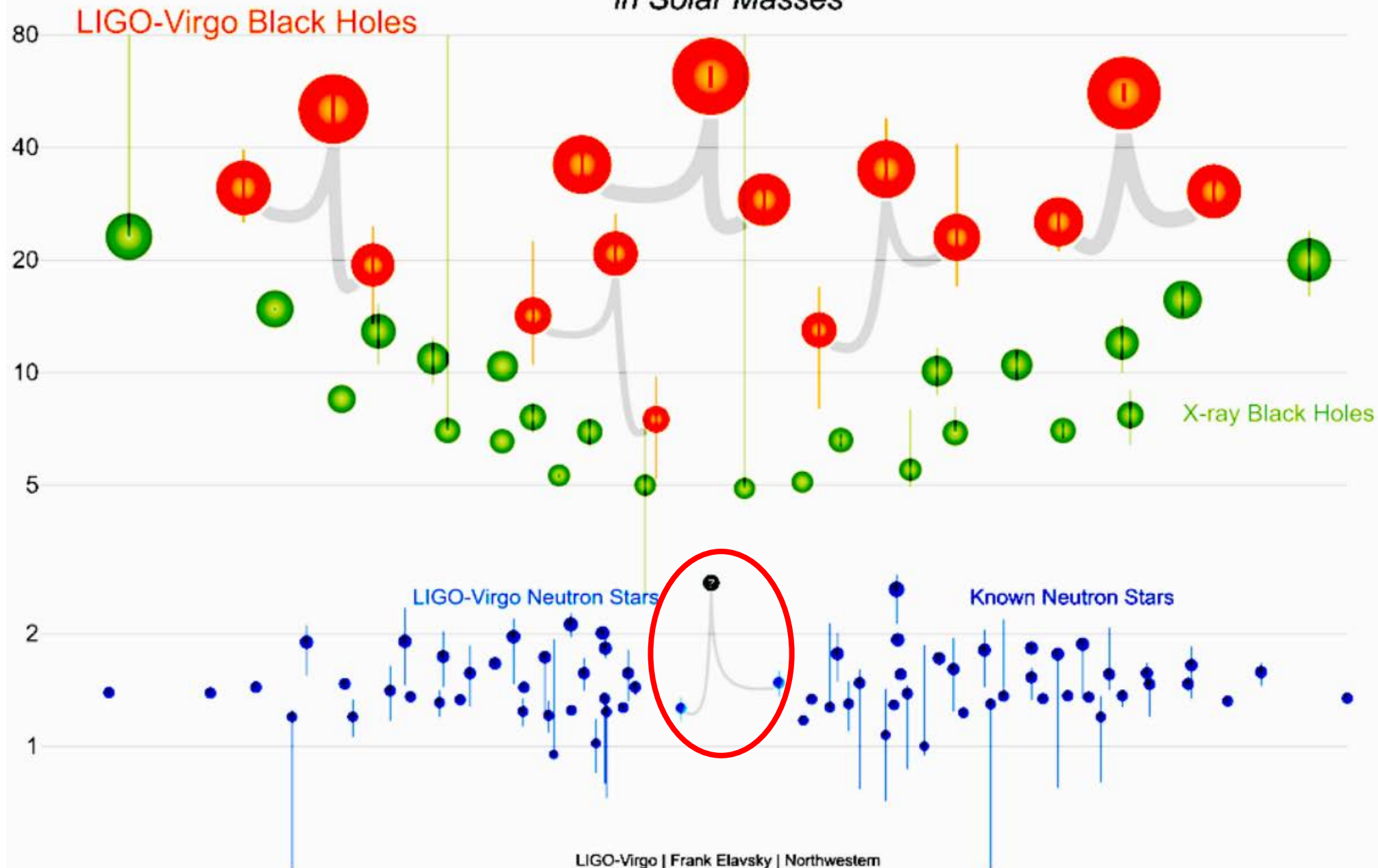


Tsinghua Symposium: 4/7-14/11  
INT17



# Masses in the Stellar Graveyard

*in Solar Masses*



**Fate of a Neutron Star Merger: n-star, black hole or transient**

**Organizer:**  
Sanjay Reddy  
Institute for Nuclear Theory  
[sareddy@uw.edu](mailto:sareddy@uw.edu)

**Advisory Committee:**  
Charles Horowitz  
Daniel Kasen  
James Lattimer  
Gabriel Martinez-Pinedo  
Brian Metzger  
David Radice  
Jocelyn Read  
Luke Roberts  
Bangalore Sathyaprakash  
Hendrik Schatz  
Masaru Shibata  
Rebecca Surman

**Program Coordinator:**  
Kimberlee Choe  
[jy24@uw.edu](mailto:jy24@uw.edu)  
(206) 685-3509

[Application form](#)

[Workshop Schedule](#)

[Talks Online](#)

[Exit Survey](#)

## INT-JINA Symposium INT-18-72R

# First multi-messenger observations of a neutron star merger and its implications for nuclear physics

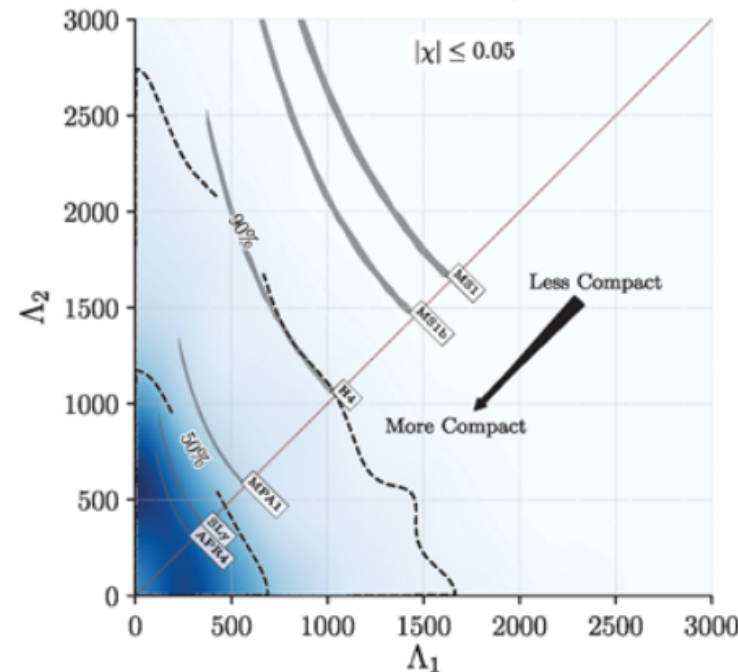
March 12 - 14, 2018

PRL 119, 161101 (2017) week ending  
20 OCTOBER 2017

PHYSICAL REVIEW LETTERS

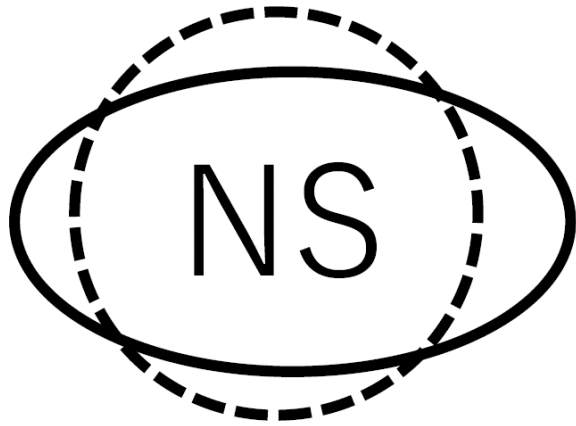
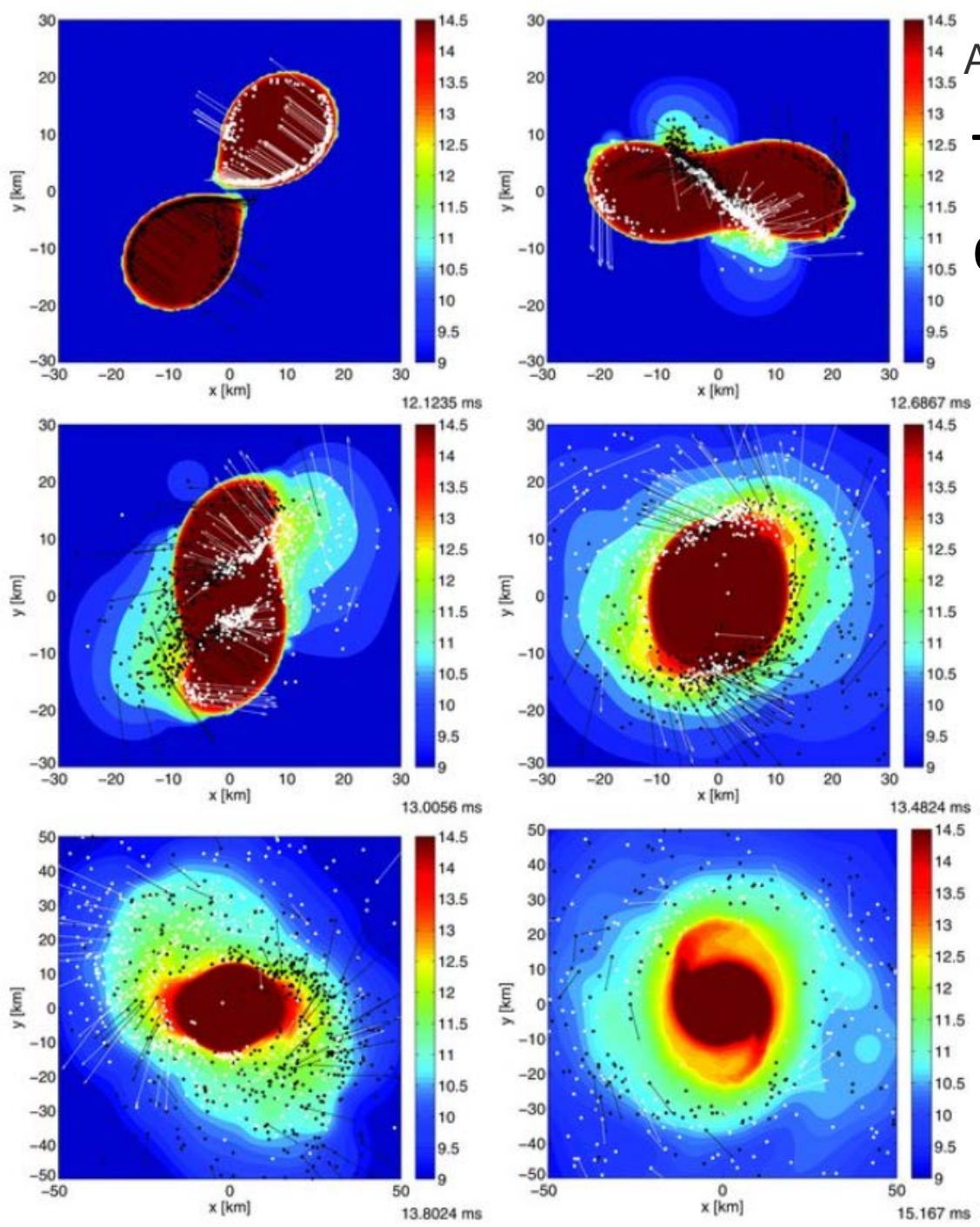
GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

B. P. Abbott *et al.*<sup>\*</sup>  
(LIGO Scientific Collaboration and Virgo Collaboration)

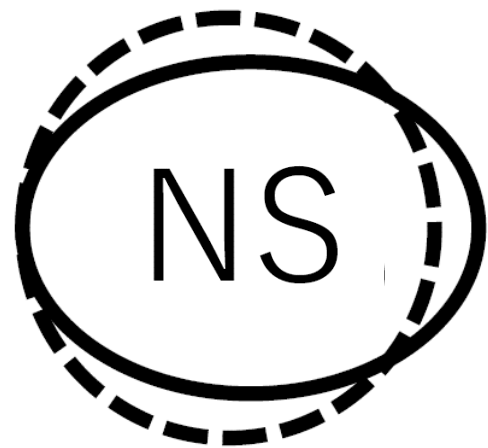


- Very stiff (unrealistic) EOS which predict  $R > 14$  kms are disfavored.
- Data appears to favor a finite polarizability but cannot distinguish between radii in the range 9-13 kms.
- Systematic errors due to spin-orbit, spin-spin interactions are included in parameter estimation.

# Tidal deformation of the Neutron Star depends on the compactness ( $M/R$ )



Soft EoS  
Large deformation



Stiff EoS  
small deformation

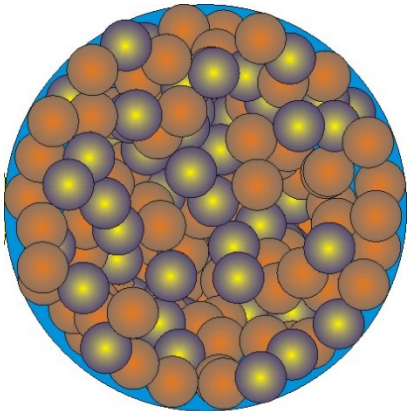
The physics, (symmetry energy), that governs the neutrons skin thickness of  $^{208}\text{Pb}$  is the same as that governing the neutron star radius

C.J. Horowitz, J. Piekarewicz, PRL 86 (2001) 5647

### Parity Radius Experiment (P-ReX)

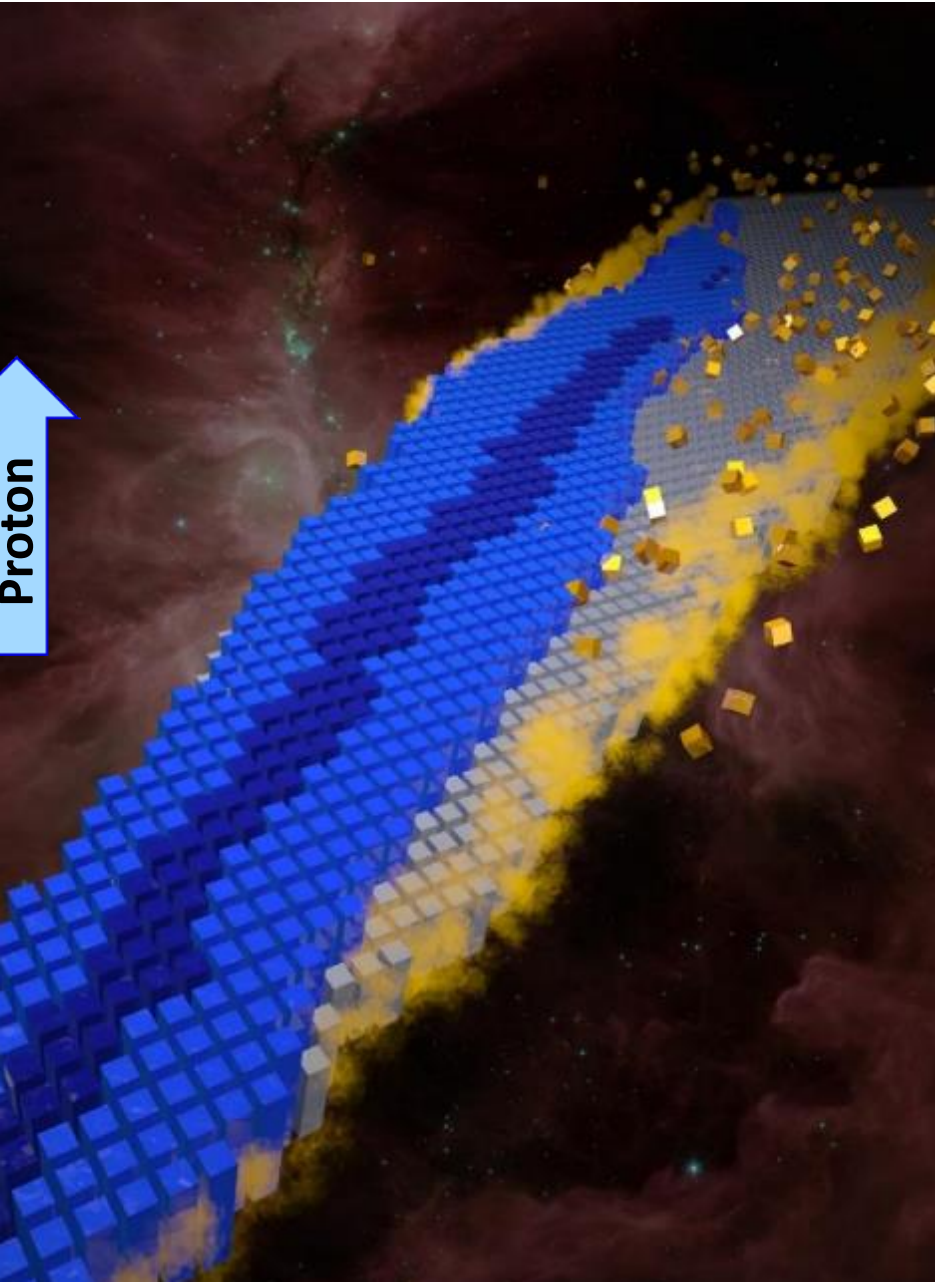
$\sim 10^{-15}$  m

$\sim 10^4$  m



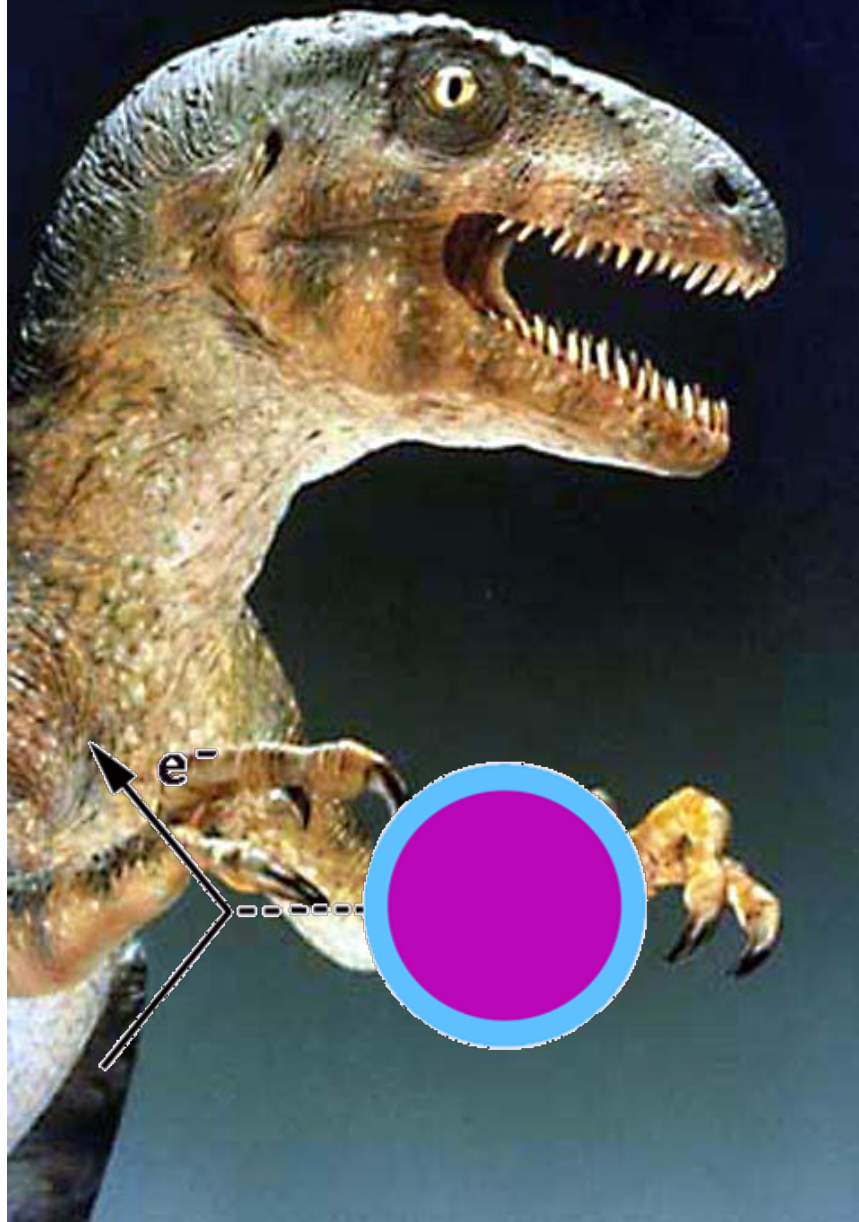
$^{208}\text{Pb}$   
 $\sim 208$

Neutron Star  
 $10^{57}$



Hubble  
ST

$^{208}\text{Pb}$  n-skin

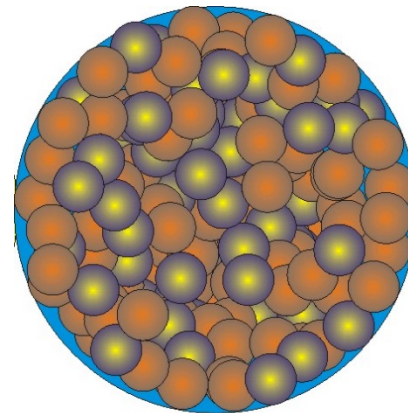


The physics, (symmetry energy), that governs the neutrons skin thickness of  $^{208}\text{Pb}$  is the same as that governing the neutron star radius

C.J. Horowitz, J. Piekarewicz, PRL 86 (2001) 5647

## Parity Radius Experiment (P-ReX)

$\sim 10^{-15}$  m



$^{208}\text{Pb}$   
 $\sim 208$

$\sim 10^4$  m



Neutron Star  
 $10^{57}$

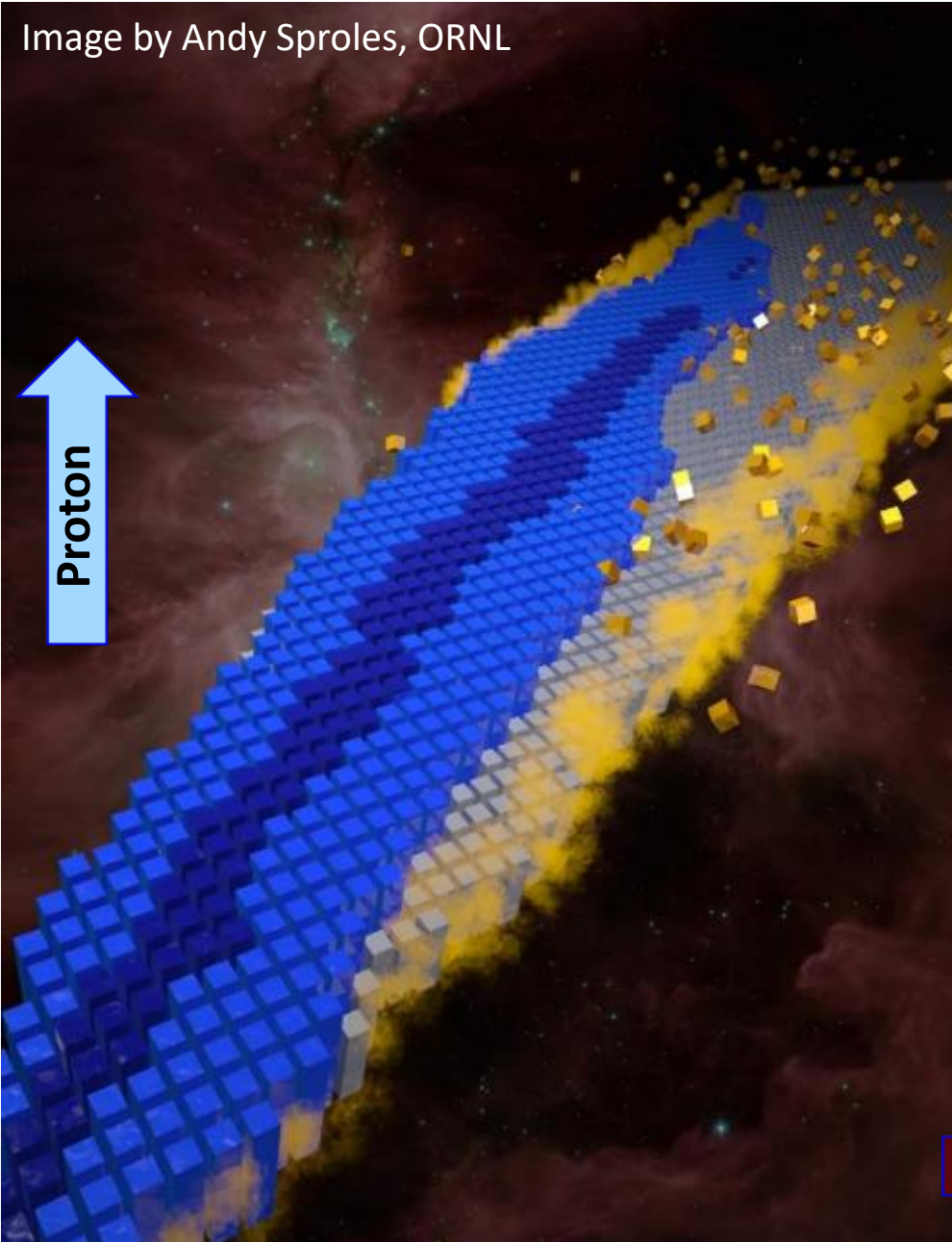
$R_{np}(^{208}\text{Pb}) < 0.25$  fm

$R(\text{NS}) < 13.76$  km

Fattoyev et al., [arXiv:1711.06615](https://arxiv.org/abs/1711.06615)

# Symmetry Energy

Image by Andy Sproles, ORNL



$$B = a_V A - a_S A^{2/3} - a_C \frac{Z(Z-1)}{A^{1/3}}$$

$$- a_{sym} \frac{(A-2Z)^2}{A}$$



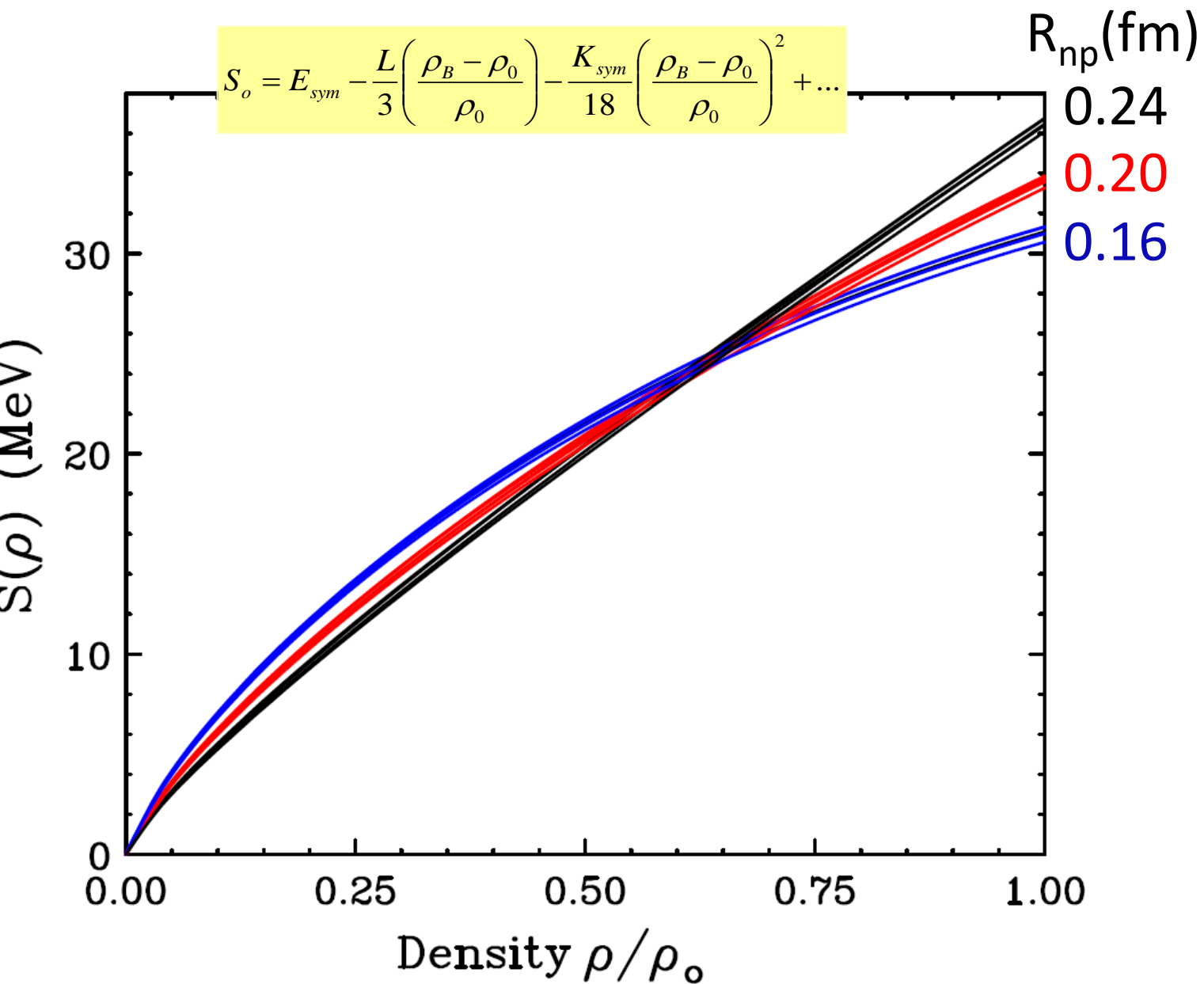
$$(a_{sym}^V A - a_{sym}^S A^{2/3}) \frac{(A-2Z)^2}{A^2}$$

*Inclusion of surface terms in symmetry*



Hubble  
ST



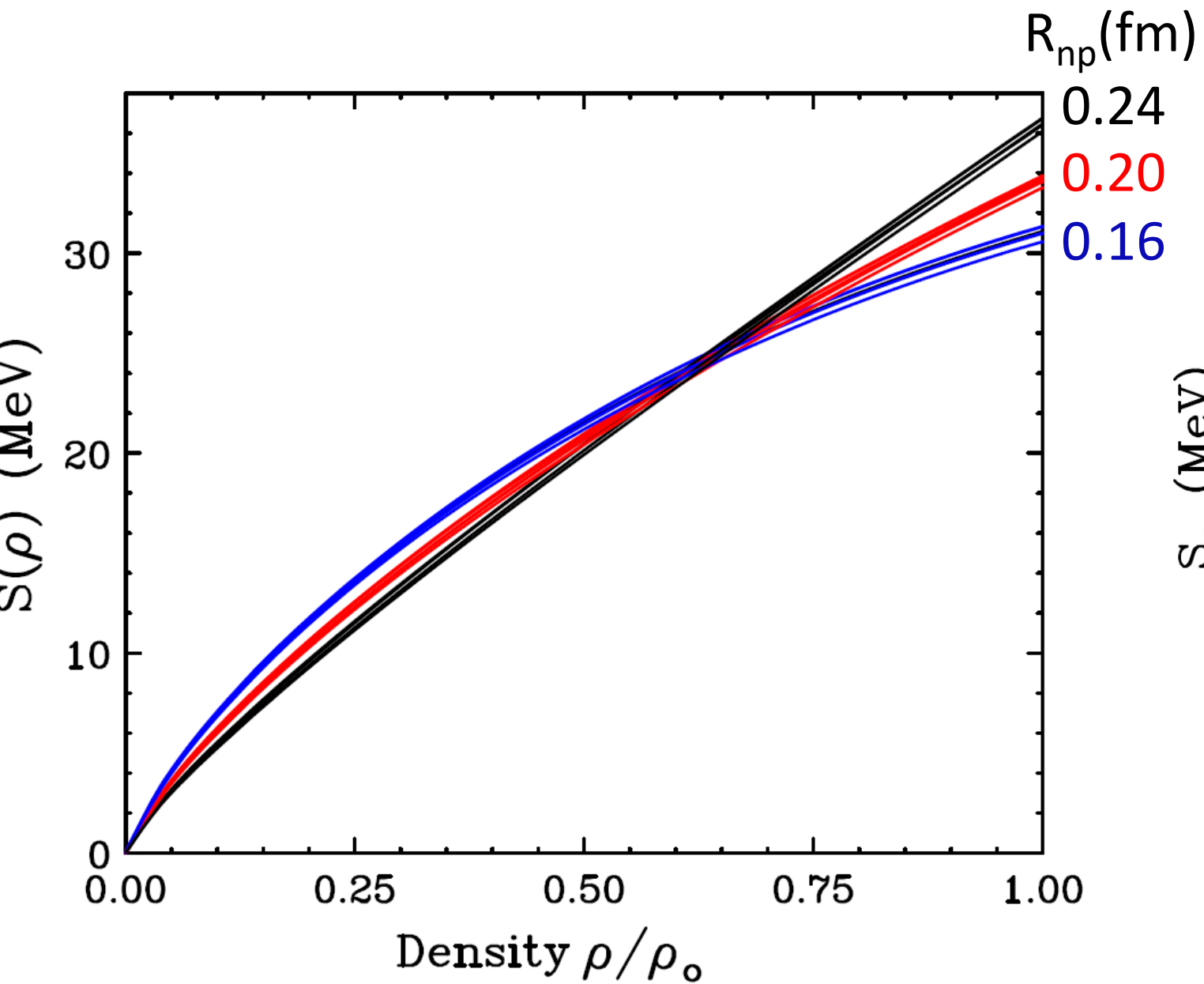


Alex Brown

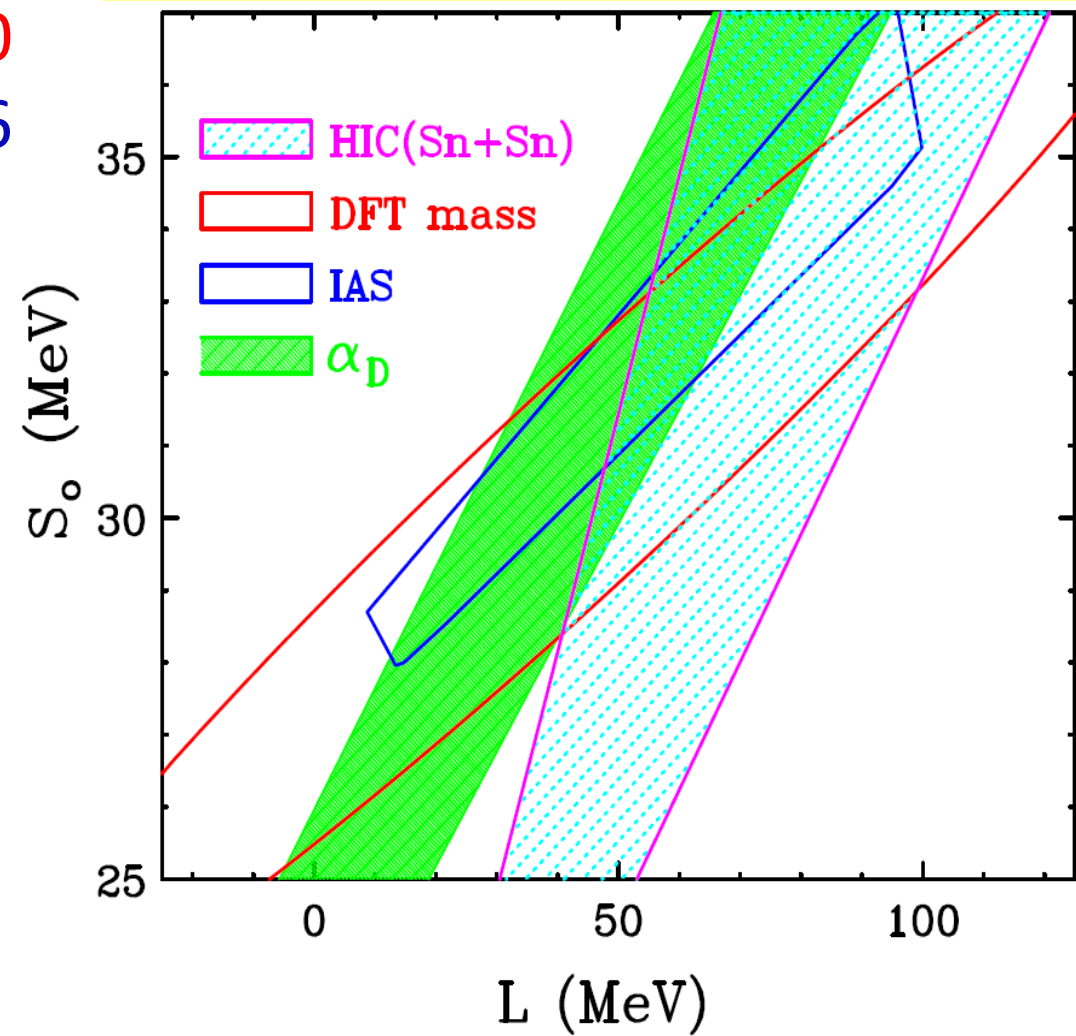
PRL 111, 232502 (2013)

Use Skyrme interactions that fit the masses of double magic nuclei

Masses and skin data are sensitive to  $\rho \sim 0.65\rho_0$   
 $E_{sym}(\rho \sim 0.65\rho_0) \sim 25$  MeV



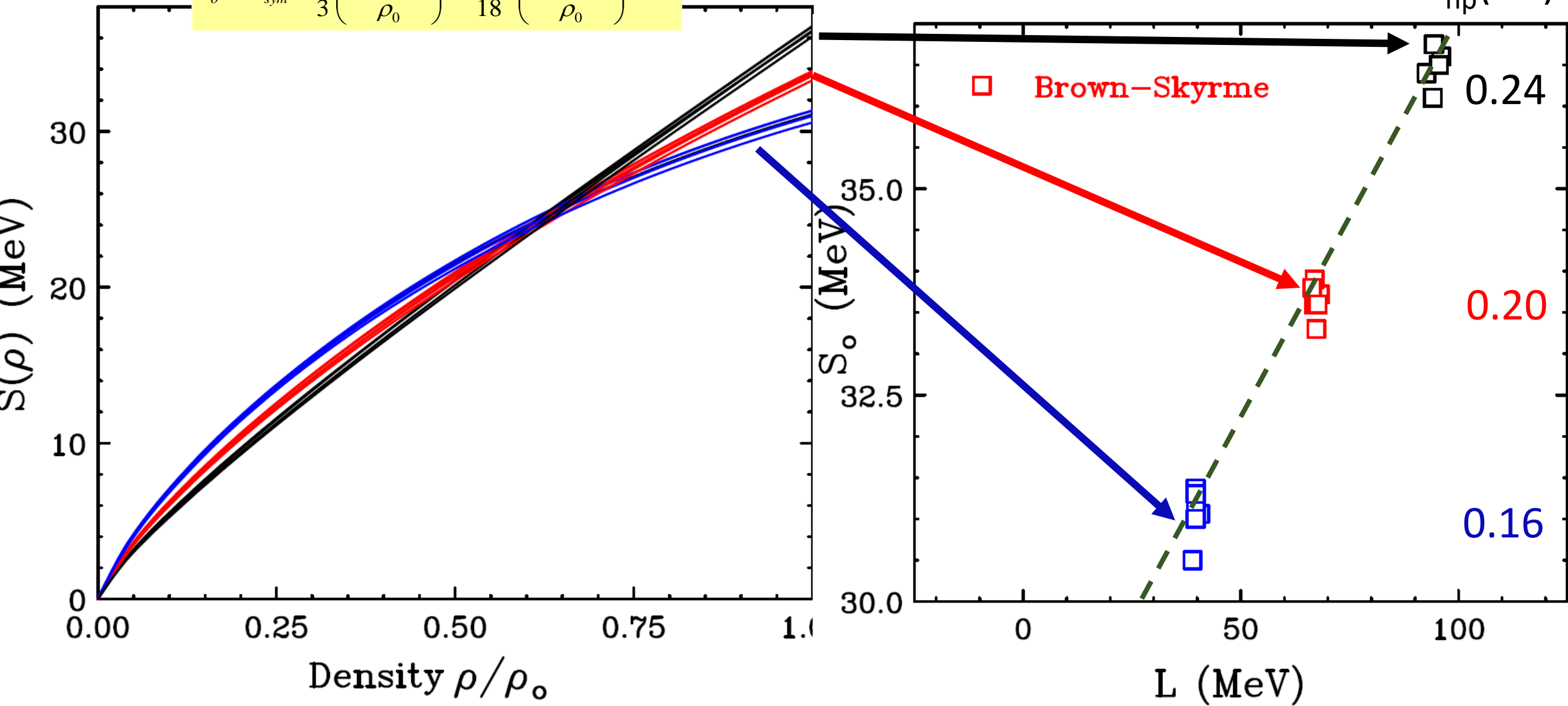
$$S_o = E_{sym} - \frac{L}{3} \left( \frac{\rho_B - \rho_0}{\rho_0} \right) - \frac{K_{sym}}{18} \left( \frac{\rho_B - \rho_0}{\rho_0} \right)^2$$



Masses and skin data are sensitive to  $\rho \sim 0.65\rho_0$

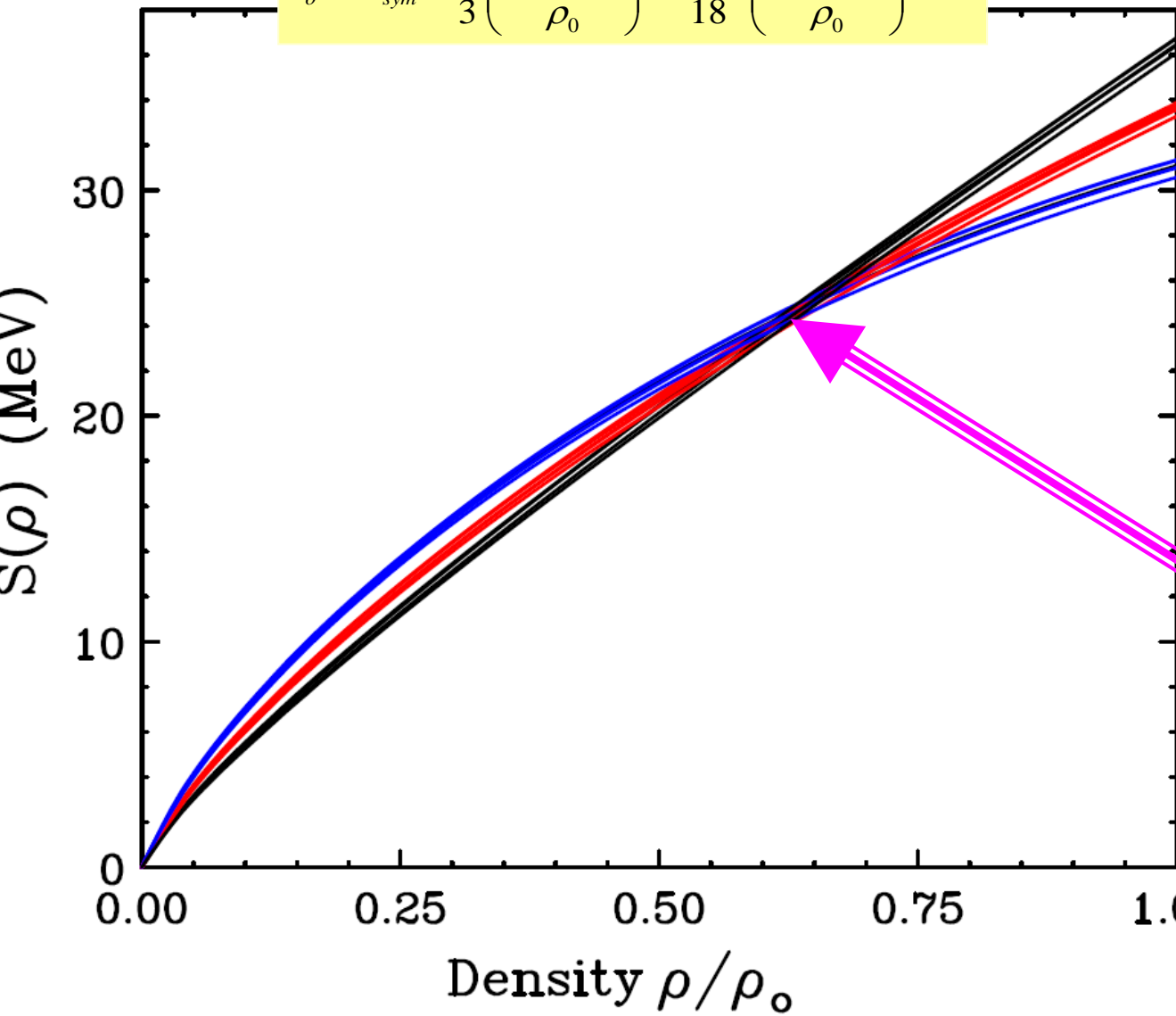
Same slope gives you sensitive density region of the observable

$$S_o = E_{sym} - \frac{L}{3} \left( \frac{\rho_B - \rho_0}{\rho_0} \right) - \frac{K_{sym}}{18} \left( \frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

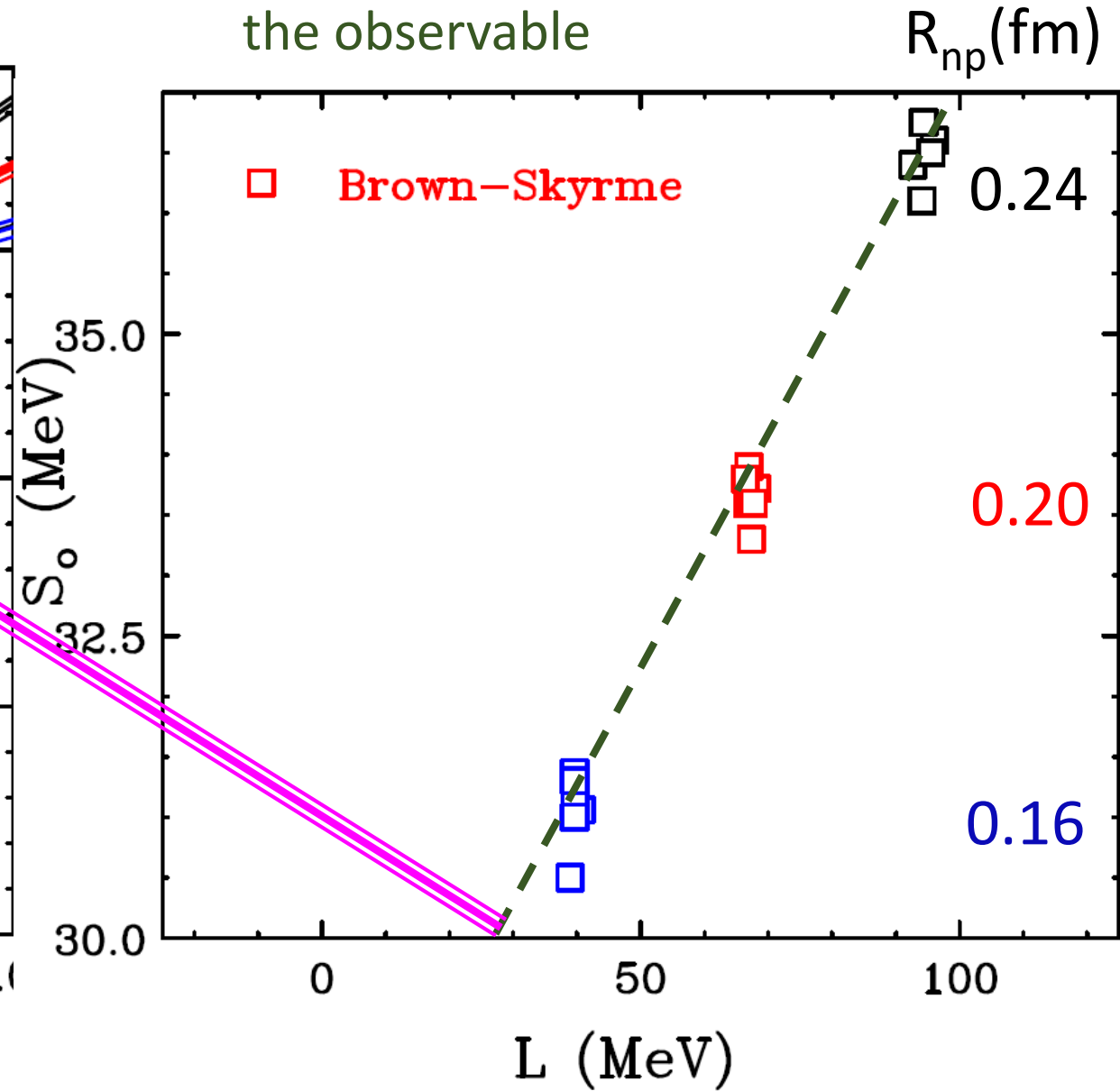


Masses and skin data are sensitive to  $\rho \sim 0.65\rho_0$

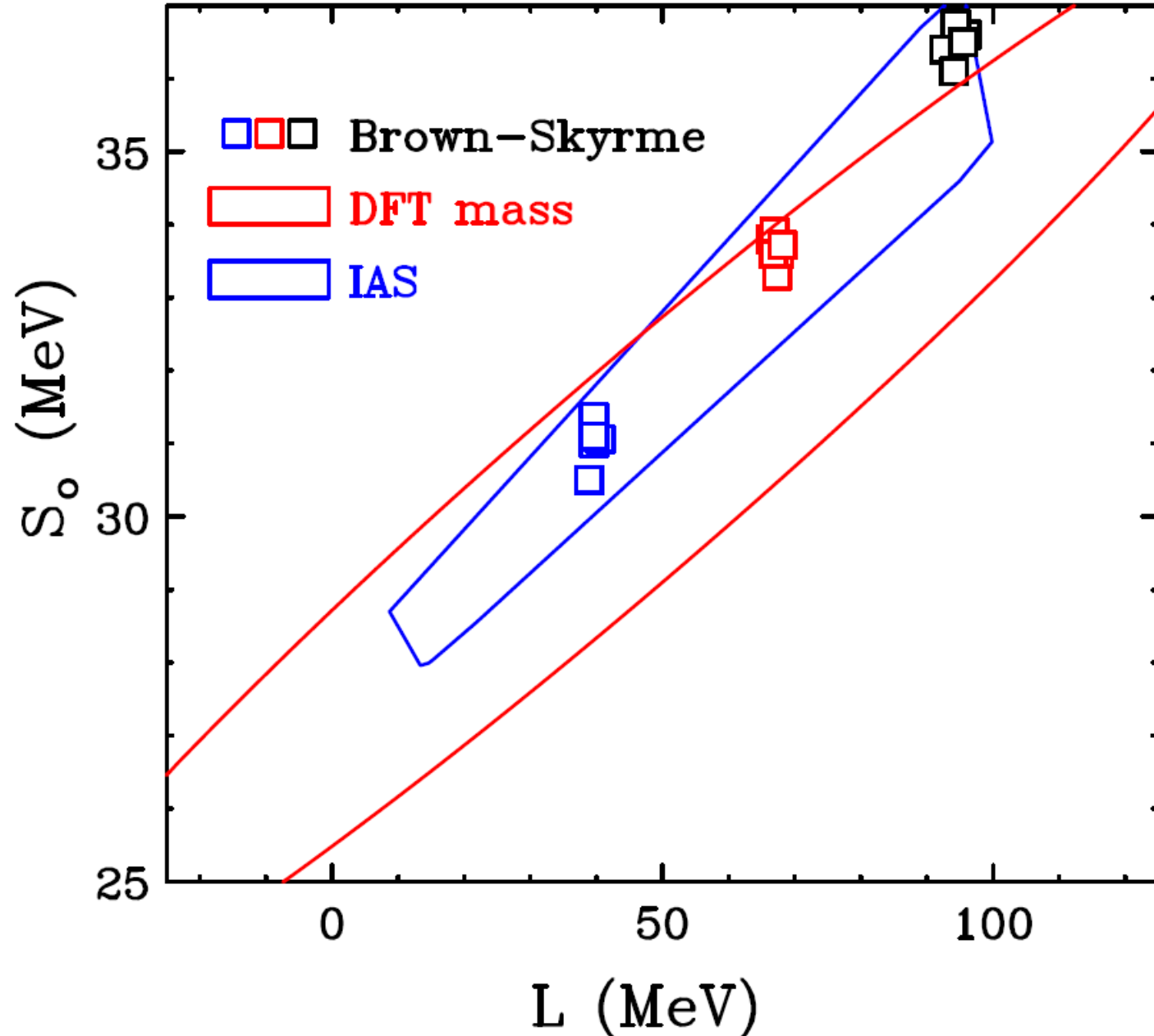
$$S_o = E_{sym} - \frac{L}{3} \left( \frac{\rho_B - \rho_0}{\rho_0} \right) - \frac{K_{sym}}{18} \left( \frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$



Same slope gives you sensitive density region of the observable



# Symmetry Energy Constraints from masses



Skyrme Functionals

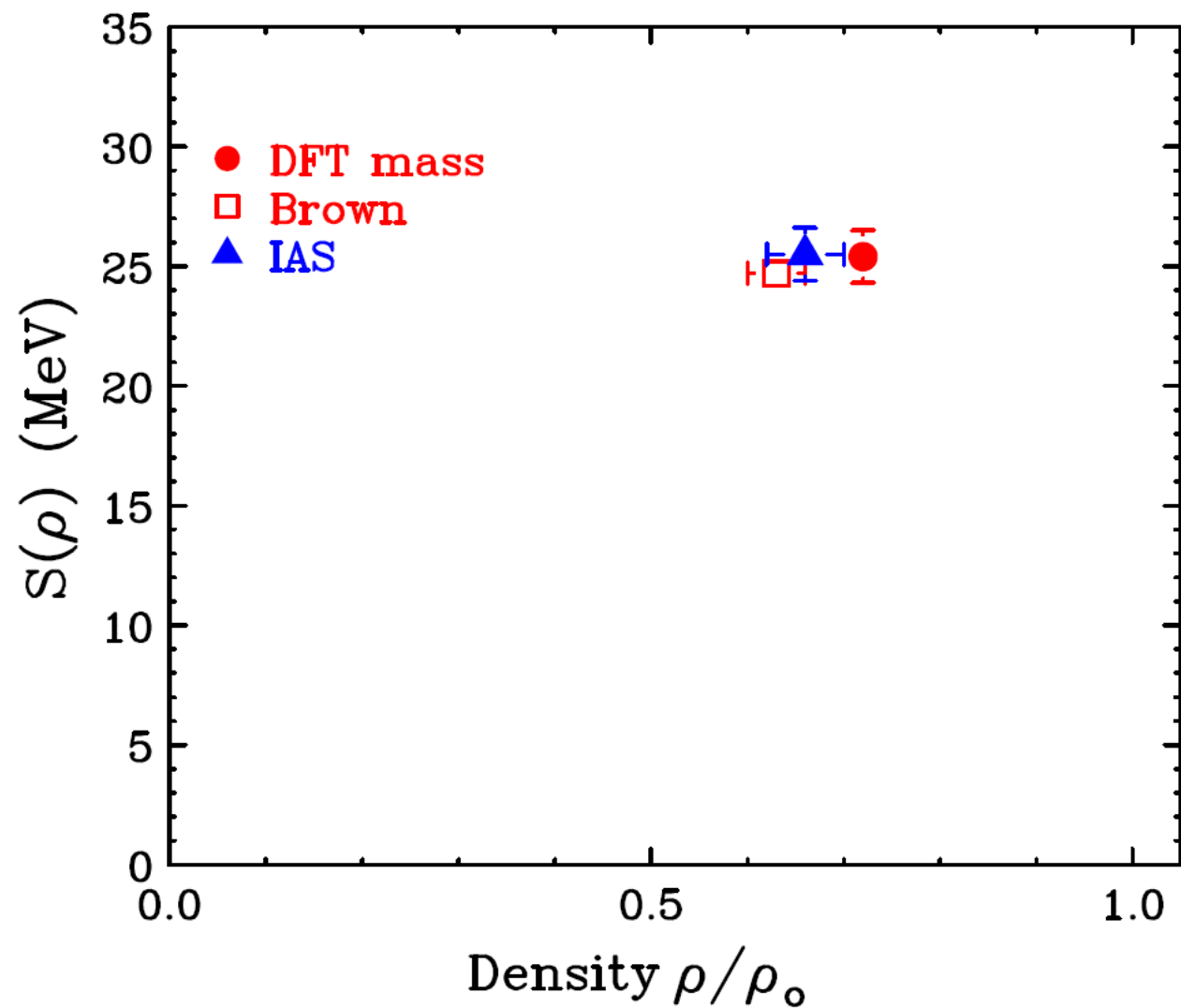
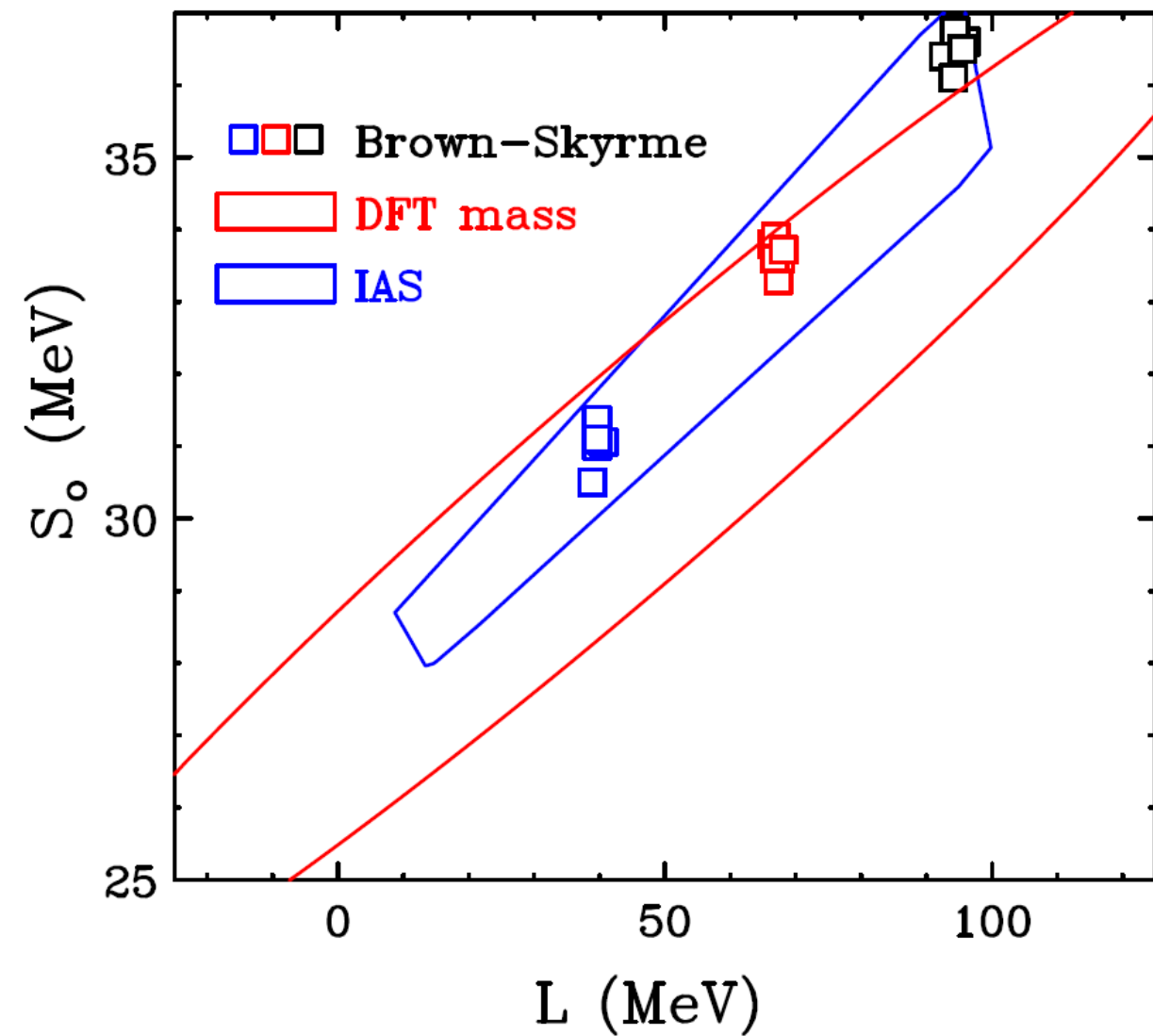
$$S(\rho) = a(\rho/\rho_0) + b(\rho/\rho_0)^{1+\sigma} + c(\rho/\rho_0)^{2/3} + d(\rho/\rho_0)^{5/3}$$

Brown: masses of doubly shell nuclei  
 $\rho_s \sim 0.63 \pm 0.03 \rho_0$   $E_{\text{sym}}(\rho_s) \sim 24.7 \pm 0.8$  MeV

IAS: Isobaric Analog States  
 $\rho_s \sim 0.67 \pm 0.03 \rho_0$   $E_{\text{sym}}(\rho_s) \sim 25.1 \pm 0.9$  MeV

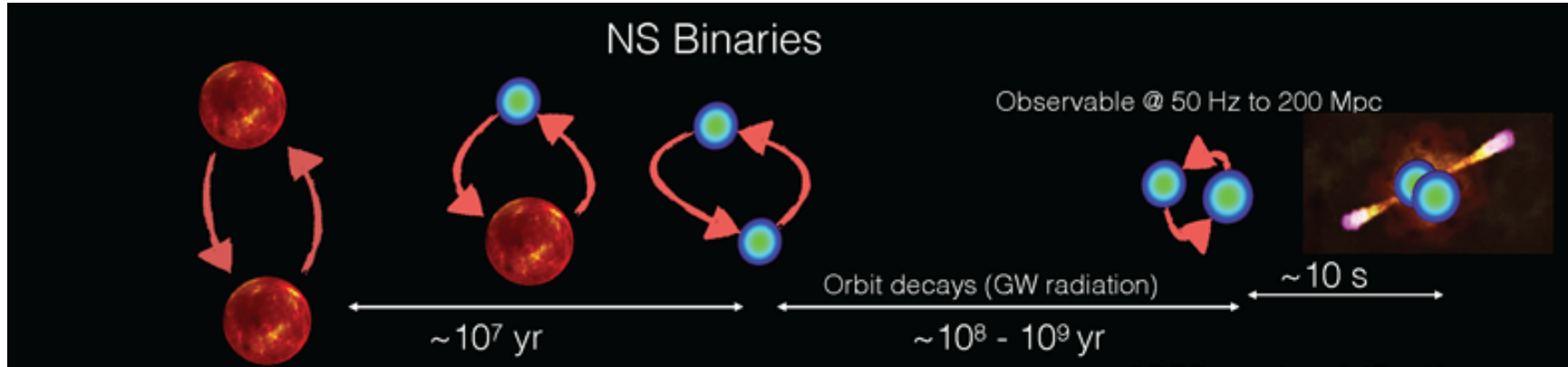
DFT: Density functional theory  
 $\rho_s \sim 0.72 \pm 0.01 \rho_0$   $E_{\text{sym}}(\rho_s) \sim 25.4 \pm 1.1$  MeV

# Symmetry Energy Constraints from masses

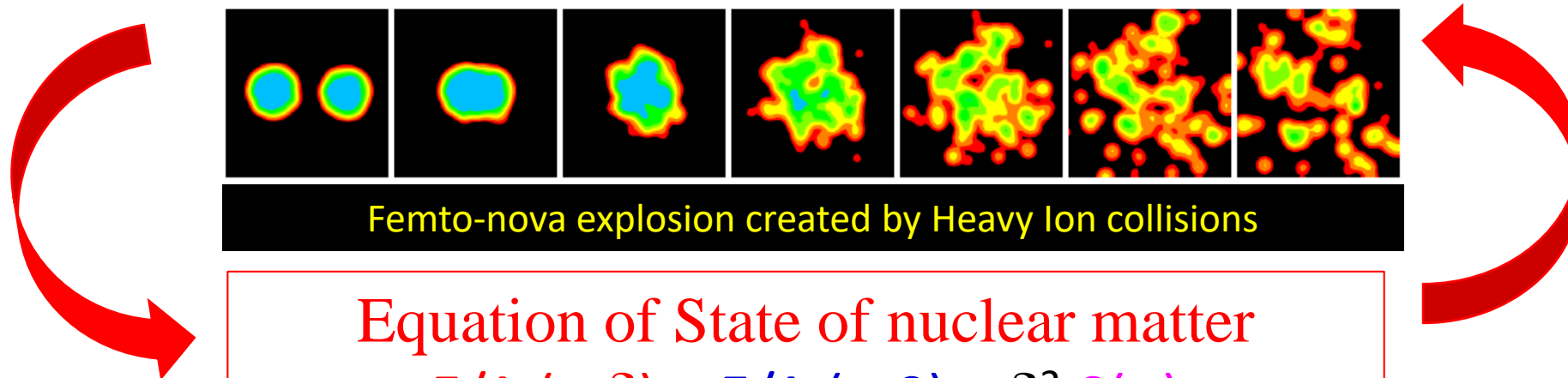


# EOS from dynamics of N-star merger and from nuclear collisions

N-Star merger:  $10^8$  year; Observation Estimates:  $\sim 2/\text{year}$



Nuclear-collisions:  $10^{-21}$  sec;  $10^7$  collisions per experiment

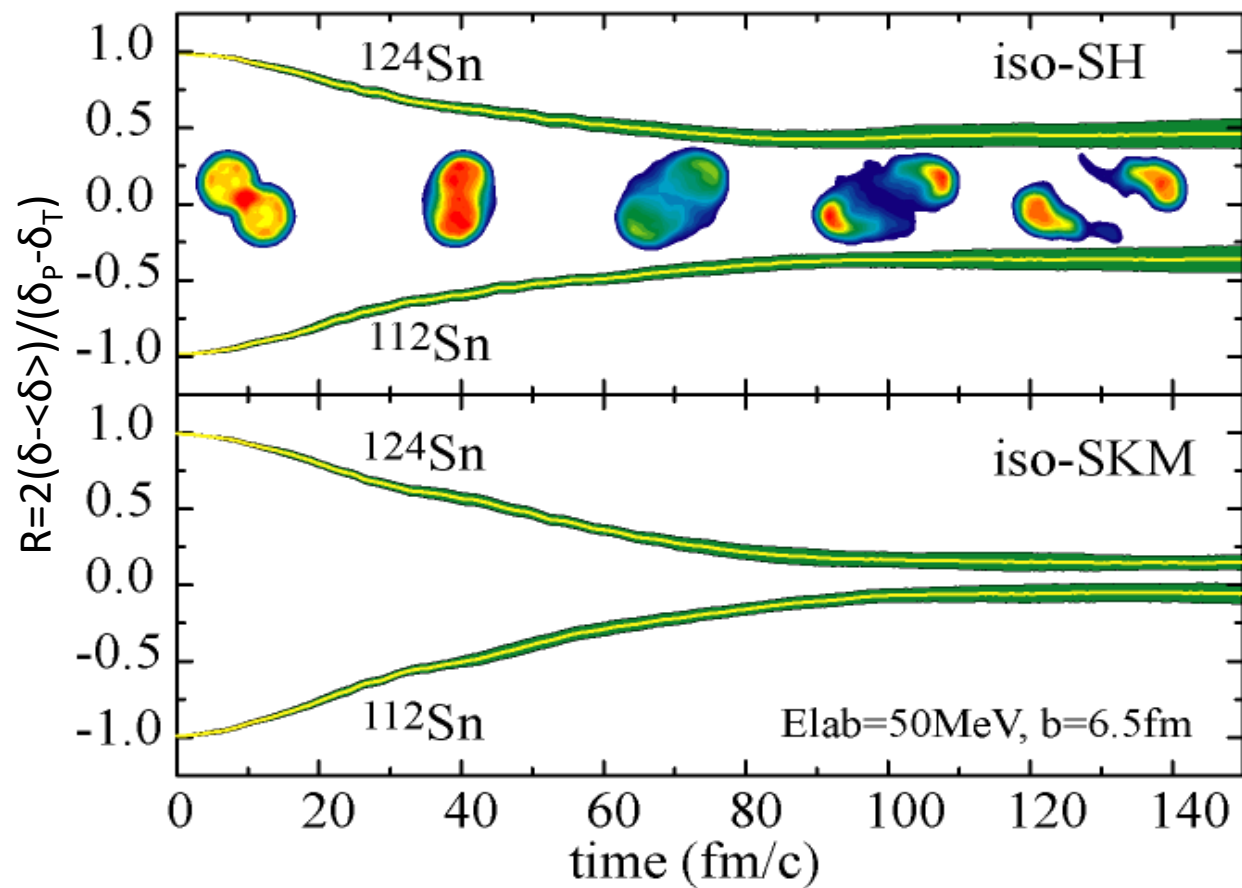
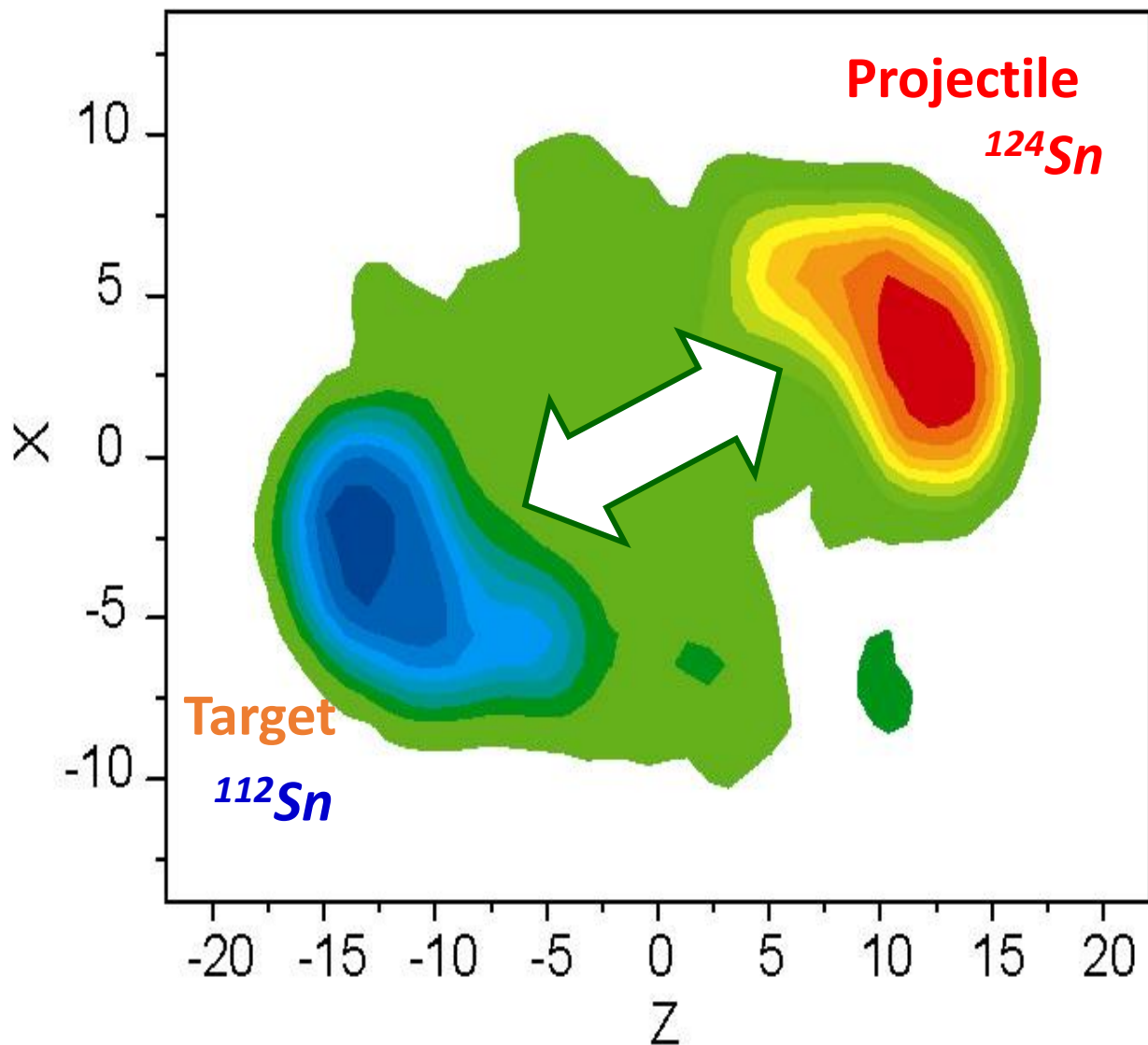


Equation of State of nuclear matter

$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho)$$

$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N - Z) / A$$

# Isospin Diffusion to constrain low density EoS

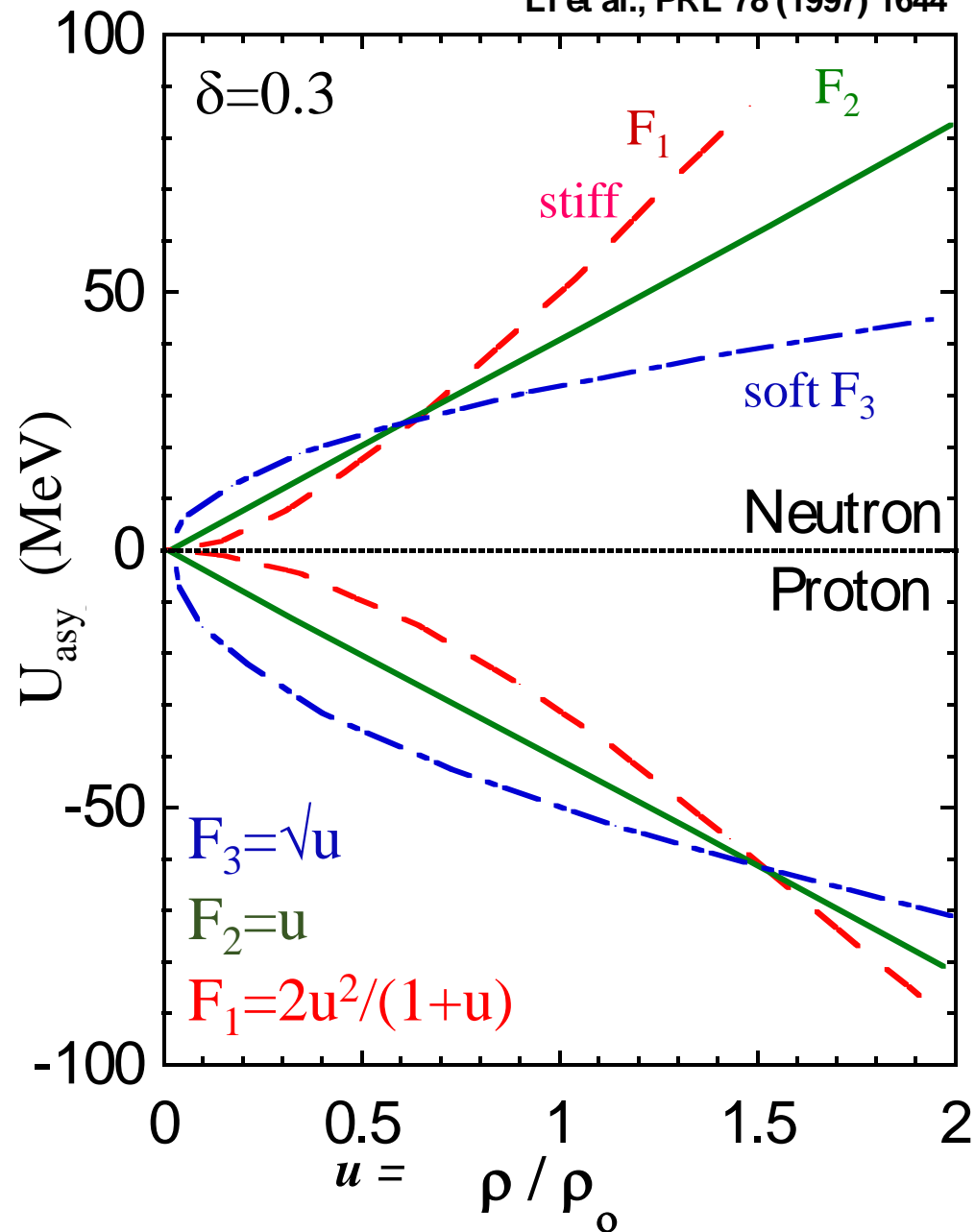


Isospin Diffusion; low  $\rho$ ,  $E_{\text{beam}}$



# Experimental Observables: n/p yield ratios

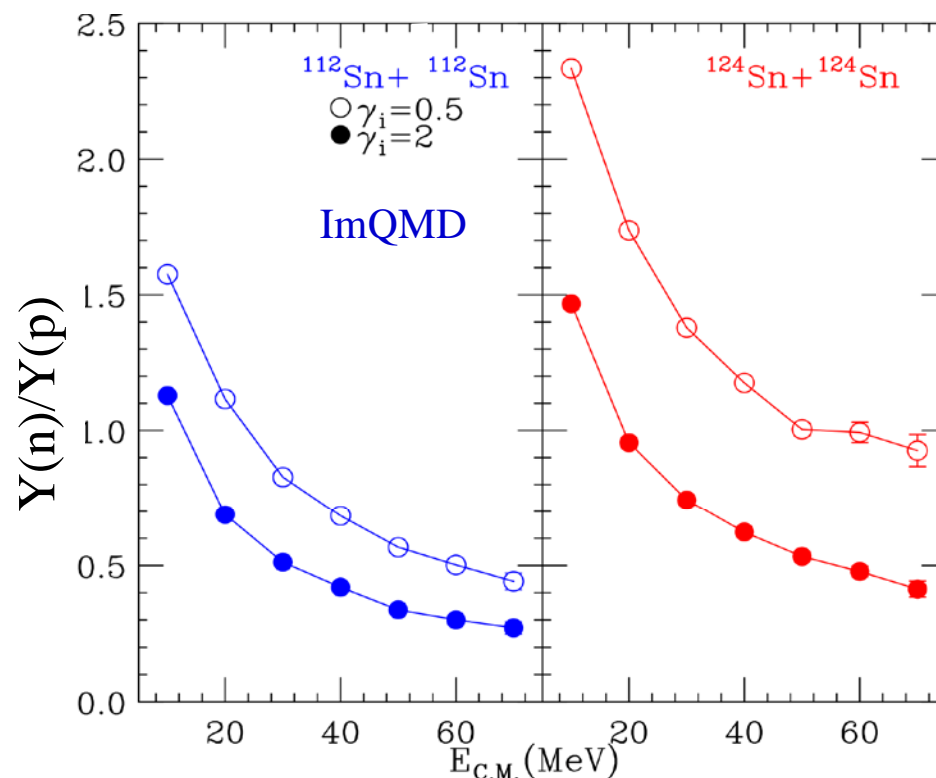
Li et al., PRL 78 (1997) 1644



• *n and p potentials have opposite sign.*

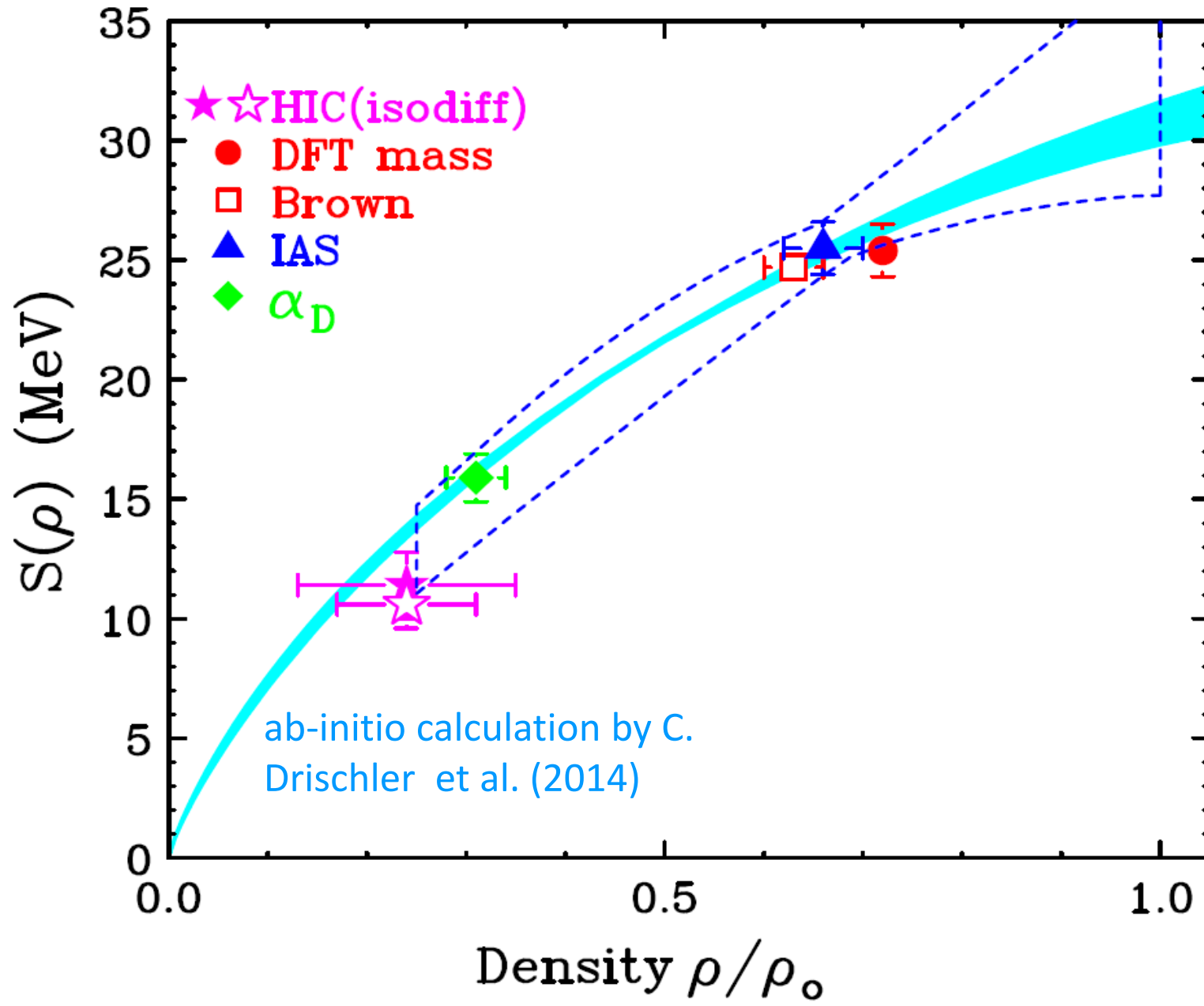
• *n & p energy spectra depend on the symmetry energy  $\rightarrow$  softer density dependence emits more neutrons at low density.*

$$S(\rho) = 12.5(\rho/\rho_0)^{2/3} + 17.6(\rho/\rho_0)^{\gamma_i}$$



• *More n's are emitted from the n-rich system and softer iso-EOS.*

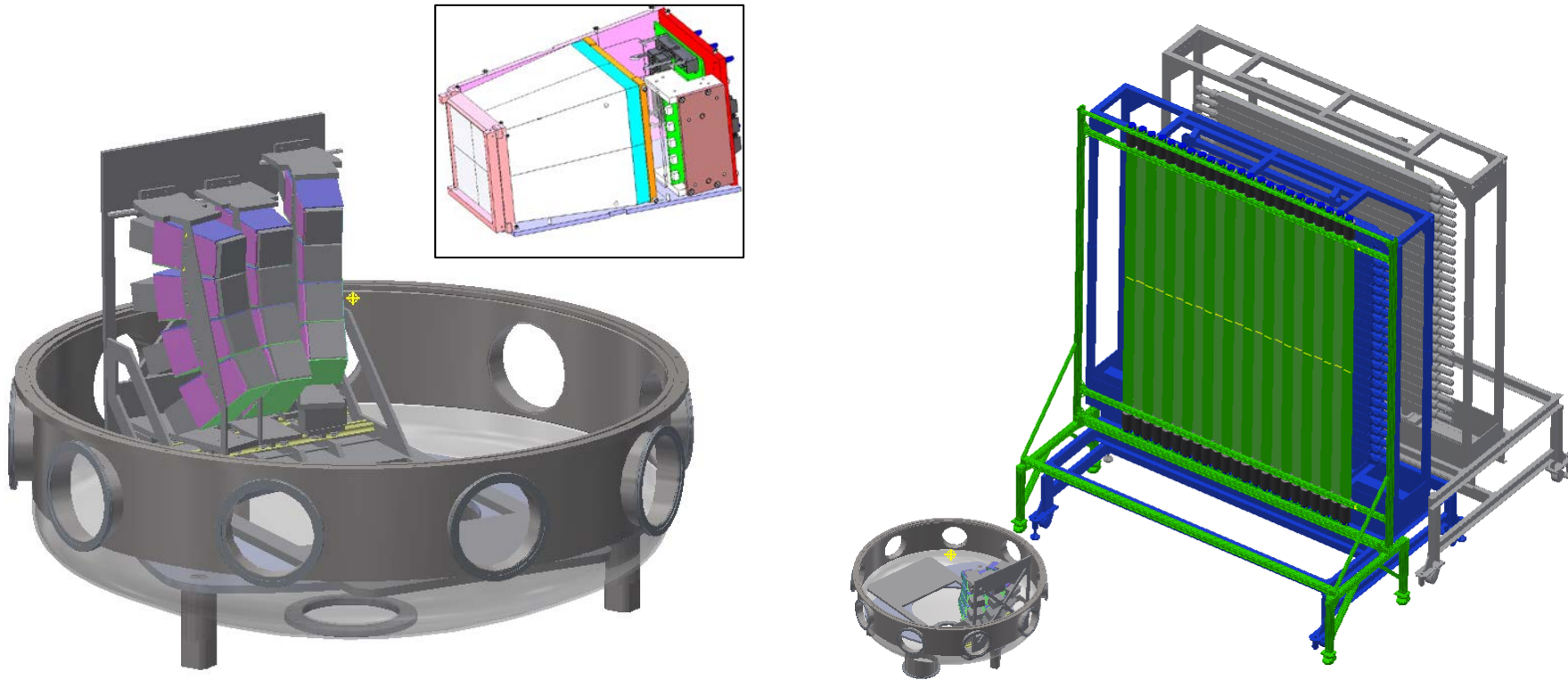
# Density dependence of Symmetry Energy at subsaturation density



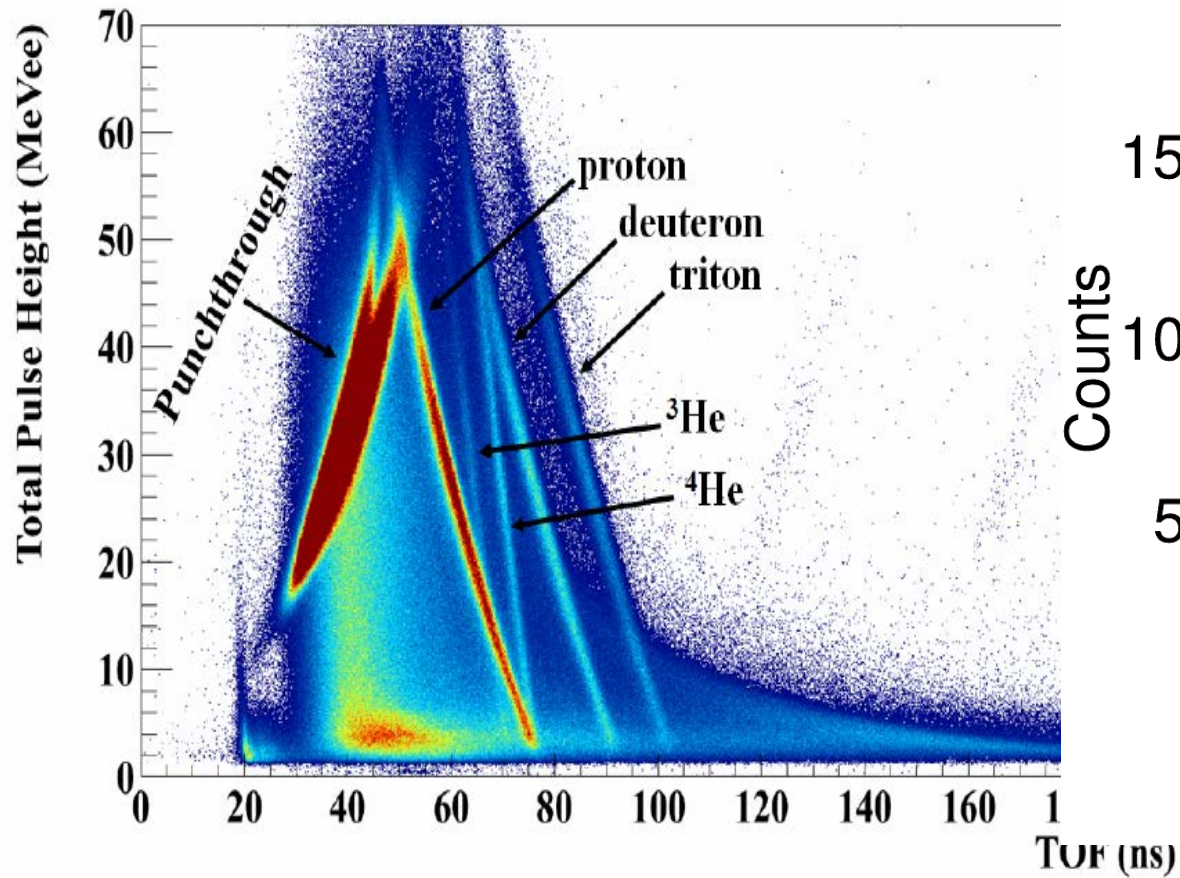
# HiRA upgrade to improve constraints on symmetry energy and $\Delta m^*$

increase CsI from 4 cm to 10 cm;  
the mass splitting effects increase  
with particle energies.

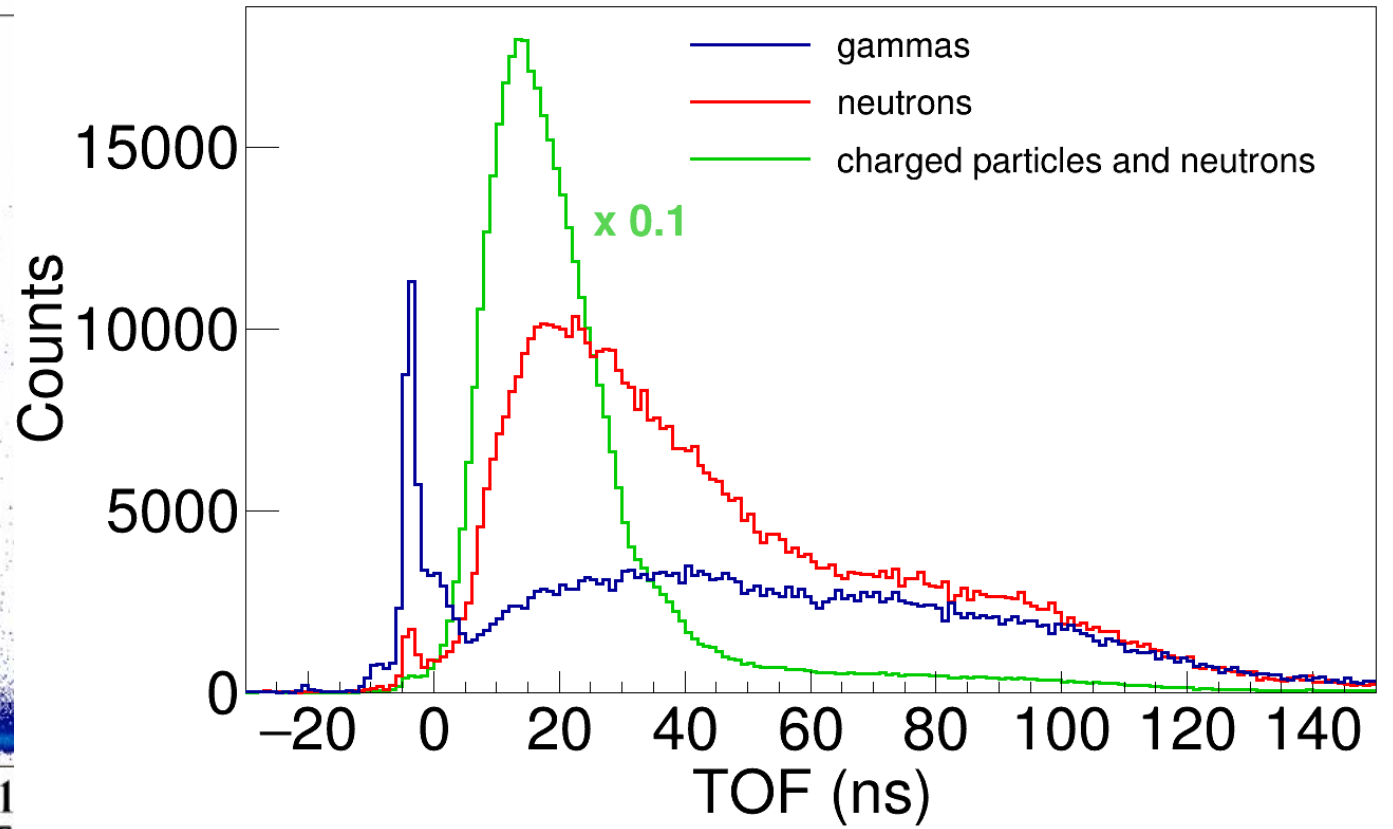
Install a new charged  
particle veto wall in front of  
two neutrons walls



Experiments finished in Feb & March 2018 @ NSCL/MSU



$^{124}\text{Ca}+^{124}\text{Sn}$   $E/A=140$  MeV  
Coupland, 2009



$^{40}\text{Ca}+^{112}\text{Sn}$   $E/A=140$  MeV  
HiRA, 2018

# Experiment e14030/e15190 - RUN LOG



[HOME](#)    
 [List all](#)    
 [Summary](#)    
 [Add run info](#)    
 [Add a comment](#)    
 [Add an event](#)    
 [Plot scaler](#)

Beam	Target	Shadow bars	Avg trigger rate	Total time [HH:MM:SS]
Ca40@56 MeV/u	112Sn	OUT	2107	12:39:56
		IN	2413	18:28:50
		TOTAL	2289/ 256M	31:08:46
Ca40@56 MeV/u	124Sn	OUT	0	0
		IN	2841	08:40:31
		TOTAL	2841/ 88M	08:40:31
Ca40@56 MeV/u	58Ni	OUT	2558	16:26:05
		IN	2694	21:05:26
		TOTAL	2635/ 355M	37:31:31
Ca40@56 MeV/u	64Ni	OUT	0	0
		IN	2751	08:05:27
		TOTAL	2751/ 80M	08:05:27
Ca40@140 MeV/u	112Sn	OUT	2168	08:25:27
		IN	2016	43:53:08
		TOTAL	2041/ 384M	52:18:35
Ca40@140 MeV/u	124Sn	OUT	3057	07:56:28
		IN	198	10:52:46
		TOTAL	1404/ 95M	18:49:14
Ca40@140 MeV/u	58Ni	OUT	3651	12:26:46
		IN	2931	32:24:36
		TOTAL	3131/ 505M	44:51:22
Ca40@140 MeV/u	64Ni	OUT	0	0
		IN	2915	11:28:46
		TOTAL		

Beam	Target	Shadow bars	Avg trigger rate	Total time [HH:MM:SS]
Ca48@56 MeV/u	112Sn	OUT	2812	06:39:33
		IN	2756	08:00:24
		TOTAL	2781/ 146M	14:39:57
Ca48@56 MeV/u	124Sn	OUT	2558	26:06:27
		IN	2756	23:52:39
		TOTAL	2653/ 477M	49:59:06
Ca48@56 MeV/u	58Ni	OUT	2619	05:41:13
		IN	2691	08:00:10
		TOTAL	2661/ 131M	13:41:23
Ca48@56 MeV/u	64Ni	OUT	2762	25:40:37
		IN	2824	29:27:25
		TOTAL	2795/ 554M	55:08:02
Ca48@140 MeV/u	112Sn	OUT	2332	06:07:25
		IN	2435	07:05:39
		TOTAL	2387/ 113M	13:13:04
Ca48@140 MeV/u	124Sn	OUT	2590	18:33:19
		IN	2229	27:50:59
		TOTAL	2373/ 396M	46:24:18
Ca48@140 MeV/u	58Ni	OUT	2353	07:34:11
		IN	2334	06:54:51
		TOTAL	2344/ 122M	14:29:02
Ca48@140 MeV/u	64Ni	OUT	2705	18:26:12
		IN	2273	27:55:13
		TOTAL		

Ca48@140 MeV/u	124Sn	OUT	2590	18:33:19
		IN	2229	27:50:59
		TOTAL	2373/ 396M	46:24:18
Ca40@140 MeV/u	112Sn	OUT	2168	08:25:27
		IN	2016	43:53:08
		TOTAL	2041/ 384M	52:18:35

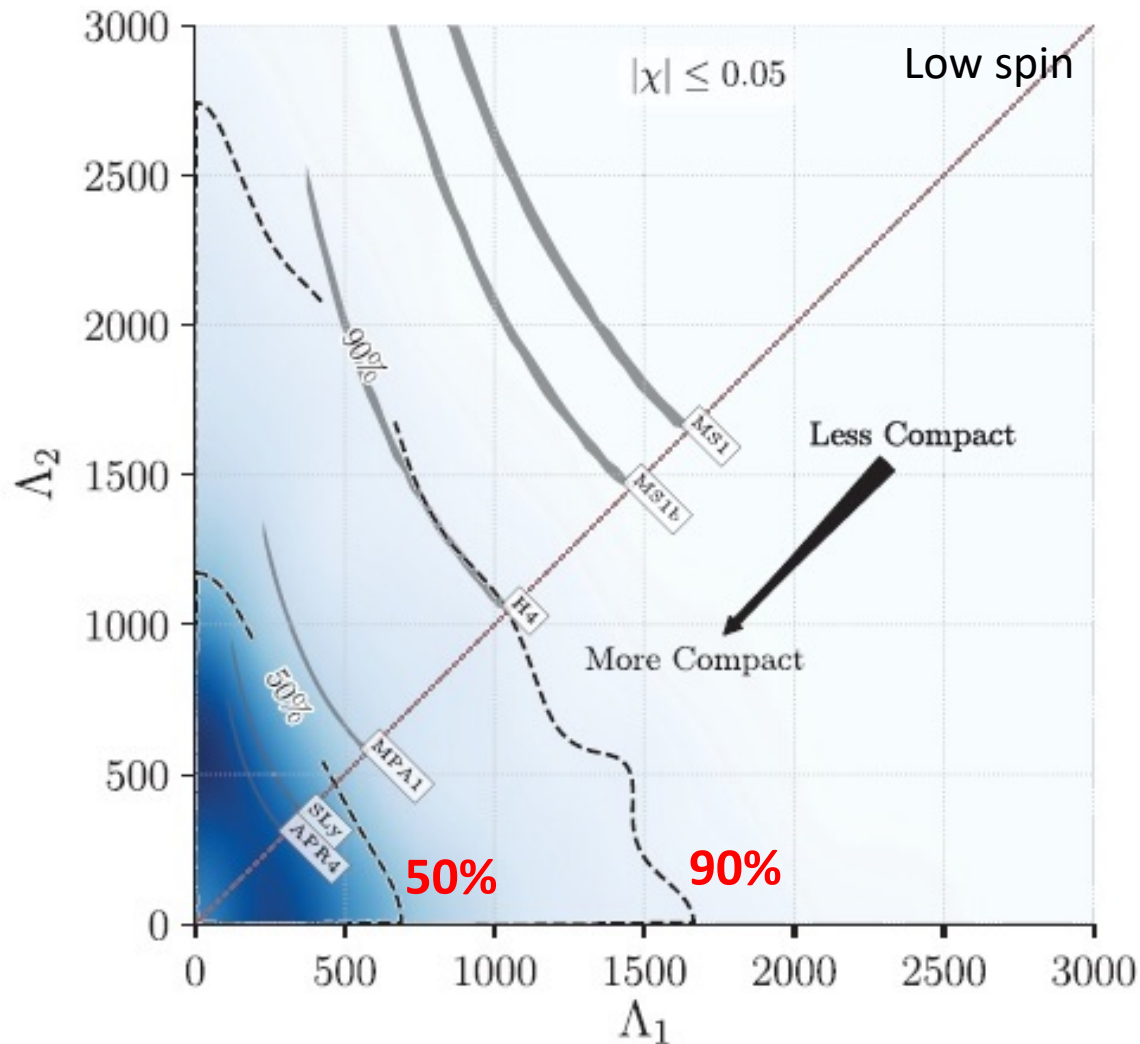
$$\Lambda = \frac{2}{3}k_2 \left( \frac{c^2 R}{GM} \right)^5 = \frac{64}{3}k_2 \left( \frac{R}{R_s} \right)^5$$

$$\tilde{\Lambda} = \frac{16}{13} \left[ \frac{(M_1 + 12M_2)M_1^4}{(M_1 + M_2)^5} \Lambda_1 + \frac{(M_2 + 12M_1)M_2^4}{(M_1 + M_2)^5} \Lambda_2 \right]$$

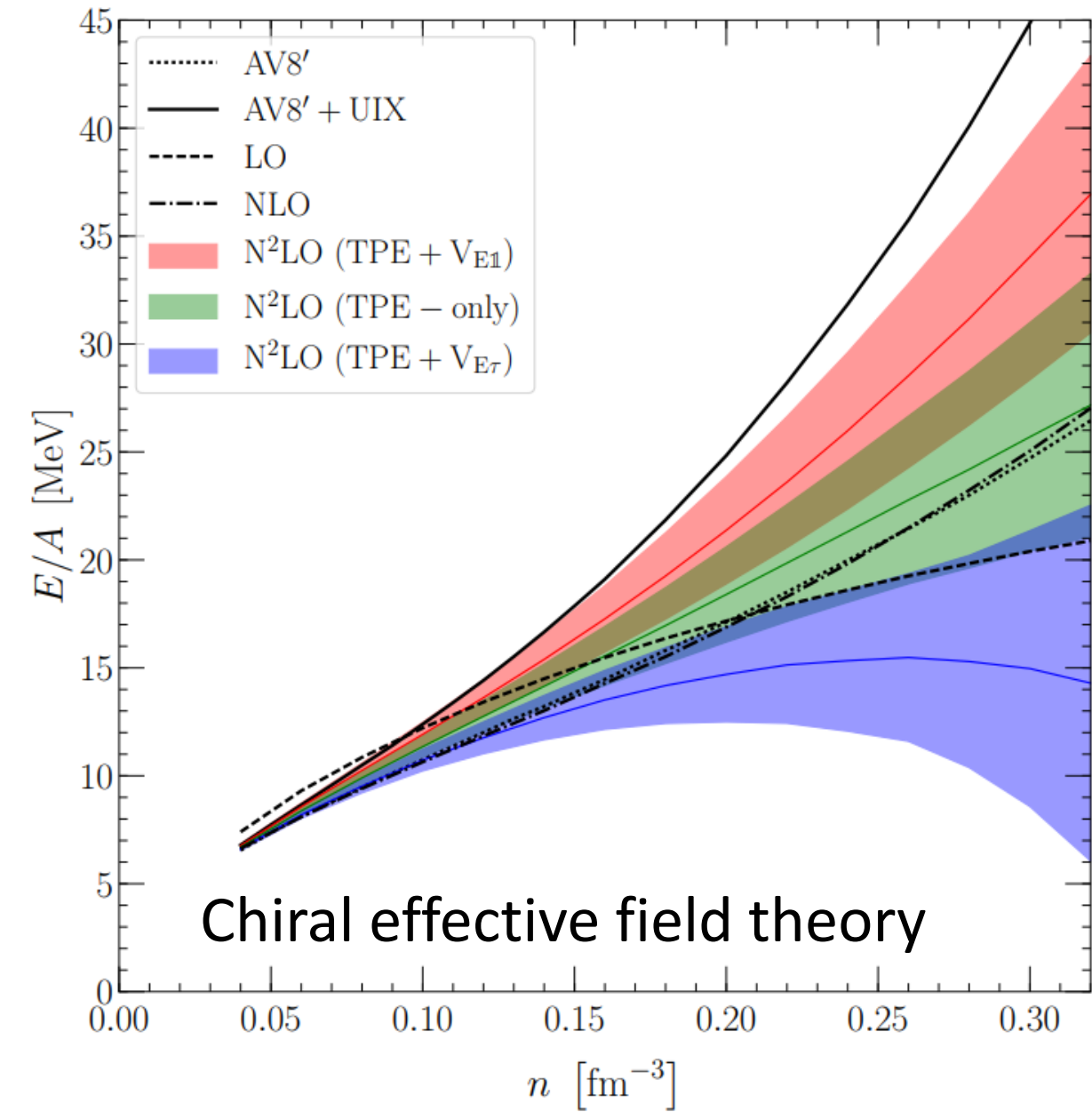
<800 (90% confidence)

$\tilde{\Lambda}$ : Preliminary analysis, waiting for updates from more sophisticated analysis (Ben Lackey)

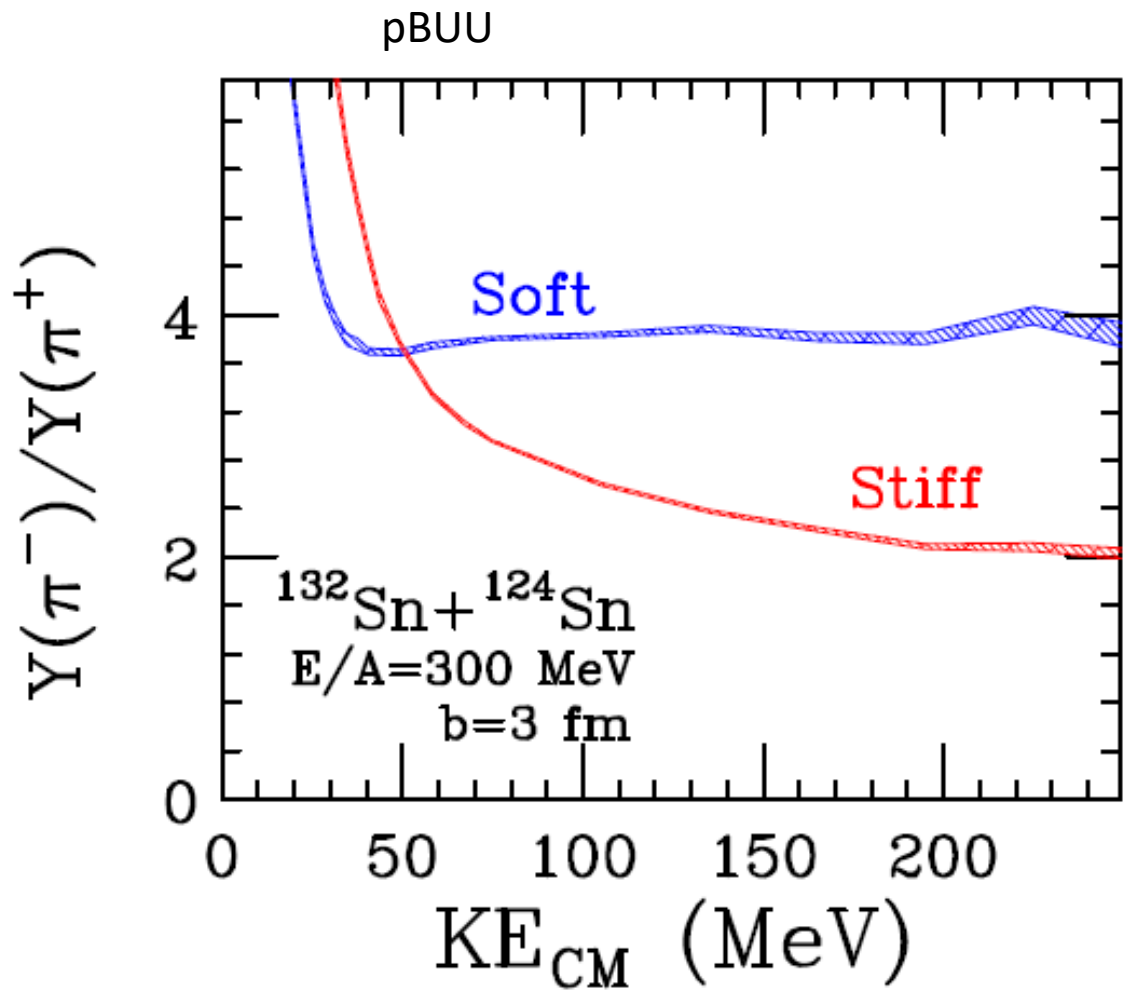
With high uncertainties e.g. include correlation between  $M_2$  and  $M_1$   
800 → 1100 (Lattimer)



The binary tidal deformability  
 $R(NS) < 13.76$  km



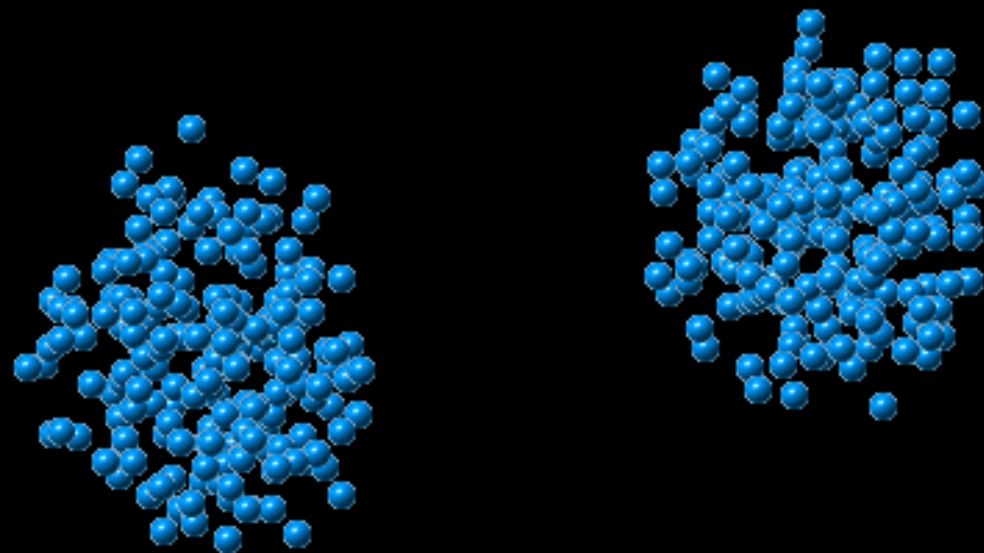
Tews et al Arxiv:1801.01923



0.00 fm/c

Au+Au collisions  
 400 MeV/u  
 b=5 fm

Nucleon   
 Baryon   
 Meson 



YongJia Wang URQMD

0 5 fm



# Experimental Setup

Primary	Beam	Target	$E_{\text{beam}}/A$	$\delta_{\text{sys}}$	evt(M)	2016
$^{124}\text{Xe}$	$^{108}\text{Sn}$	$^{112}\text{Sn}$	269	0.09	8	4/30-5/4
	$^{112}\text{Sn}$	$^{124}\text{Sn}$	270	0.15	5	5/4-5/6
$^{238}\text{U}$	$^{132}\text{Sn}$	$^{124}\text{Sn}$	269	0.22	9	5/25-5/29
	$^{124}\text{Sn}$	$^{112}\text{Sn}$	270	0.15	5	5/30-6/1
<b>Z=1,2,3</b>			<b>100, 200</b>		<b>0.6</b>	<b>6/1</b>





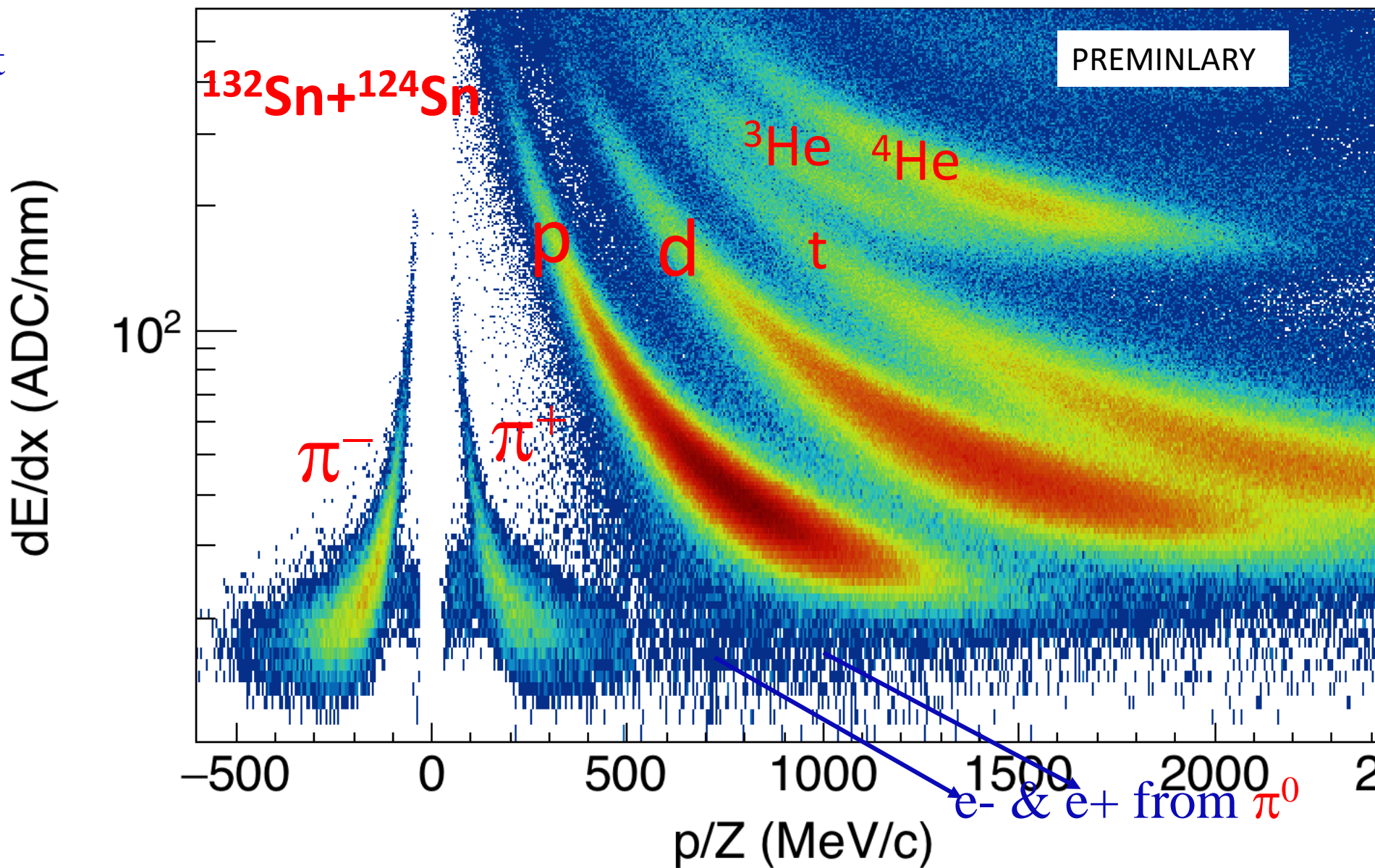
### On Site Experimenters

- J. Barney (MSU)
  - G. Cerizza (MSU)
  - J. Estee (MSU)
  - B. Hong (Korea U)
  - T. Isobe (RIKEN)\*
  - G. Jhang (Korea U)
  - M. Kaneko (Kyoto U)
  - M. Kurata-Nishimura (RIKEN)
  - P. Lasko (IFN, Krakow)
  - H. Lee (RISP)
  - J. Lee (Korea U)
  - J. Lukasik (IFN, Krakow)
  - W. Lynch (MSU)\*
  - A. McIntosh (TAMU)
  - P. Morfouace (MSU)
  - T. Murakami (Kyoto U)\*
  - S. Nishimura (RIKEN)
  - P. Pawlowski (IFN, Krakow)
  - C. Santamaria (MSU)
  - R. Shane (MSU)
  - D. Suzuki (RIKEN)
  - B. Tsang (MSU)\*
  - Y. Zhang (Tsinghua U)
- \*spokespersons

Other Participants: H. Baba, Chica, Ichihara, Kondo, T. Nakamura, H. Otsu, Saito, Togano  
NeuLAND Collaboration: Leyla Atar, Tom Aumann, Igor Gasparic, A. Horvat, H. Scheit

Need more analysis and understanding especially on detector and analysis efficiencies

Symmetry energy is not an observable. We have to use transport models to simulate the reactions and compare to data. Mean field (symmetry energy) plus others parameters are input to the transport models. Need to have different transport models under control?



# Transport Code Evaluation Project

## Writing group

B. Tsang, H. Wolter, Y.X. Zhang<sup>2</sup>, J. Xu<sup>1</sup>, M. Colonna, P. Danielewicz, A Ono, Y.J. Wang

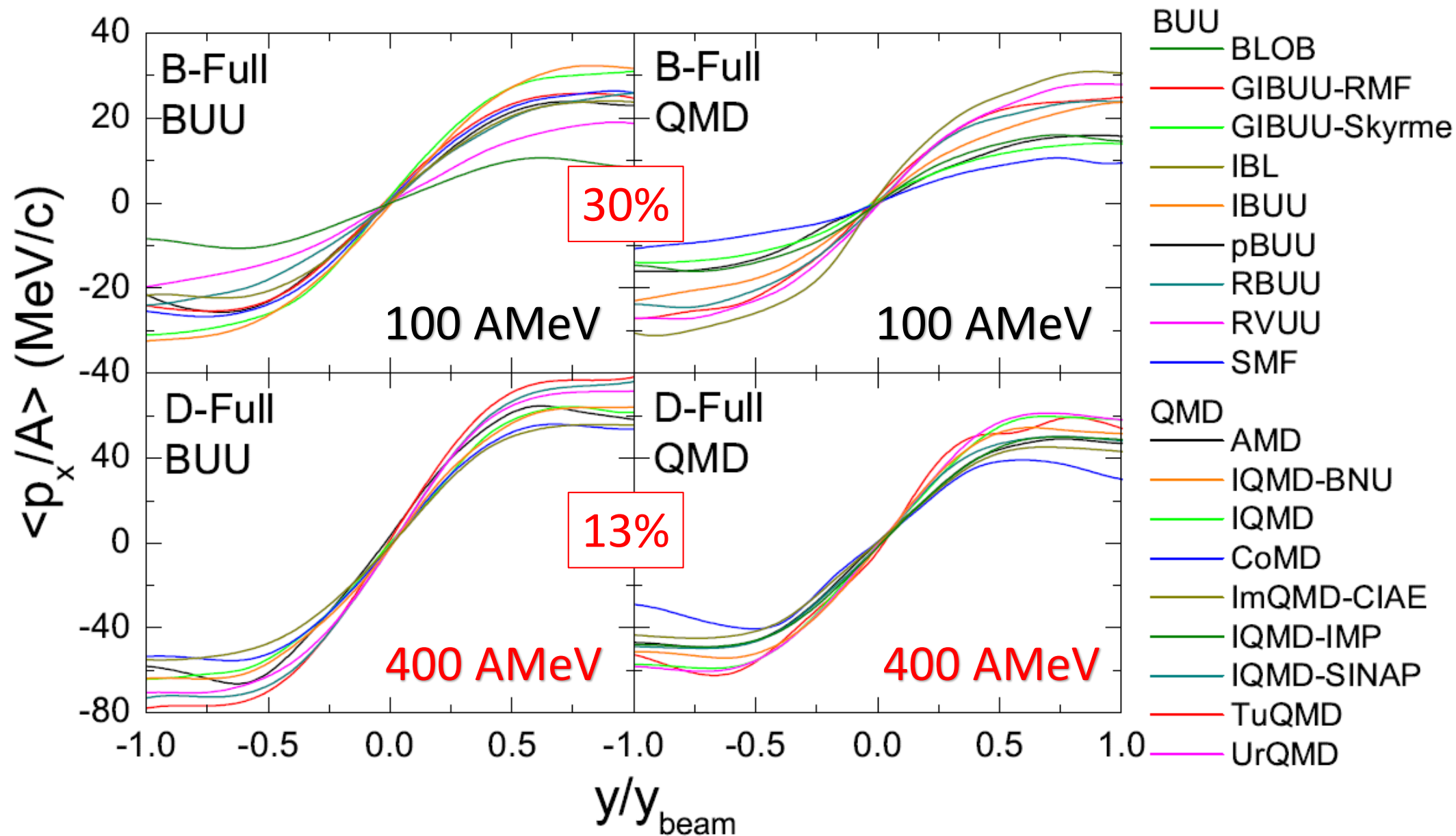
BUU Type	Code	Box			
		flow	cas	Vlas	pion
		pub	pub		
BUU-VM <sup>a</sup>	S. Mallik		X	X	X
BLOB	P. Napolitani	X			
GIBUU-RMF	J. Weil	X	X		
GIBUU-Sky	J. Weil	X			
IBL	W.J. Xie	X			
IBUU	J. Xu	X	X	X	X
pBUU	Danielewicz	X	X	X	X
RBUU	K. Kim	X			
RVUU	C.M. Ko	X	X	X	X
SMASH	Oliinychenko		X		
SMF	M. Colonna	X	X	X	X

QMD Type	Code	Box			
		flow	cas	Vlas	pion
		pub	pub		
ImQMD	Y.X. Zhang	X	X	X	
IQMD-BNU	J. Su	X	X	X	
IQMD	C. Hartnack	X			
IQMD-IMP	Z.Q. Feng	X	X	X	X
IQMD-SINAP	G.Q. Zhang	X			
JAM	A. Ono		X	X	X
JQMD	T. Ogawa		X	X	X
TuQMD	D. Cozma	X	X	X	X
UrQMD	Y.J. Wang	X	X	X	X

**Pub: Xu et al., PRC.93.044609 (2016)**

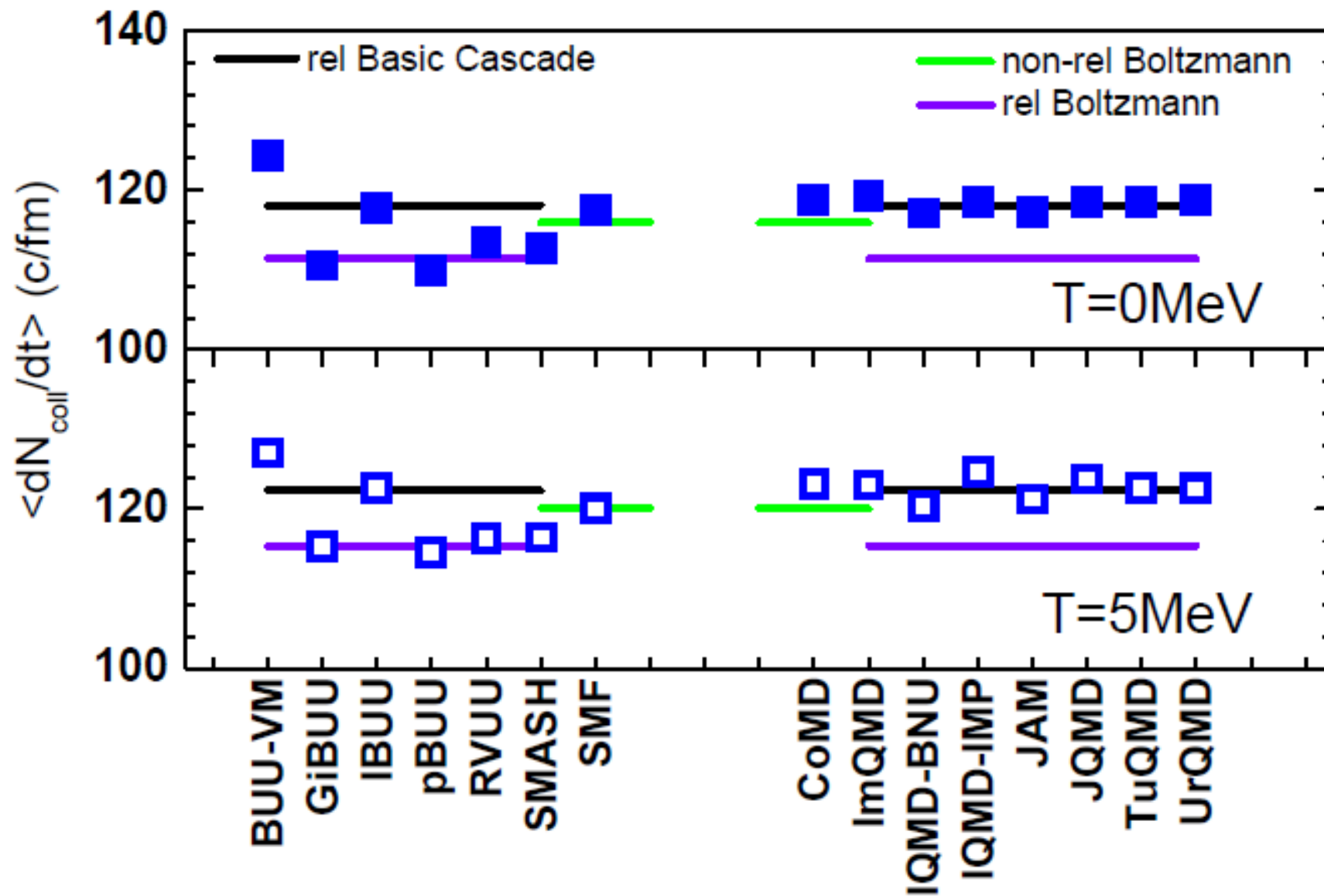
**Pub : Zhang et al., PRC 97, 035505 (2017)**

# Code Evaluation Project I, PhysRevC.93.044609



# Code Evaluation Project II -- Box Simulations on Collisions w/wo Pauli Blocking

Comparison to Analytical limits : Zhang et al., arXiv:1711.05950



Without Pauli Blocking  
Collisions well controlled.

# Transport Code Evaluation Project

## Writing group

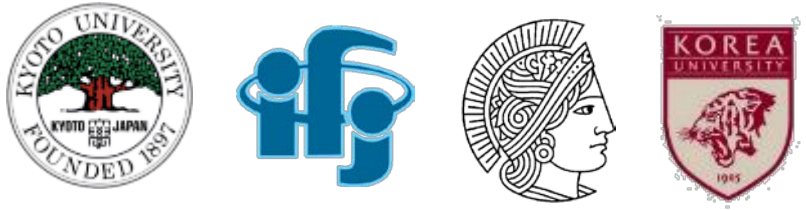
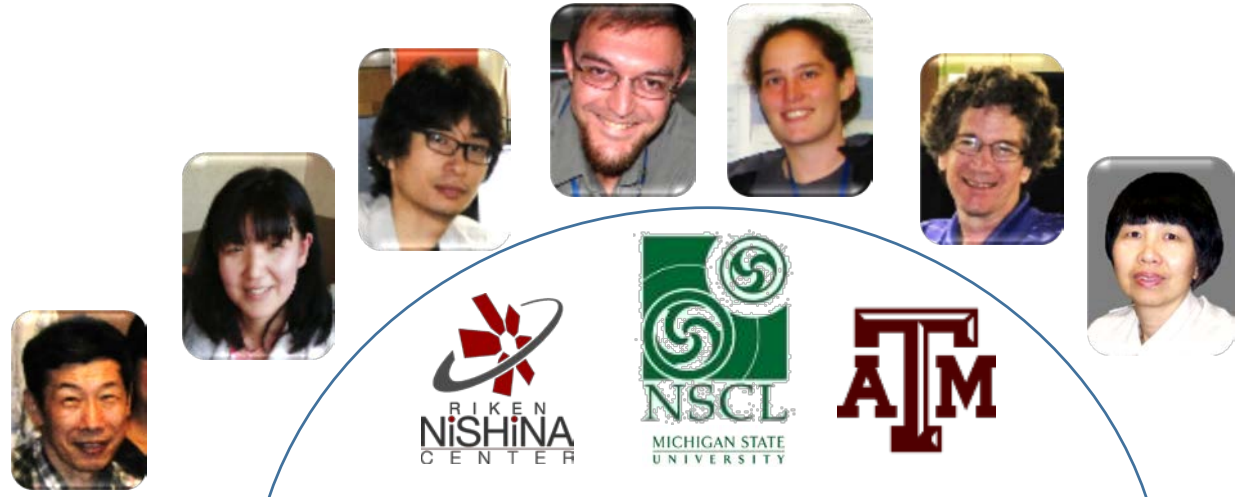
B. Tsang, H. Wolter, Y.X. Zhang<sup>2</sup>, J. Xu<sup>1</sup>, M. Colonna, P. Danielewicz, A Ono, Y.J. Wang

BUU Type	Code	Box			
		flow	cas	Vlas	pion
		pub	pub		
BUU-VM <sup>a</sup>	S. Mallik		X	X	X
BLOB	P. Napolitani	X			
GIBUU-RMF	J. Weil	X	X		
GIBUU-Sky	J. Weil	X			
IBL	W.J. Xie	X			
IBUU	J. Xu	X	X	X	X
pBUU	Danielewicz	X	X	X	X
RBUU	K. Kim	X			
RVUU	C.M. Ko	X	X	X	X
SMASH	Oliinychenko		X		
SMF	M. Colonna	X	X	X	X

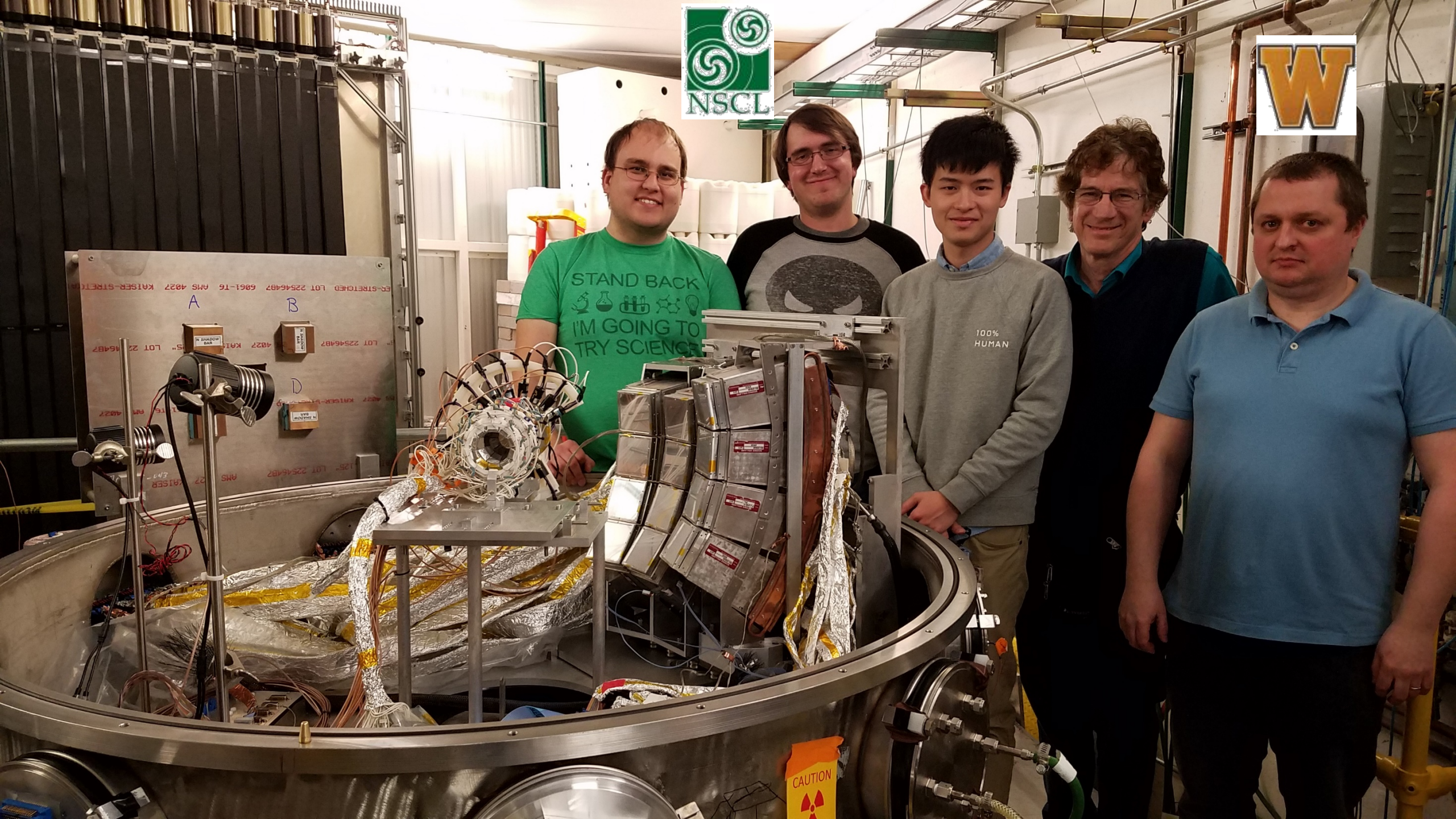
QMD Type	Code	Box			
		flow	cas	Vlas	pion
		pub	pub		
ImQMD	Y.X. Zhang	X	X	X	
IQMD-BNU	J. Su	X	X	X	
IQMD	C. Hartnack	X			
IQMD-IMP	Z.Q. Feng	X	X	X	X
IQMD-SINAP	G.Q. Zhang	X			
JAM	A. Ono		X	X	X
JQMD	T. Ogawa		X	X	X
TuQMD	D. Cozma	X	X	X	X
UrQMD	Y.J. Wang	X	X	X	X

**Pub: Xu et al., PRC.93.044609 (2016)**

**Pub : Zhang et al., PRC 97, 035505 (2017)**







# Summary and Outlook

- Laboratory measurements have provided constraints on the symmetry energy and the equation of state for neutron-rich matter.
  - Significant constraints at sub-saturation densities.
  - Constraints on effective mass splitting around and above saturation densities.
- The important density range of  $\rho_0 \leq \rho \leq 2\rho_0$  is accessible via heavy ion reaction.
  - Experimental results from SpiRIT!
- Improving the reliability of transport theory predictions.
  - Code evaluation project is making significant progress in this direction.
- Need to connect our EoS results to the neutron star merger results