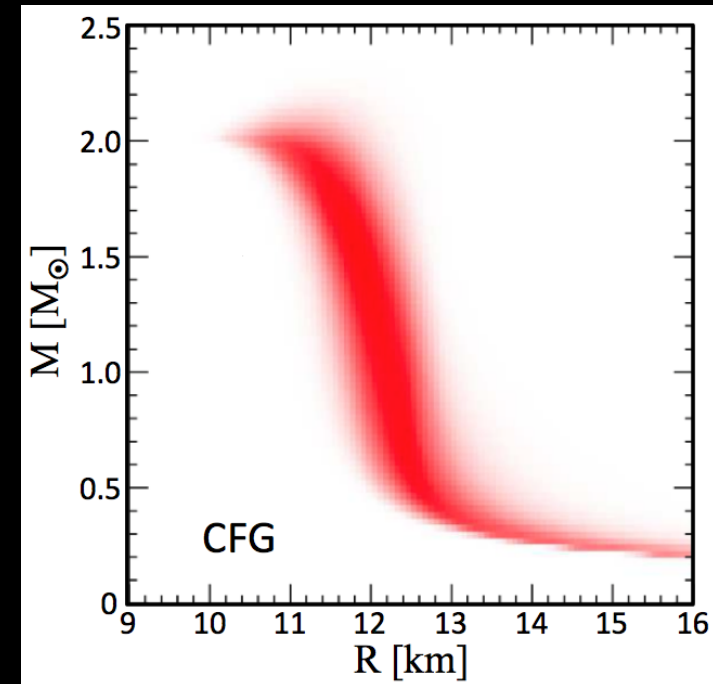
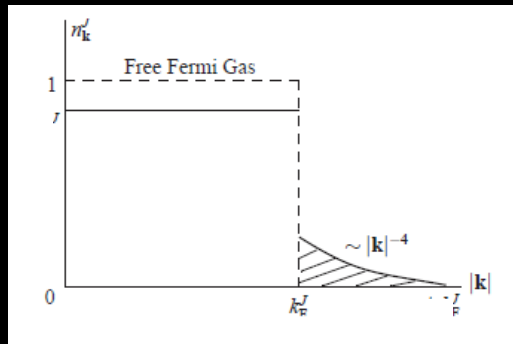


# 6th International Symposium on Nuclear Symmetry Energy (NuSYM16)

June 13- June 17, 2016, Tsinghua University, Beijing, China

## Analysis of Neutron Stars Observations Using a Correlated Fermi Gas Model

O. Hen, A.W. Steiner, E. Piasezky,  
and L.B. Weinstein



# Short Range (tensor) Correlations in nuclei

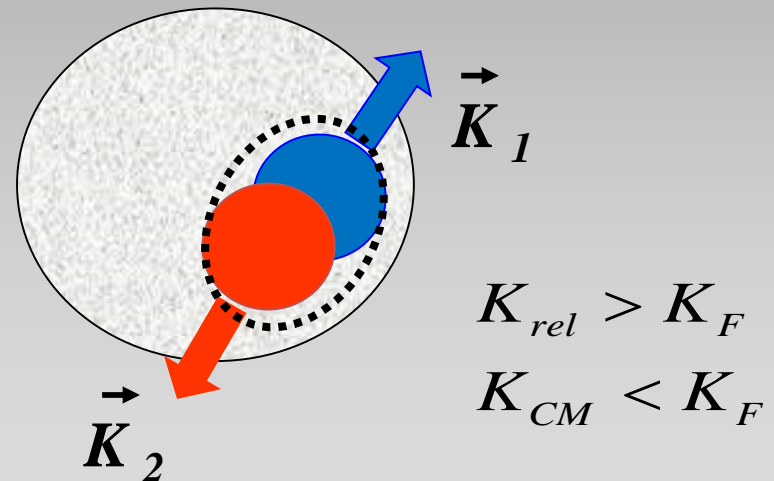
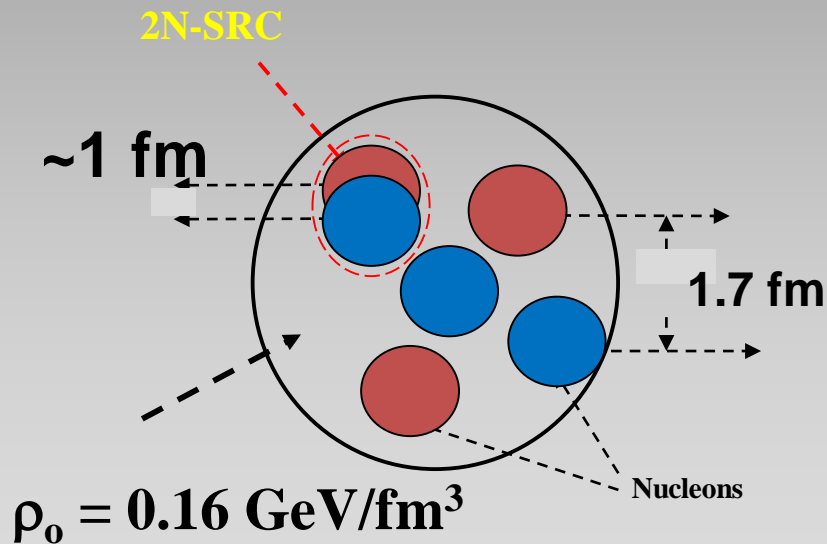
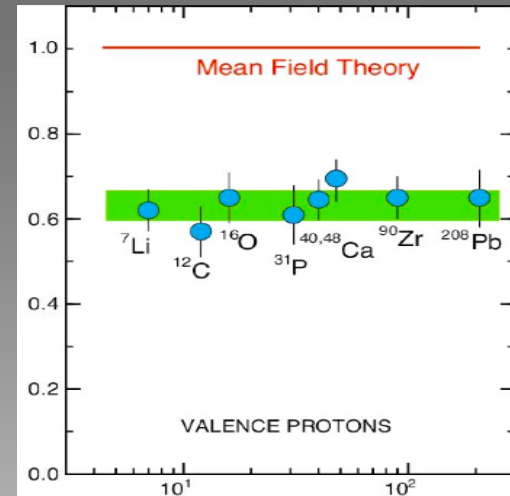
## Hard Semi inclusive scattering

$A(e, e'p)$

Only 60-70% of the expected single-particle strength.



SRC and LRC



# Short Range (tensor) Correlations in nuclei

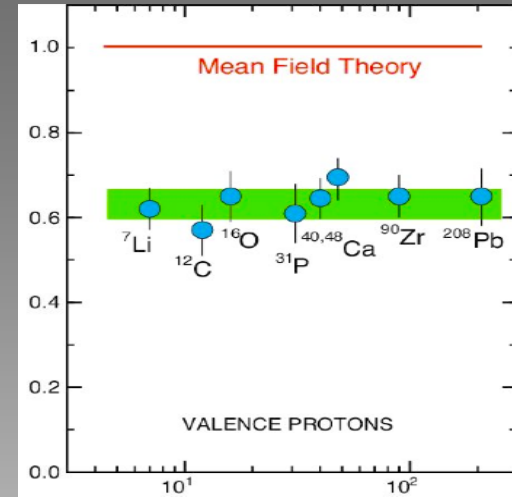
## Hard Semi inclusive scattering

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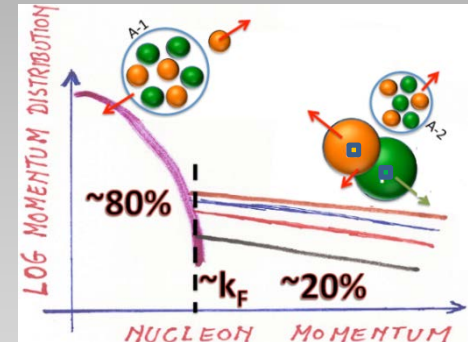
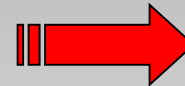
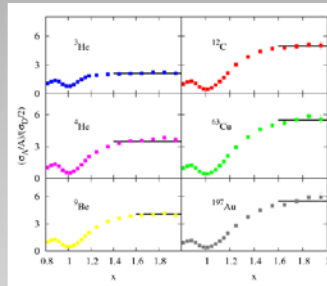


SRC and LRC



## Hard inclusive scattering

$$A(e, e')$$



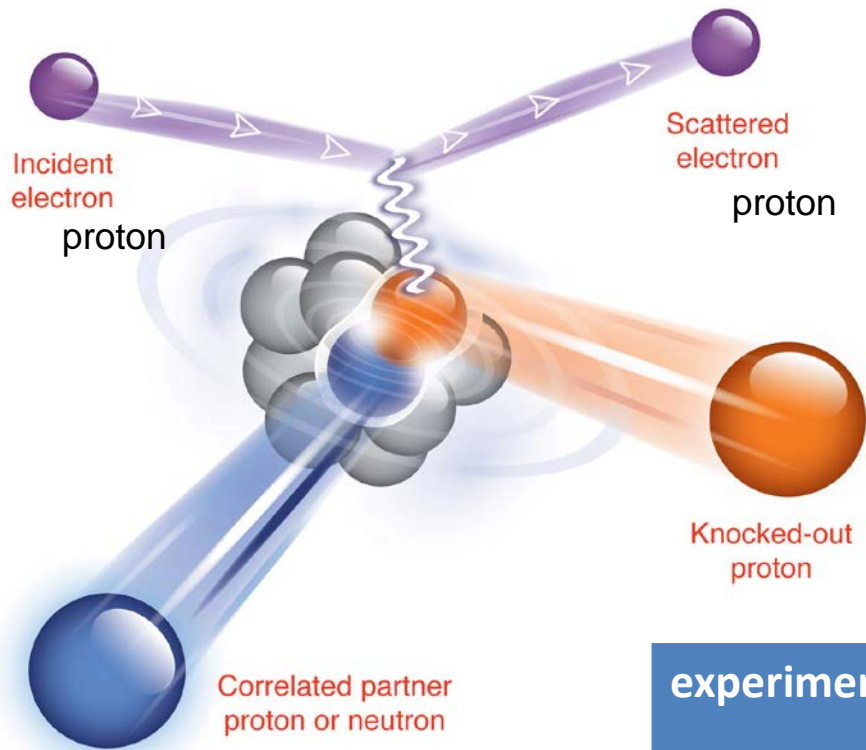
This 20-25 % includes all three isotopic compositions (pn, pp, or nn) for the 2N-SRC phase in <sup>12</sup>C.



## Hard exclusive scattering

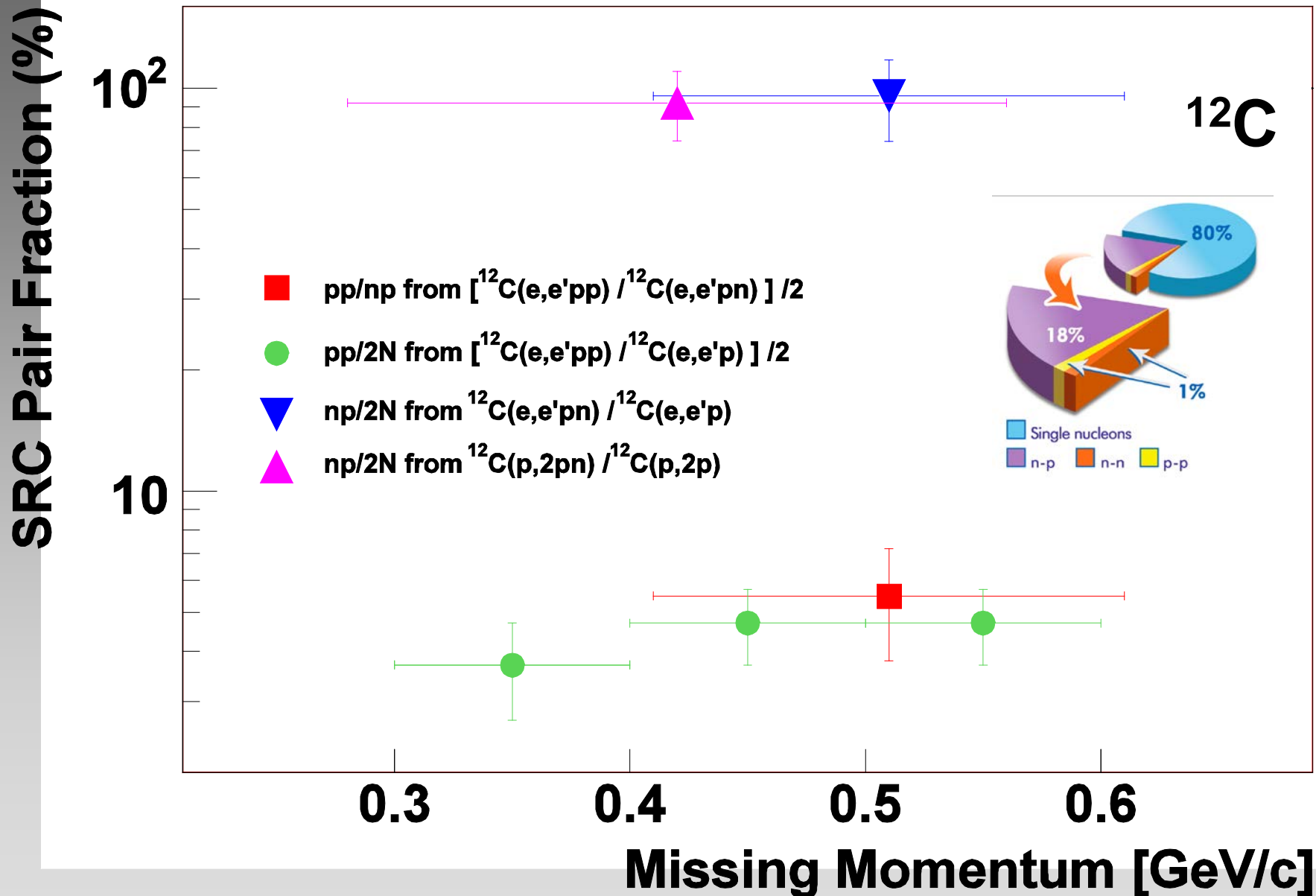
$$A(e, e'pp) \text{ and } A(e, e'pn)$$

# Quasi-Free scattering off a nucleon in a short range correlated pair

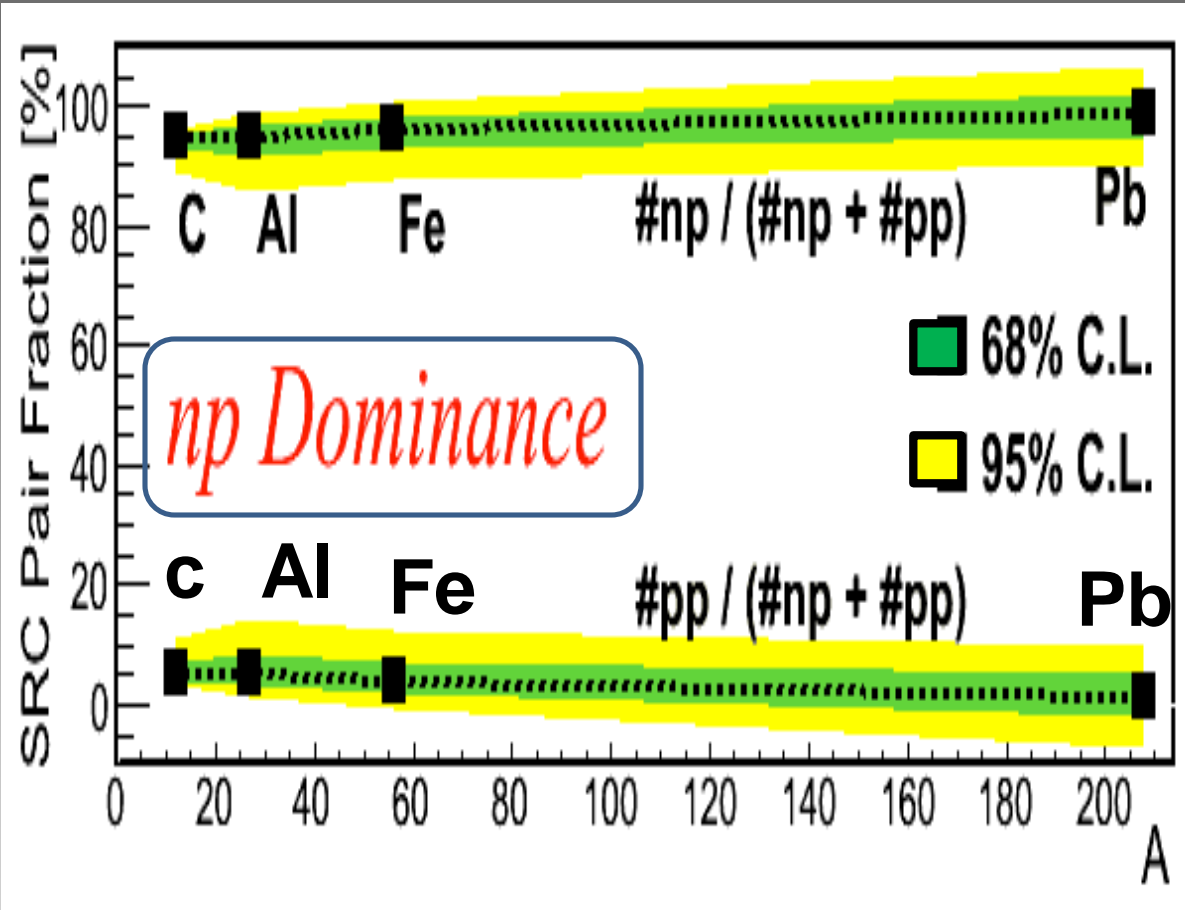


Hard exclusive  
triple – coincidence measurements

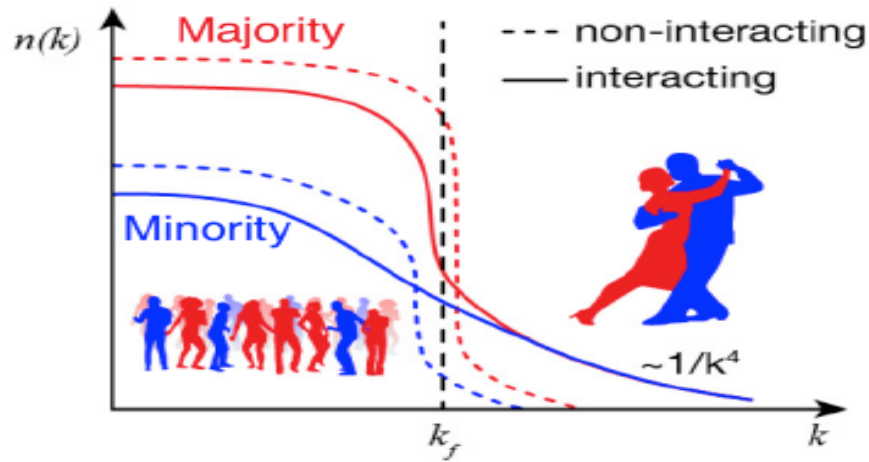
experiment	nuclei	pairs	$P_{miss}$ [MeV/c]
EVA/BNL	$^{12}\text{C}$	pp only	300-600
E01-015/ Jlab	$^{12}\text{C}$	pp and np	300-600
E07-006/ JLab	$^4\text{He}$	pp and np	400-850
CLAS/JLab	C, Al, Fe, Pb	pp only	300-700



# np / pp SRC pairs ratio



O. Hen et al., Science 346, 614 (2014).



**Neutron-skin in coordinate and proton-skin in momentum in heavy nuclei:**  
*What we can learn from their correlation in an Extended<sup>+</sup> Thomas-Fermi Approximation*

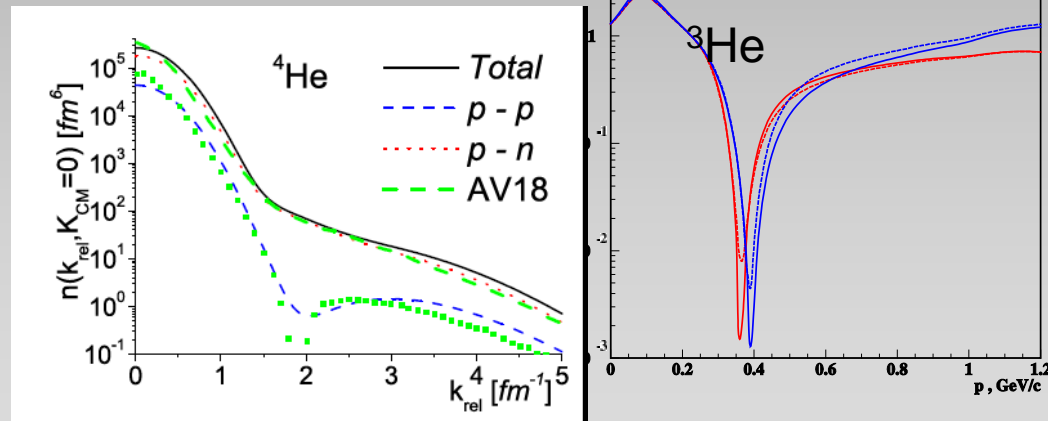
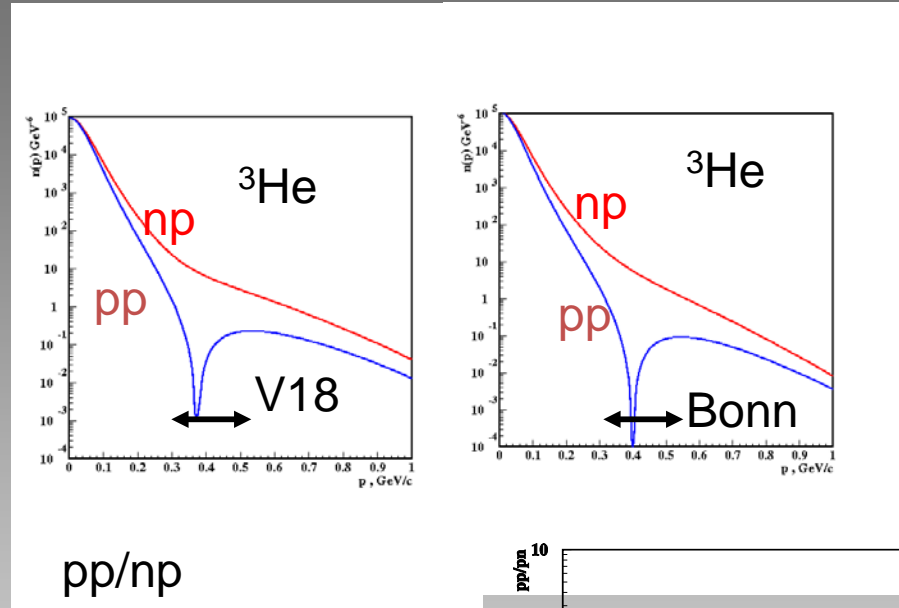
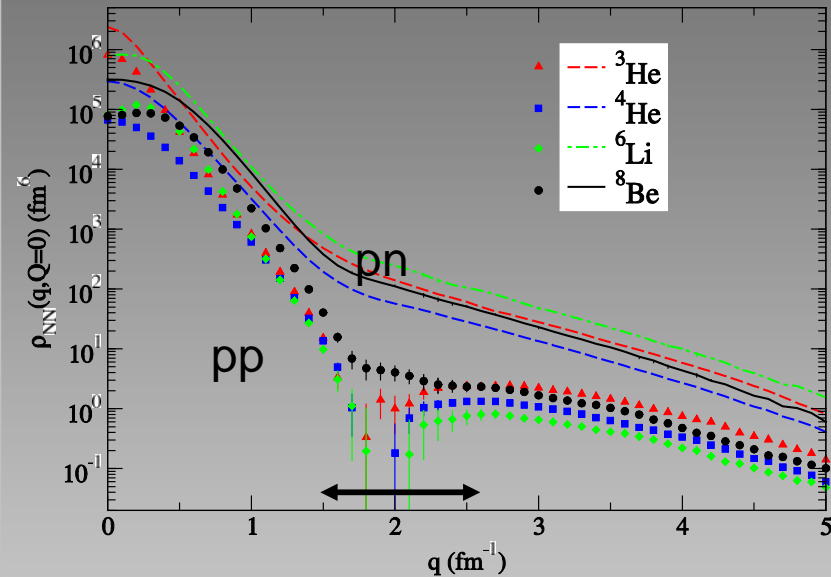
## Bao-An Li

a LOT more n than p in the skin.

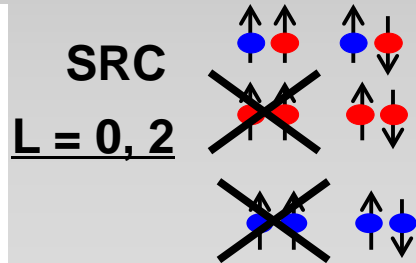
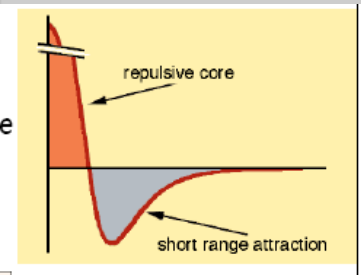
➔ protons in the skin move faster than neutrons.

➔ The fraction of high-momentum protons is larger in the skin than in the core.

At 300-600 MeV/c there is an excess strength in the np momentum distribution due to the strong correlations induced by the tensor NN potential.



Schiavilla, Wiringa, Pieper, Carson, PRL 98, 132501 (2007).



Ciofi and Alvioli  
PRL 100, 162503 (2008).

Sargsian, Abrahamyan, Strikman  
Frankfurt PR C71 044615 (2005)

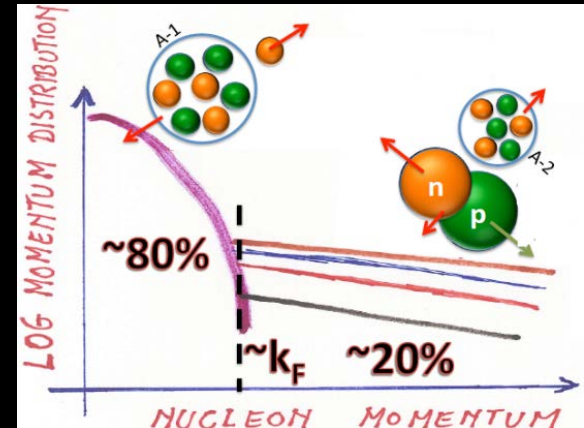


## Nuclei:

Identified triple coincidence SRC pairs  
in: ( $^3\text{He}$ , )  $^4\text{He}$ ,  $^{12}\text{C}$ ,  $^{27}\text{Al}$ ,  $^{56}\text{Fe}$ , and  $^{208}\text{Pb}$

High momentum tail in nuclei  
dominated by SRC pairs

np-SRC dominance



Short Range (tensor) Correlations  
are need to describe :

the short distance structure of nuclei

Momentum and energy distributions  
of nucleons in nuclei

Free Fermi Gas (FFG)  
is **WRONG !**



Symmetry energy ?

# Symmetry Energy

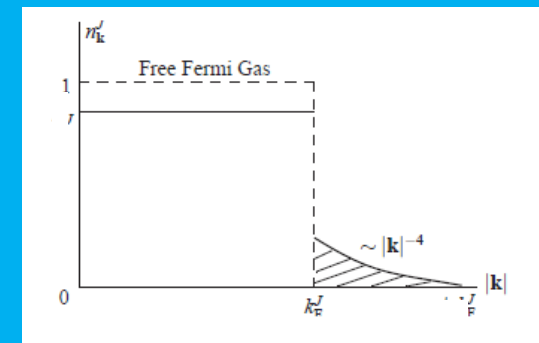
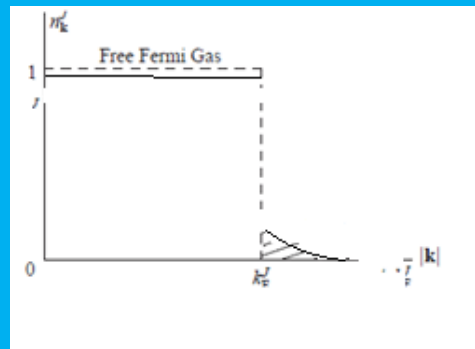
$$E(\rho_n, \rho_p) = E_0(\rho_n = \rho_p) + E_{sym}(\rho) \left( \frac{\rho_n - \rho_p}{\rho} \right)^2 + O(\delta^4)$$

symmetry energy

$$E_{sym}(\rho) \approx E(\rho)_{\text{PNM}} - E(\rho)_{\text{SNM}}$$

(Pure Neutron Matter)
(Symmetric Nuclear Matter)

$$E_{sym}(\rho) = E_{sym}^{kin}(\rho) + E_{sym}^{pot}(\rho)$$

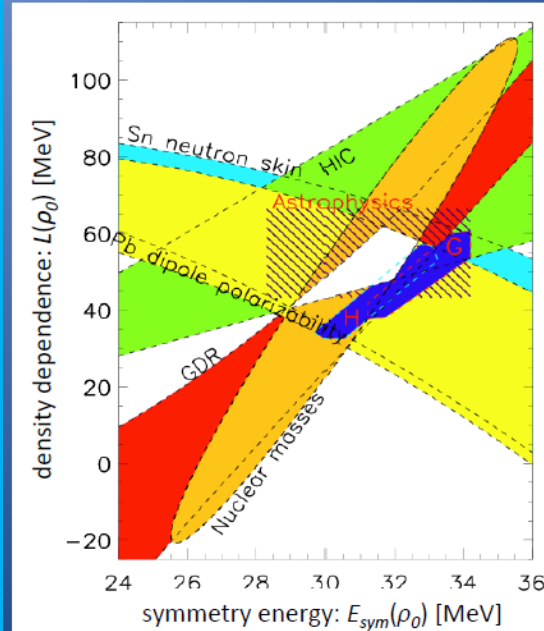


$$E_{sym}^{kin}(\text{with SRC}) < E_{sym}^{kin}(\text{no SRC})$$

# If the potential part is extracted by:

$$E_{sym}^{pot}(\rho_0) = E_{sym}(\rho_0) - E_{sym}^{kin}(\rho_0)$$

## Symmetry Energy @ Saturation Density ( $\rho_0$ )



Global analysis  
of world data:

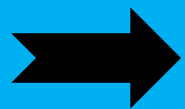
$$28.9 \leq E_{sym}(\rho_0) \leq 34.1$$

$$42.4 \leq L(\rho_0) \leq 74.4$$

J. Lattimer and Y. Lim, *Astrophys. J.* 771, 51 (2013)

\* $L(\rho_0) = 3\rho[dE/d\rho]|_{\rho_0}$

**SRC**  
**np-SRC dominance**



$$E_{sym}^{kin}(\text{with SRC}) < E_{sym}^{kin}(\text{no SRC})$$

$$E_{sym}^{pot}(\text{with SRC}) > E_{sym}^{pot}(\text{no SRC})$$

# Density dependence of Symmetry Energy

$$E_{sym}(\rho) = E_{sym}^{kin}(\rho_0) \cdot \left(\frac{\rho}{\rho_0}\right)^\alpha + E_{sym}^{pot}(\rho_0) \cdot \left(\frac{\rho}{\rho_0}\right)^\gamma$$

**FG:**  $E_{sym}^{kin}(\rho_0) = 12.5 \text{ MeV}$       $\alpha = 2/3$

**with Tensor Correlations (CFG):**

$$E_{sym}^{kin}(\rho) = E_{sym}^{kin}(\rho)|_{FG} - \Delta E_{sym}^{kin}(\rho)$$

where the SRC correction term is:

$$\Delta E_{sym}^{kin} \equiv \frac{E_F^0}{\pi^2} c_0 \left[ \lambda \left(\frac{\rho}{\rho_0}\right)^{1/3} - \frac{8}{5} \left(\frac{\rho}{\rho_0}\right)^{2/3} + \frac{3}{5} \frac{1}{\lambda} \left(\frac{\rho}{\rho_0}\right) \right]$$

**Lower  $\gamma$**



## Tensor correlations:

**Breaks the Fermi Gas picture**

**Reduce the kinetic symmetry Energy (at  $\rho_0$ )**

**Enhance the potential symmetry Energy (at  $\rho_0$ )**

**Soften the potential symmetry density dependence**

**Impact on Compact Astronomical Systems ?**

# How large is the effect ?

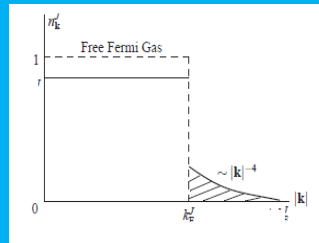
## Free Fermi Gas (FFG)

$$n(k) = \begin{cases} A & k < k_F \\ 0 & k > k_F \end{cases}$$

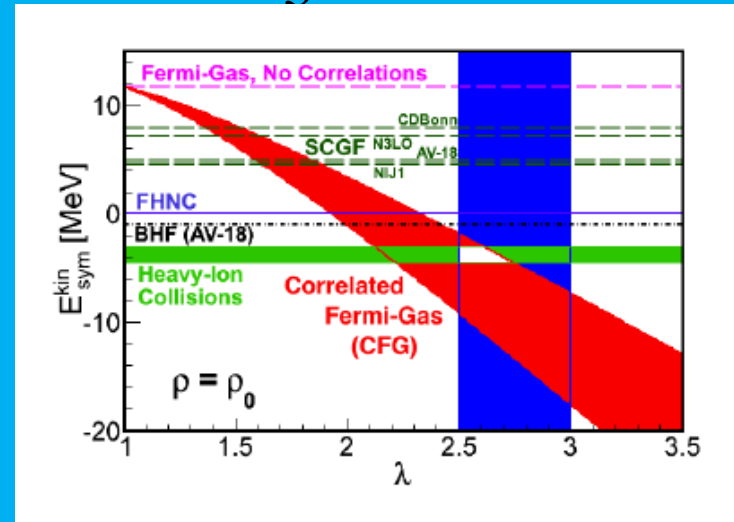


$$E_{sym}^{kin} = (2^{2/3} - 1) \cdot \frac{3}{5} \cdot E_F(\rho_0) \approx 12.5 \text{ MeV}$$

## With correlations (CFG)



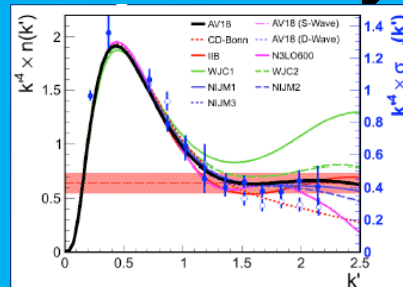
$$n(k) = \begin{cases} A_0 & k < k_F \\ C_0 / k^4 & k_F < k < \lambda k_F \\ 0 & k > \lambda k_F \end{cases}$$



	$E_{sym}^{kin}(\rho_0)$ [MeV]	$\gamma$ $\pm 1\sigma(2\sigma)$
CFG	$-10 \pm 3$	$0.25 \pm 0.05$
FG	$-10 \pm 3$	$0.58 \pm 0.05$
	0	$0.55 \pm 0.06$
	12.5	$0.48 \pm 0.10$
	17	$0.41 \pm 0.13$
Tsang <i>et al.</i> [6]	12.5	$0.7^{+0.1(0.35)}_{-0.2(0.3)}$

$$c_0 = 4.16 \pm 0.95,$$

$$\lambda \approx 2.75 \pm 0.25$$



# Can the drastically reduced $\gamma$ be consistent with n - starts data ?



## Analysis of Neutron Stars Observations Using a Correlated Fermi Gas Model

O. Hen,<sup>1</sup> A.W. Steiner,<sup>2,3,4</sup> E. Piasezky,<sup>1</sup> and L.B. Weinstein<sup>5</sup>

Global fit of NS EOS to NS mass/radius data taking into account:  
terrestrial constrains and physical limitations (causality and hydro dynamical stability)

**EOS:** 3 energy – density regions

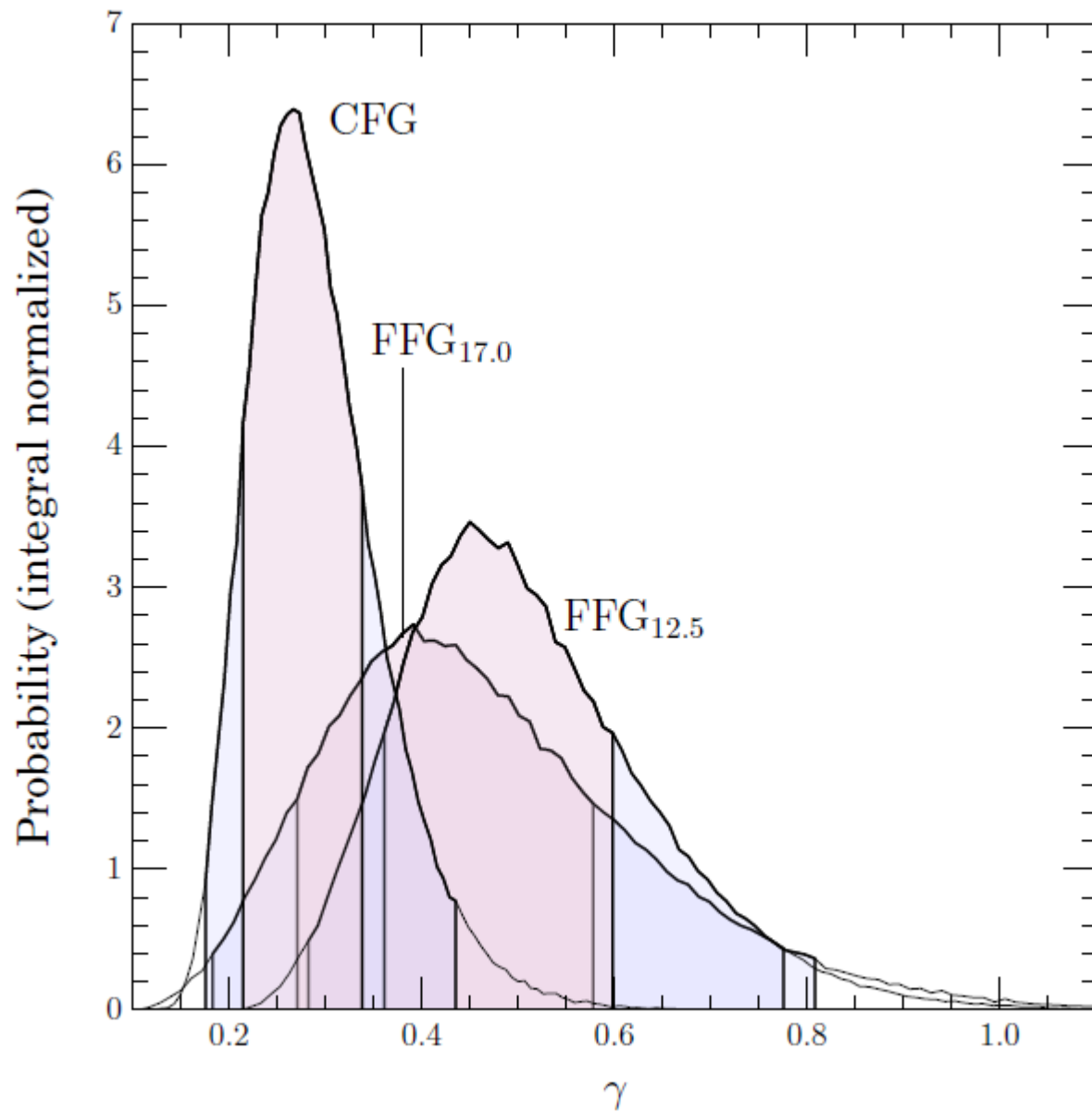
low ( $<15 \text{ MeV}/\text{fm}^3$ ), medium ( $15\text{-}350 \text{ MeV}/\text{fm}^3$ ), high ( $>350 \text{ MeV}/\text{fm}^3$ )

A. W. Steiner, J. M. Lattimer, and E. F. Brown, *Astro-phys. J.* **722**, 33 (2010), 1005.0811.

**Data :** here include high precision mass extractions from Pulsar-timing measurements, simultaneous mass-radius extractions from photospheric radius expansion (PRE) X-ray burst measurements, and thermal spectra measurement of low-mass X-ray Binaries (LMXB)

**Bayesian analysis  
using FFG and CFG ,models**

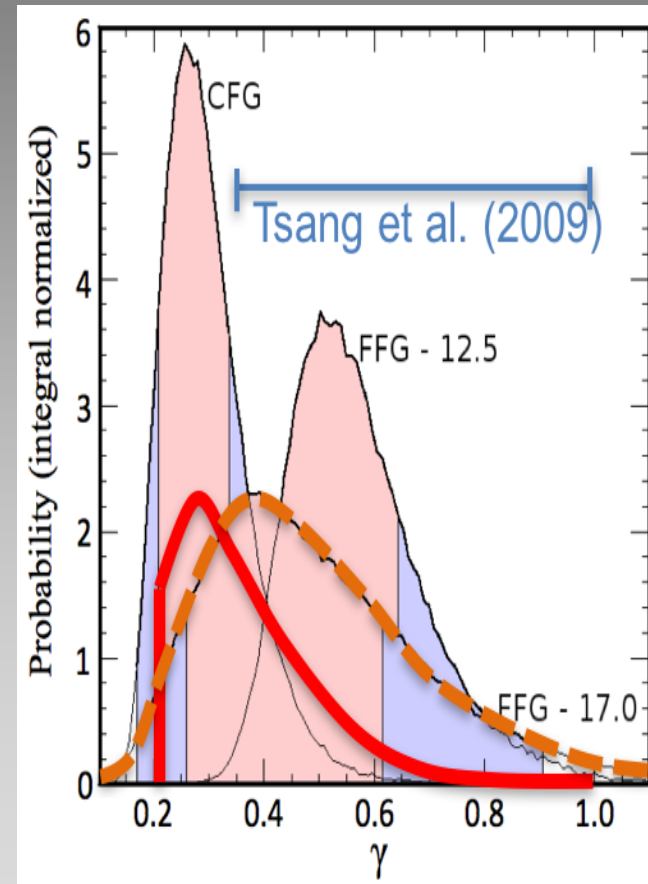
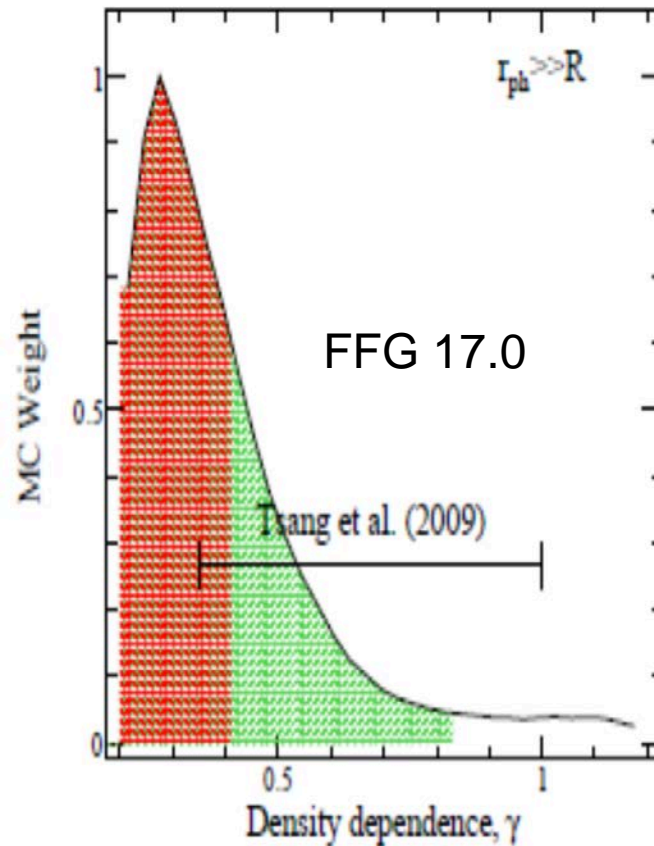


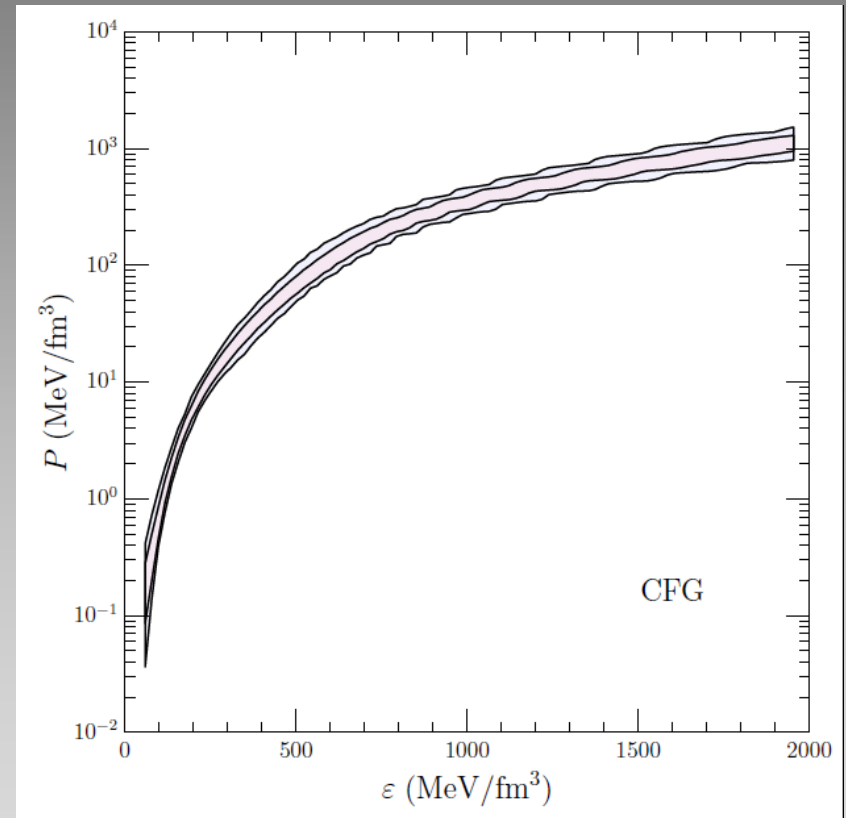
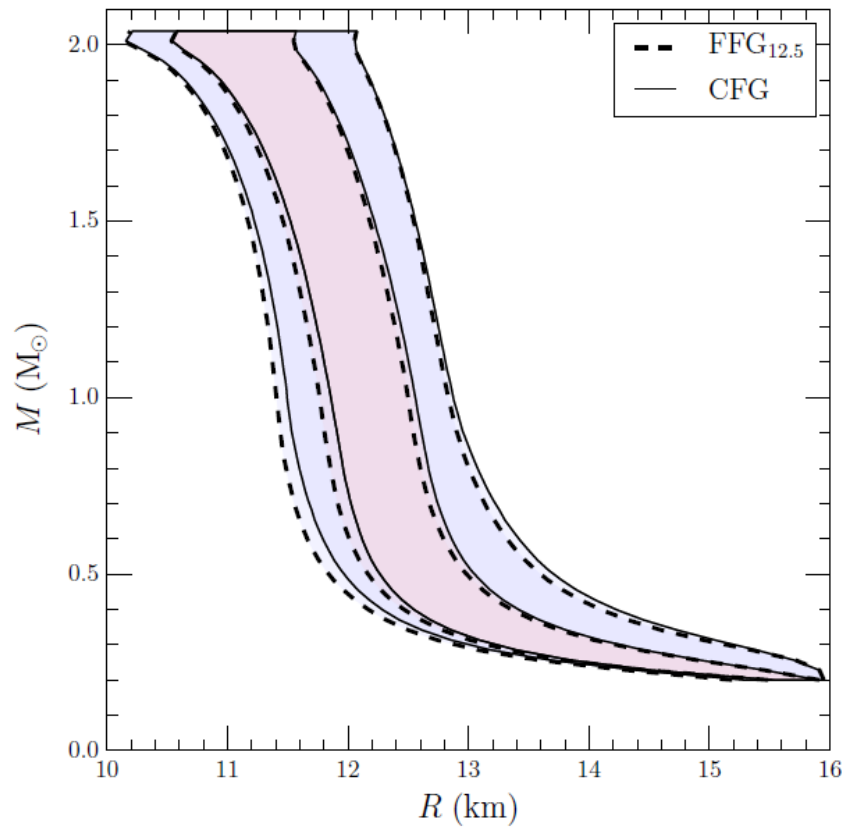


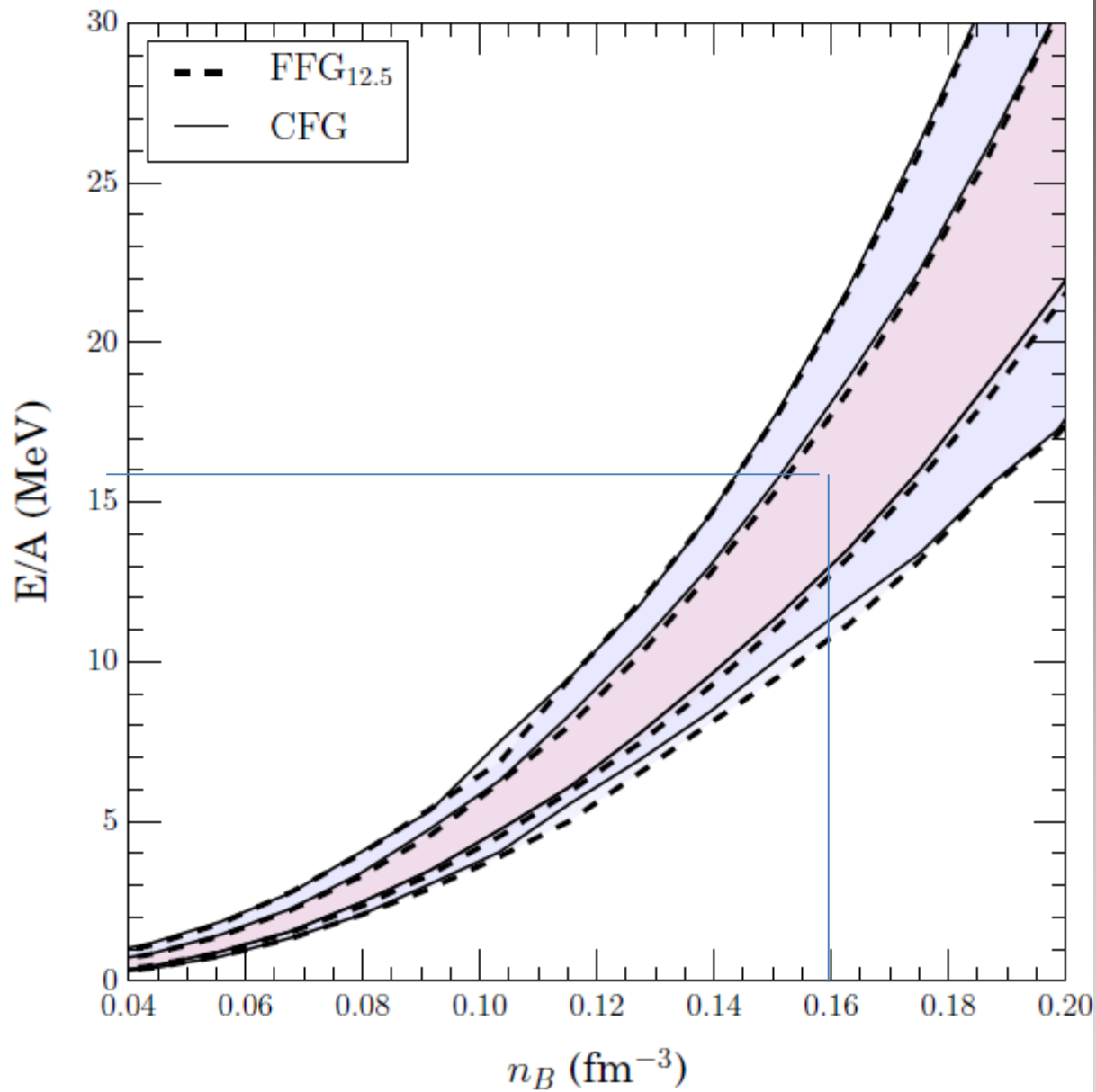
Analysis of Neutron Stars Observations Using a Correlated Fermi Gas Model

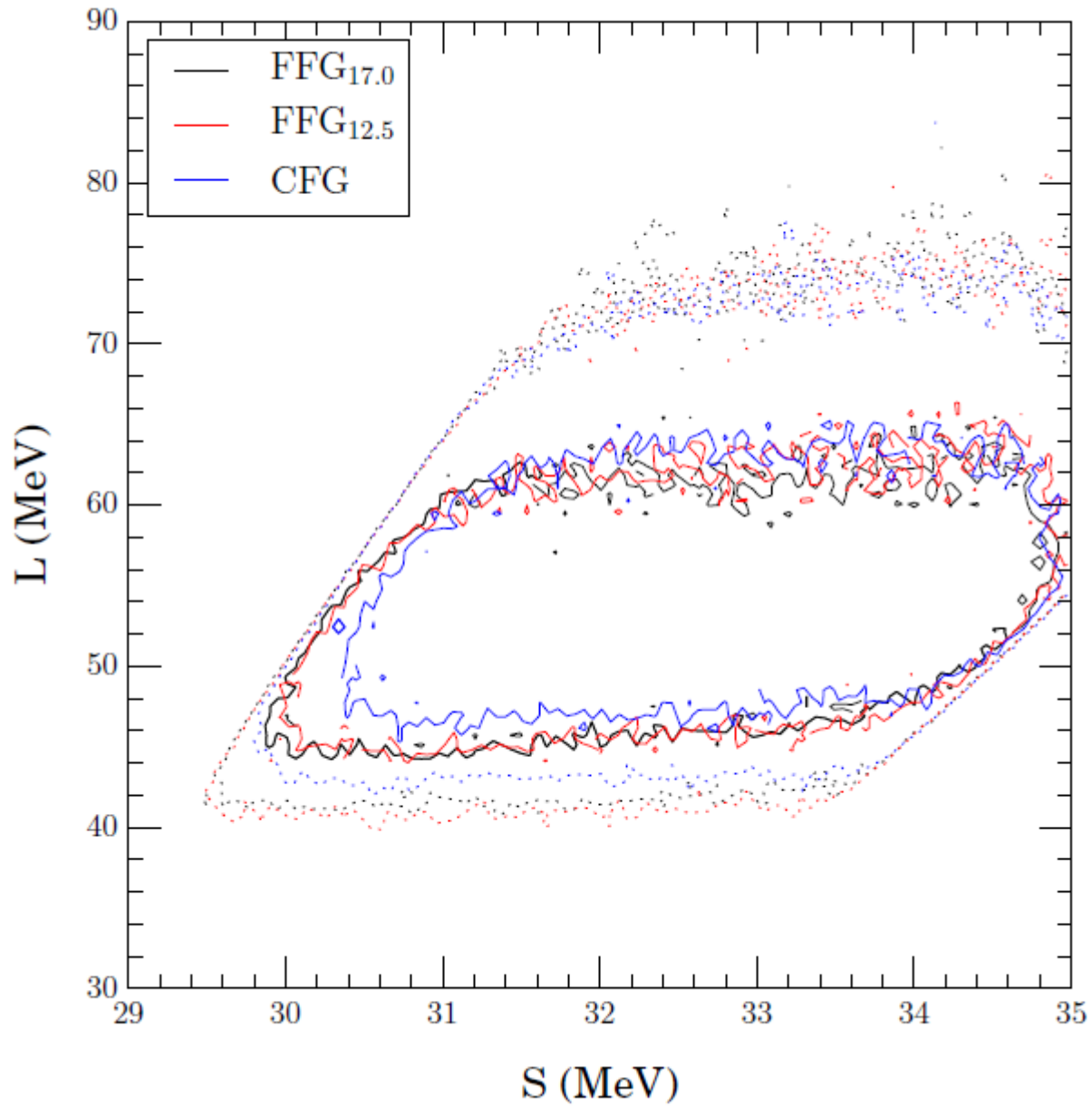
SLB astro phys J 722, 33 (2010)

JACWILCOB, et al. (2010)









# EOS global fits to Neutron Star Observations

## Incorporating CFG model into global fits to neutron stars observables

- Data can be fit using both FFG and CFG models
- Most observables are insensitive to the use of FFG / CFG
- Resulting  $\gamma$  is very different:
  - CFG: 0.21 – 0.34
  - FFG (12.5): 0.42 – 0.64



# Let me speculate:

**If calculations of heavy-ions collisions will be done with realistic momentum distribution (i.e. not ignoring SRC) the resulted density dependent of the potential symmetry ( $\gamma$ ) energy will also be found to be soft.**



See talk by

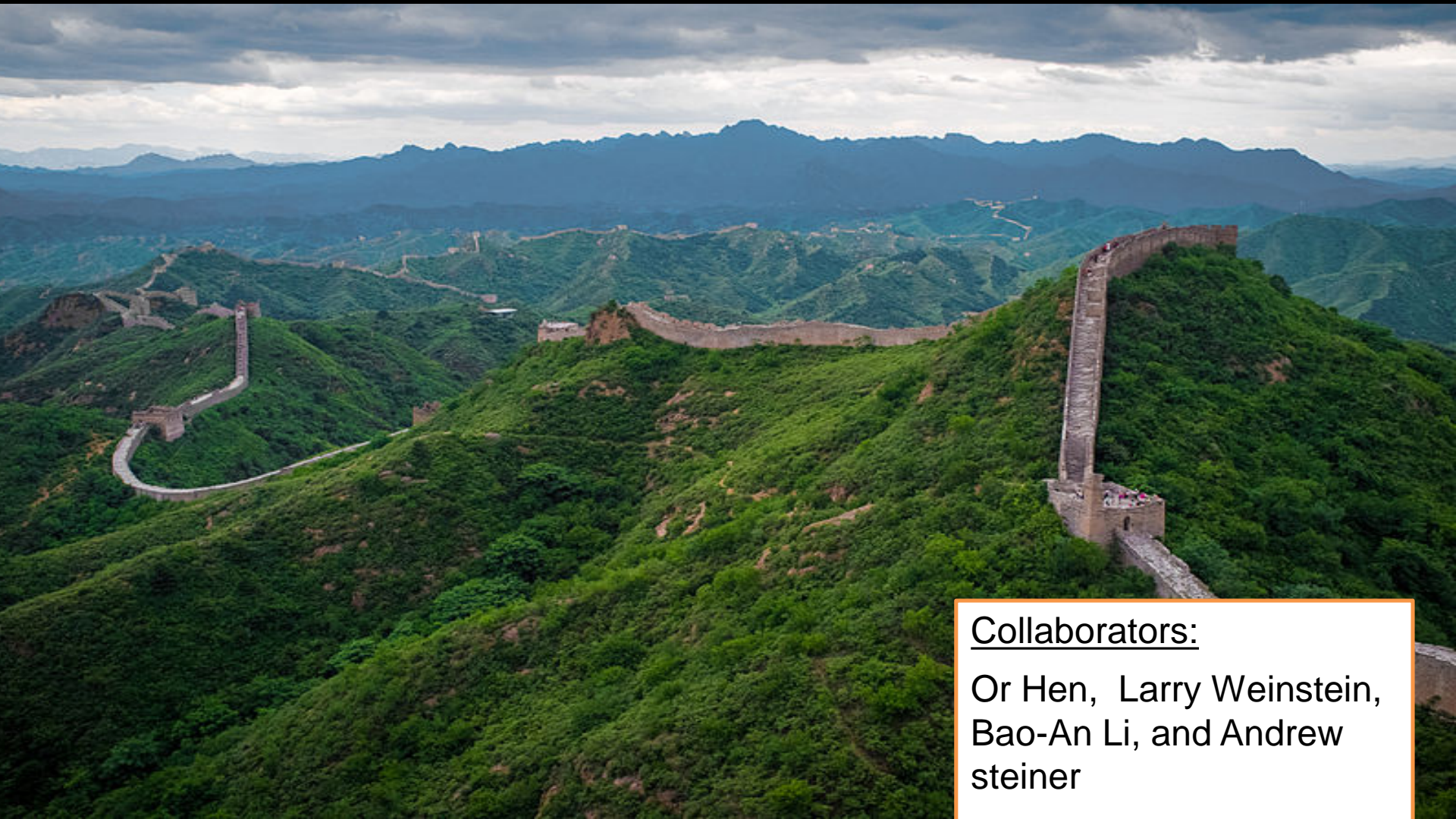
Or Hen

Next generation studies of short-range correlations using electron, proton and gamma



# Acknowledgment

I would like to thank the organizers for the invitation.

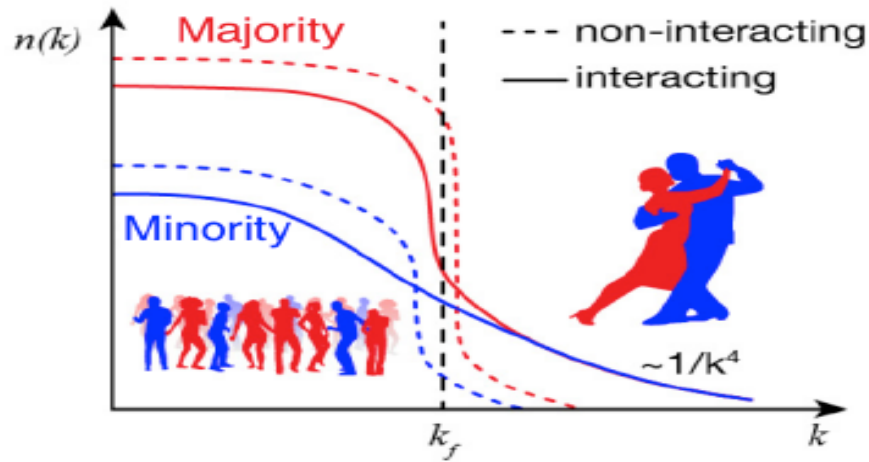


## Collaborators:

Or Hen, Larry Weinstein,  
Bao-An Li, and Andrew  
steiner





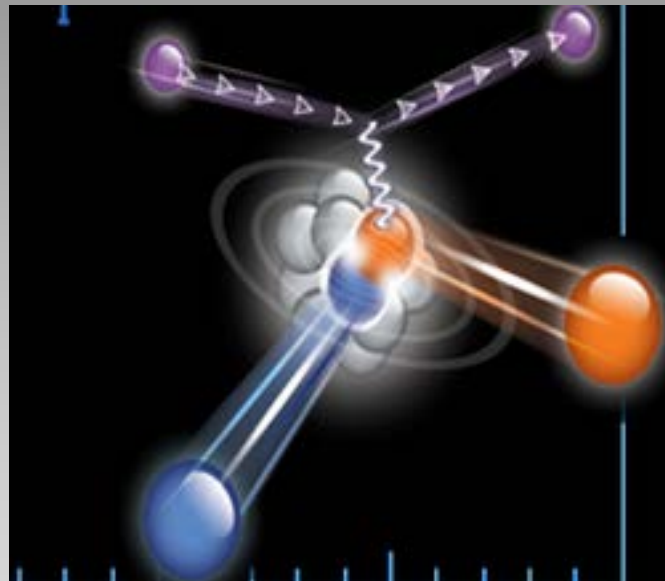
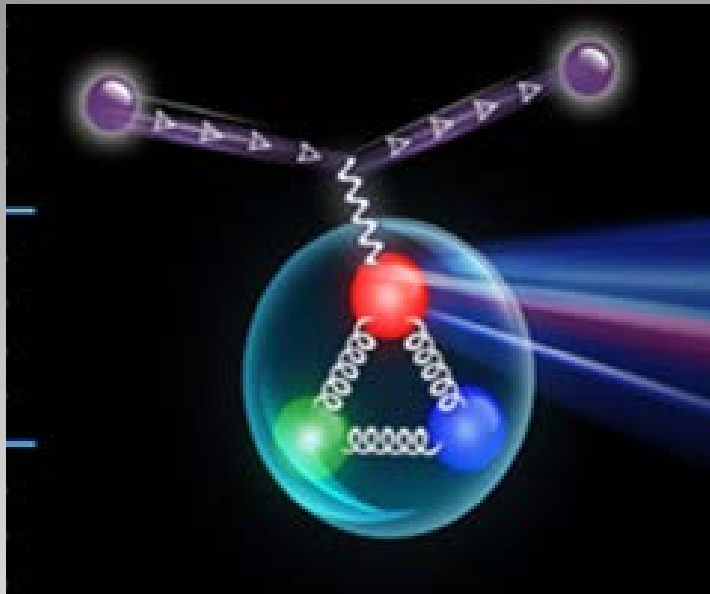


**Neutron-skin in coordinate and proton-skin in momentum in heavy nuclei:**  
*What we can learn from their correlation in an Extended<sup>+</sup> Thomas-Fermi Approximation*

**Bao-An Li**

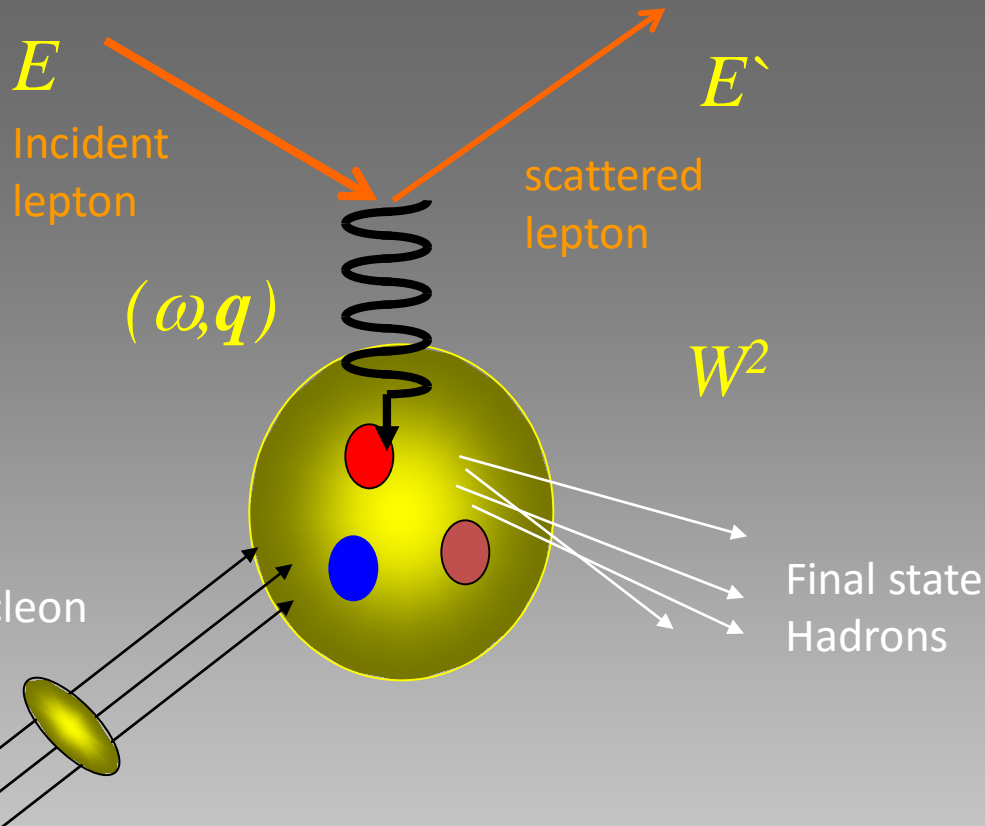
**The fraction of high-momentum protons is larger in the skin than in the core.**

# The EMC effect and Short Range Correlation in nuclei





# Deep Inelastic Scattering (DIS)



$$Q^2 = -q_\mu q^\mu = q^2 - \omega^2$$

$$\omega = E' - E$$

$$x_B = \frac{Q^2}{2m\omega} \quad \left( = \frac{Q^2}{2(q \cdot p_T)} \right)$$

$$0 \leq x_B \leq 1$$

$x_B$  gives the fraction of nucleon momentum carried by the struck parton

Electrons, muons, neutrinos

SLAC, CERN, HERA, FNAL, JLAB

$E, E'$  5-500 GeV

$Q^2$  5-50 GeV<sup>2</sup>

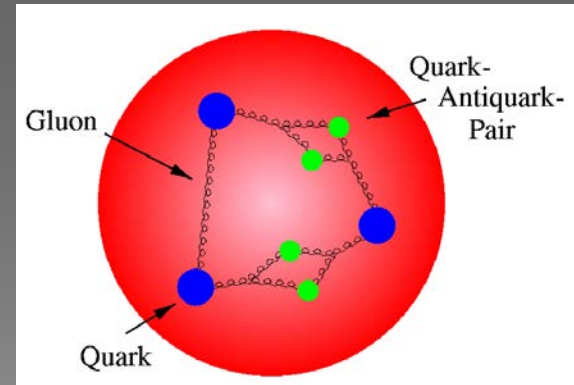
$w^2 > 4$  GeV<sup>2</sup>

$0 \leq x_B \leq 1$

Information about nucleon vertex is contained in  $F_1(x, Q^2)$  and  $F_2(x, Q^2)$ , the unpolarized structure functions

DIS scale: several tens of GeV

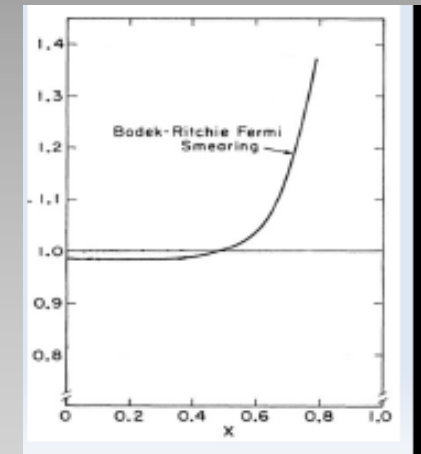
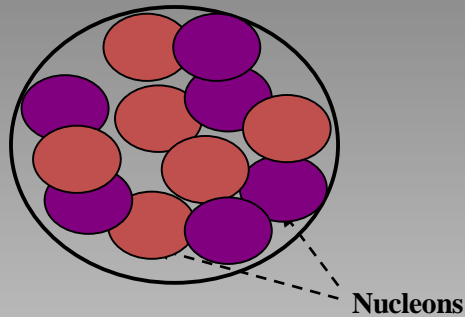
Nucleon in nuclei are bound by  $\sim$ MeV



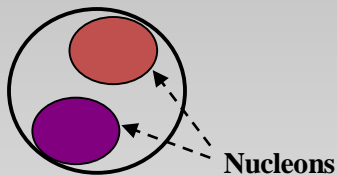
(My) Naive expectations :

DIS off a bound nucleon = DIS off a free nucleon

(Except for small Fermi momentum corrections)



Deuteron: binding energy  $\sim$ 2 MeV  
Average nucleons separation  $\sim$ 2 fm



DIS off a deuteron = DIS off a free proton neutron pair



# The European Muon Collaboration (EMC) effect

Questions :

DIS off a bound nucleon  $\neq$  DIS off a free nucleon?

A bound nucleon  $\neq$  A free nucleon?

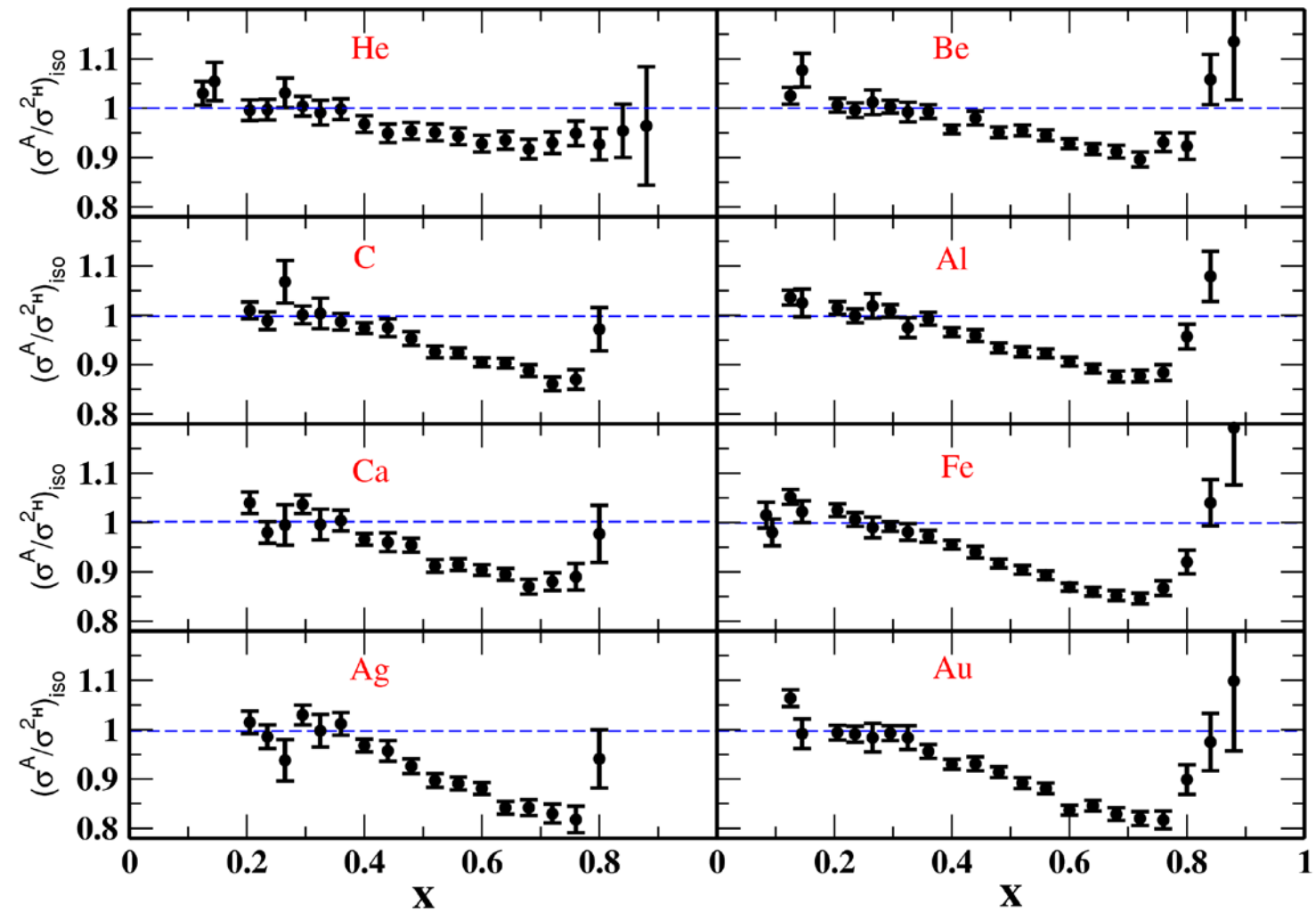
$$\sigma_d^{DIS} \stackrel{?}{=} \sigma_p^{DIS} + \sigma_n^{DIS}$$

Is there an 'EMC effect' in Deuterium ?



$\sigma^{DIS}$  per nucleon in nuclei  $\neq$   $\sigma^{DIS}$  per nucleon in deuteron





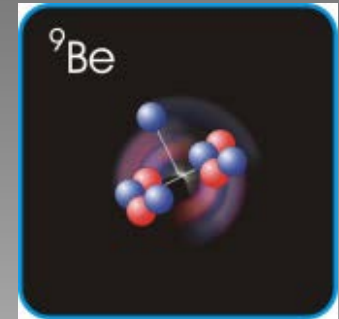
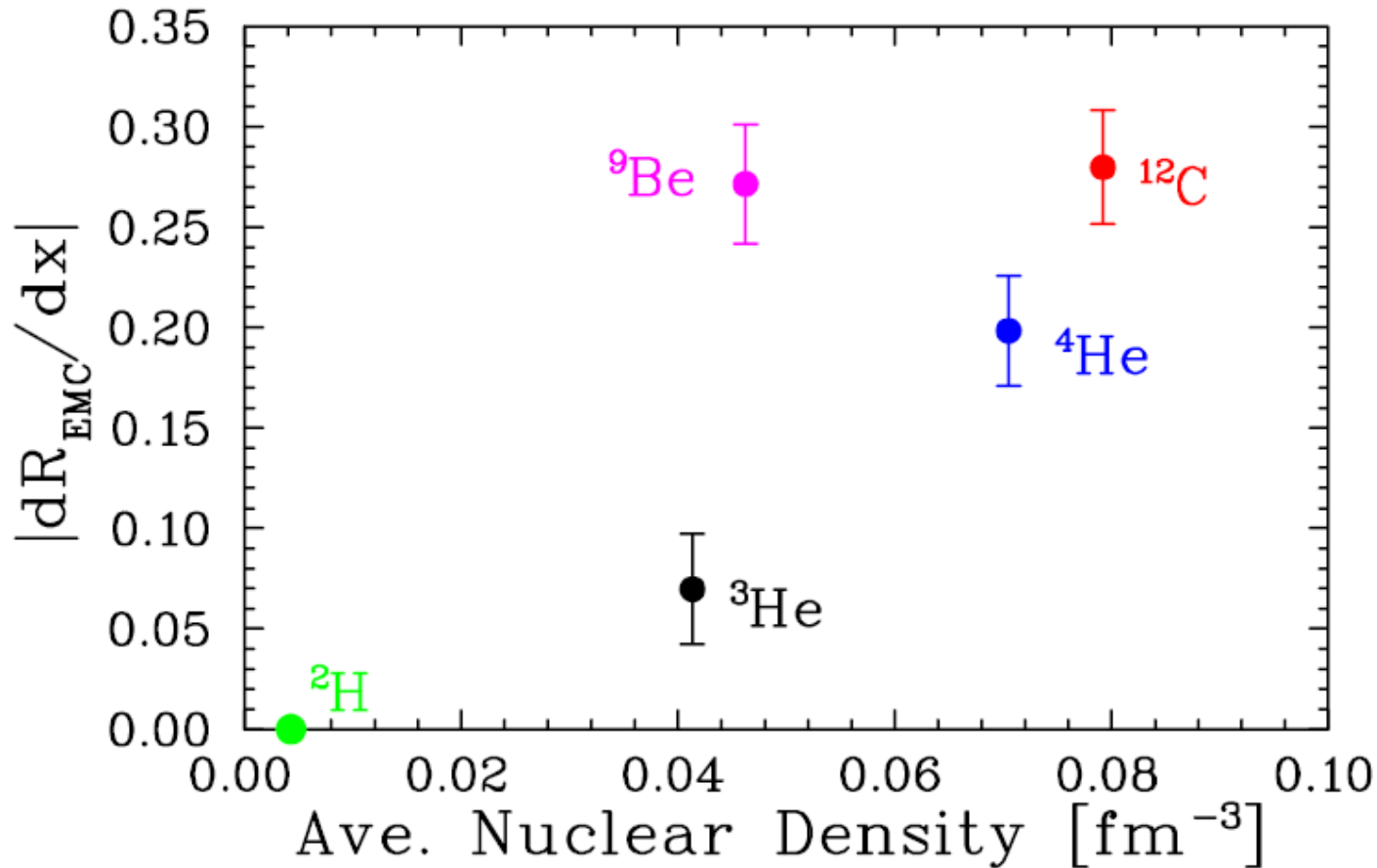
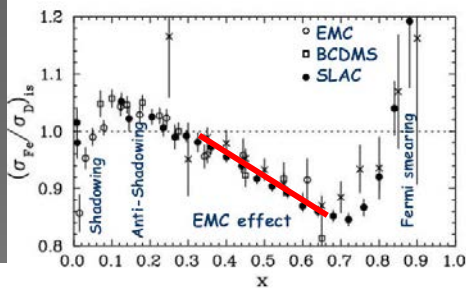
Data from CERN SLAC JLab  
1983- 2009

EMC collaboration, Aubert et al. PL B 123,275 (1983)

SLAC Gomez et al., Phys Rev. D49,4348 (1994)

A review of data collected during first decade, Arneodo, Phys. Rep. 240,301(1994)

# EMC is a not a bulk property of nuclear medium



JLab / Hall C

Seely et al. PRL 103, 202301 (2009)

Scaled nuclear density =  $(A-1)/A \langle \rho \rangle$   
 $\rightarrow$  remove contribution from struck nucleon

$\langle \rho \rangle$  from ab initio few-body calculations  
 $\rightarrow$  [S.C. Pieper and R.B. Wiringa, *Ann. Rev. Nucl. Part. Sci.* 51, 53 (2001)]

# The European Muon Collaboration (EMC) effect

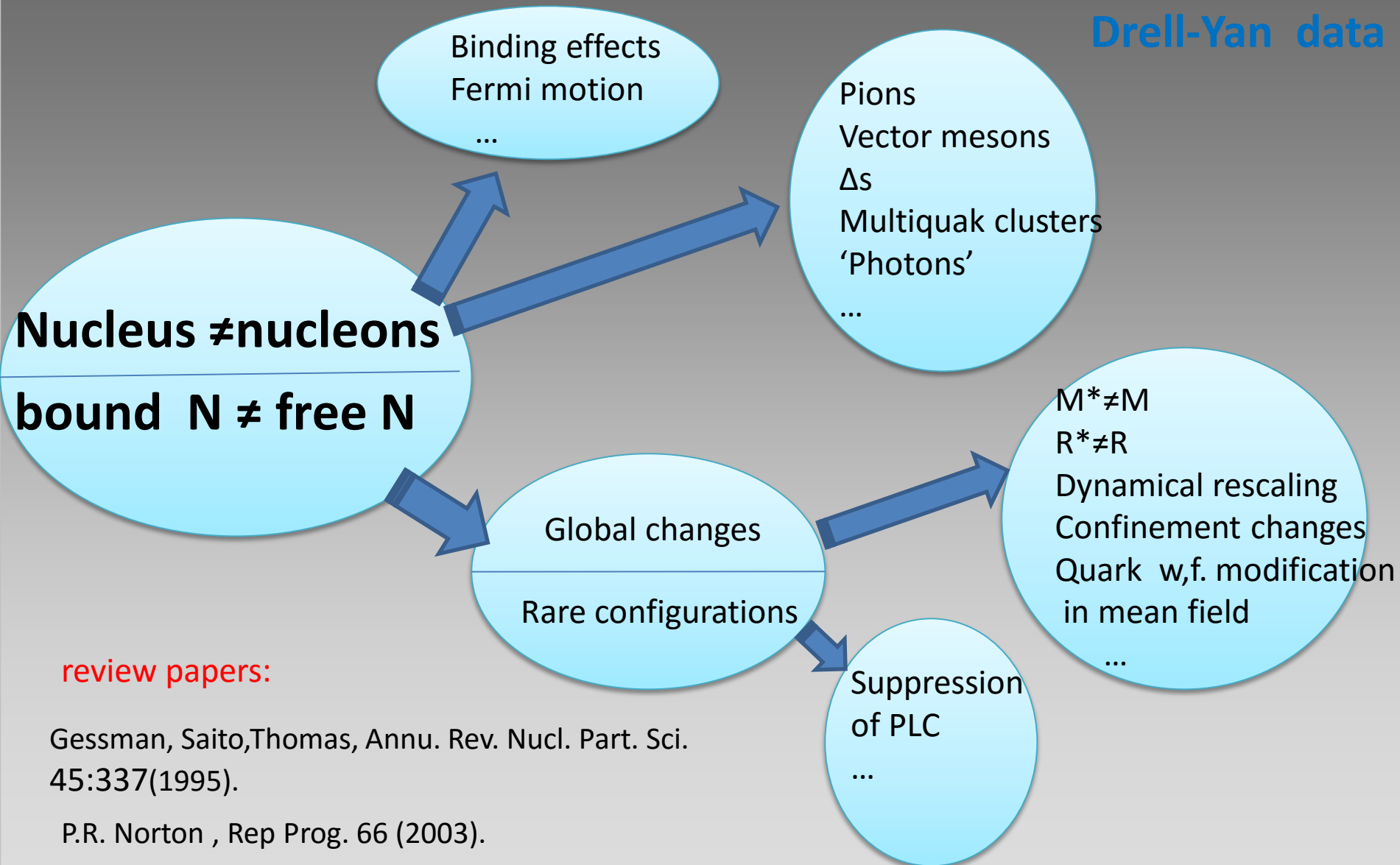


**Well established measured effect  
with no consensus as to its origin**



# Models of the EMC effect

## Drell-Yan data



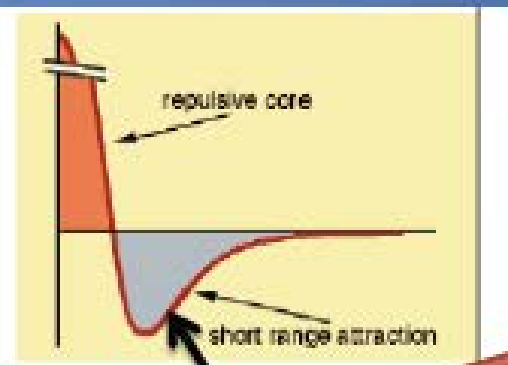
review papers:

Gessman, Saito, Thomas, Annu. Rev. Nucl. Part. Sci. 45:337(1995).

P.R. Norton , Rep Prog. 66 (2003).

Frankfurt and Strikman (2012)

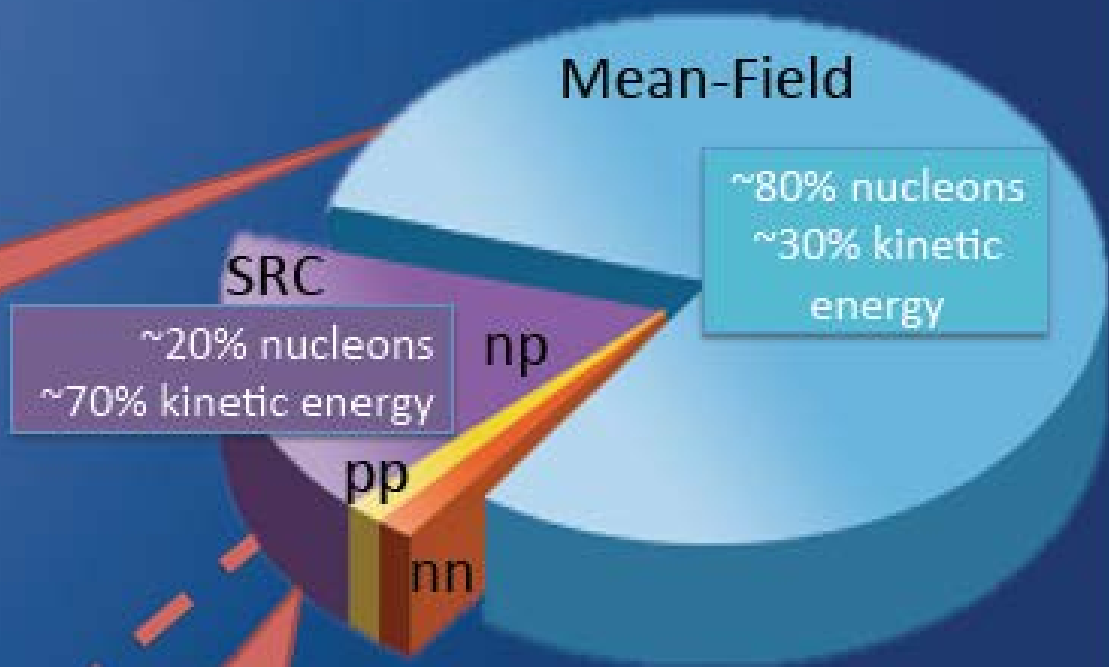
# Where is the EMC Effect?



Largest attractive force

Mean-Field

High local nuclear matter density, large momentum, large off shell, large virtuality



SRC

$$v = p^2 - m^2$$



## Inclusive electron scattering $A(e,e')$

### Deep Inelastic Scattering

→ Partonic (quark) Structure of Hadrons

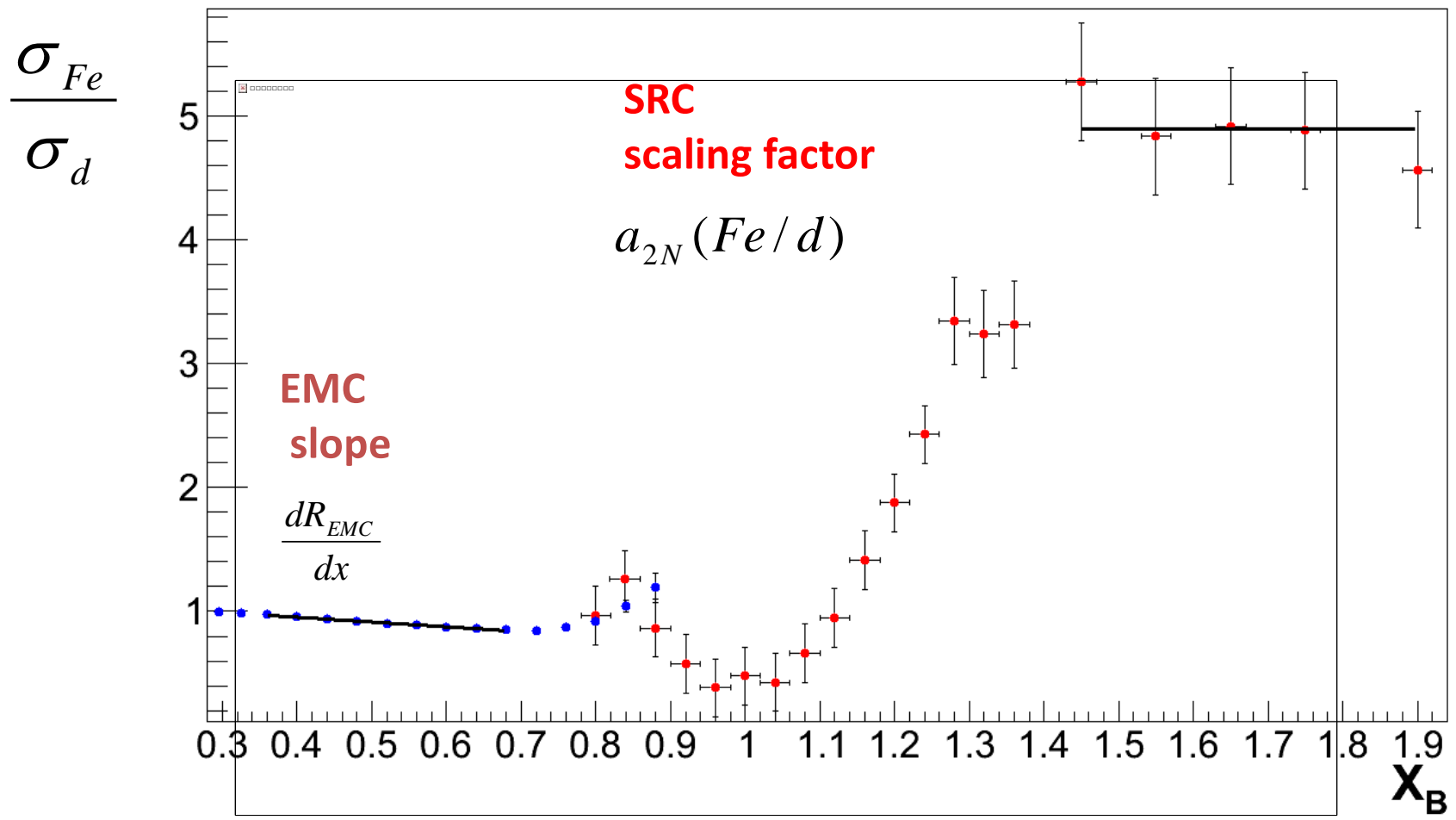
### Inclusive Scattering at $X_B > 1$

$A(e,e')$

→ Partonic (nucleon) Structure of Nucleus



# Comparing magnitude of EMC effect and SRC scaling factors



SLAC data:

Gomez et al., Phys. Rev. D49, 4348 (1983).

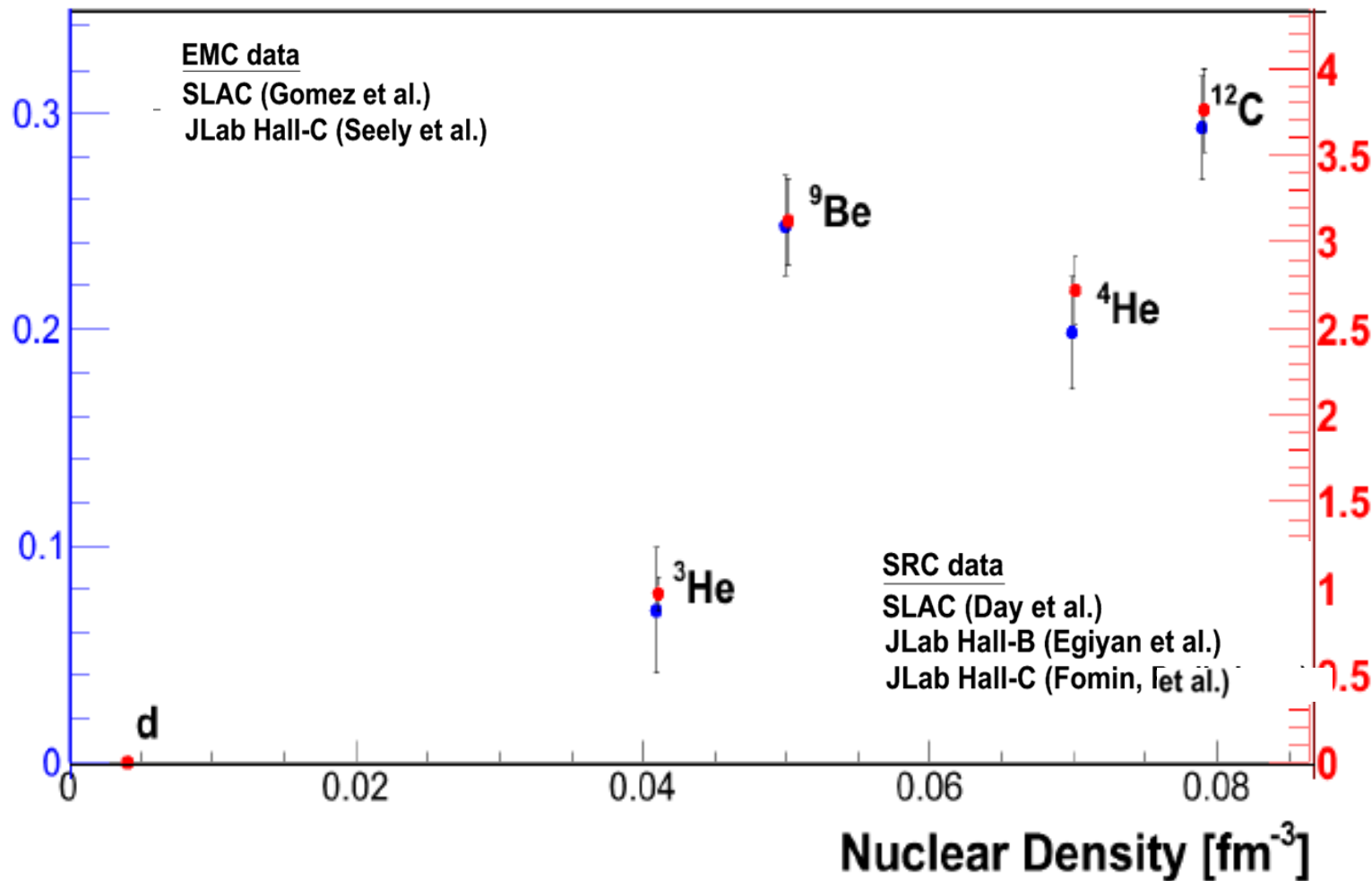
$Q^2=2, 5, 10, 15 \text{ GeV}/c^2$  (averaged)

Frankfurt, Strikman, Day, Sargsyan, Phys. Rev. C48 (1993) 2451.

$Q^2=2.3 \text{ GeV}/c^2$



Slopes  $0.35 \leq X_B \leq 0.7$   $dR_{EMC}/dX_B$



EMC data

SLAC (Gomez et al.)

JLab Hall-C (Seely et al.)

SRC data

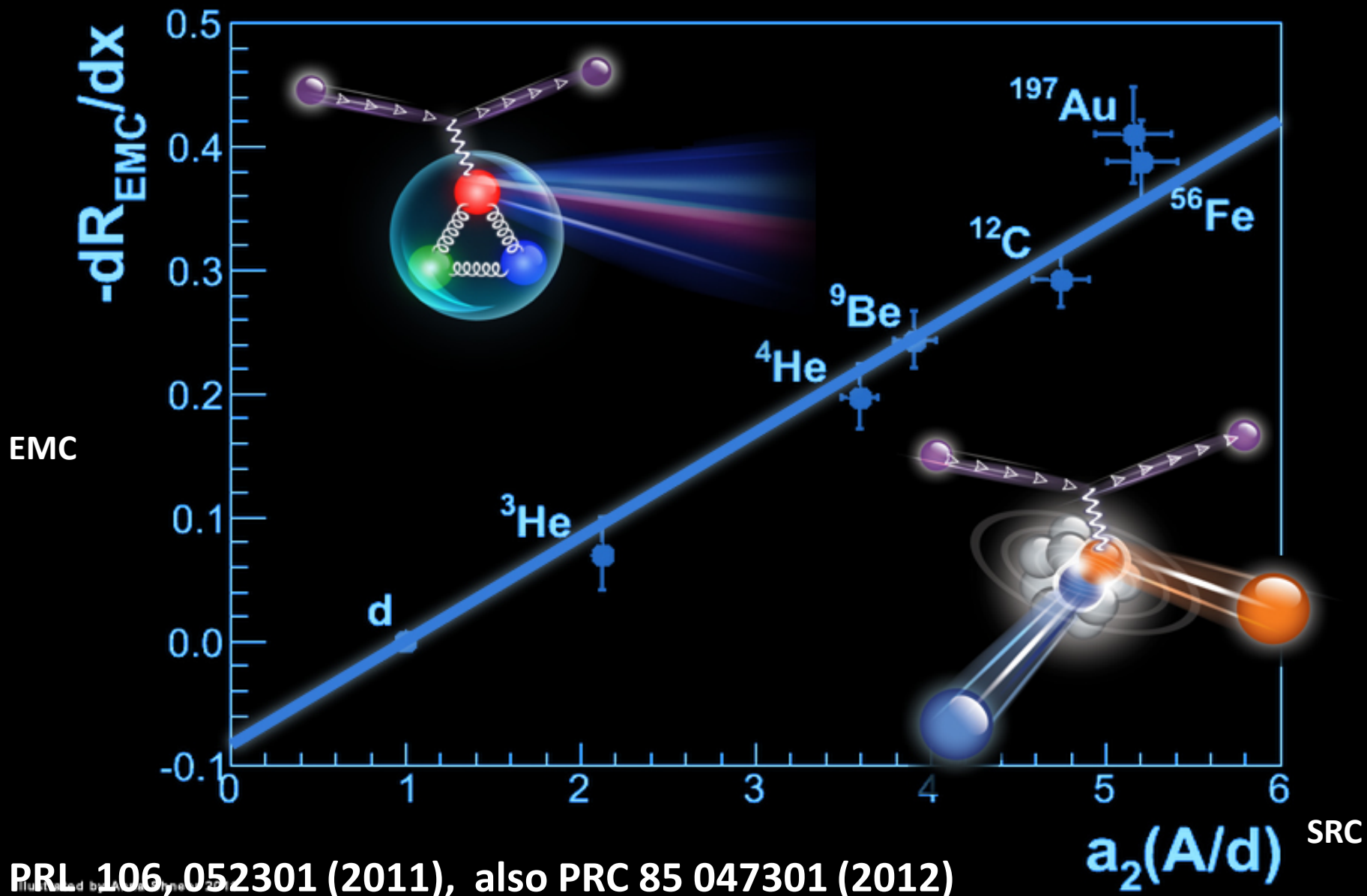
SLAC (Day et al.)

JLab Hall-B (Egiyan et al.)

JLab Hall-C (Fomin, et al.)

Scaling factors  $X_B \geq 1.4$   $a_2(A/d)-1$







# Deuteron is not a free np pair

$$\sigma_d \neq \sigma_p + \sigma_n$$

$$\frac{\sigma_d}{\sigma_p + \sigma_n} \approx \frac{\sigma_{^3\text{He}}}{\sigma_d}$$

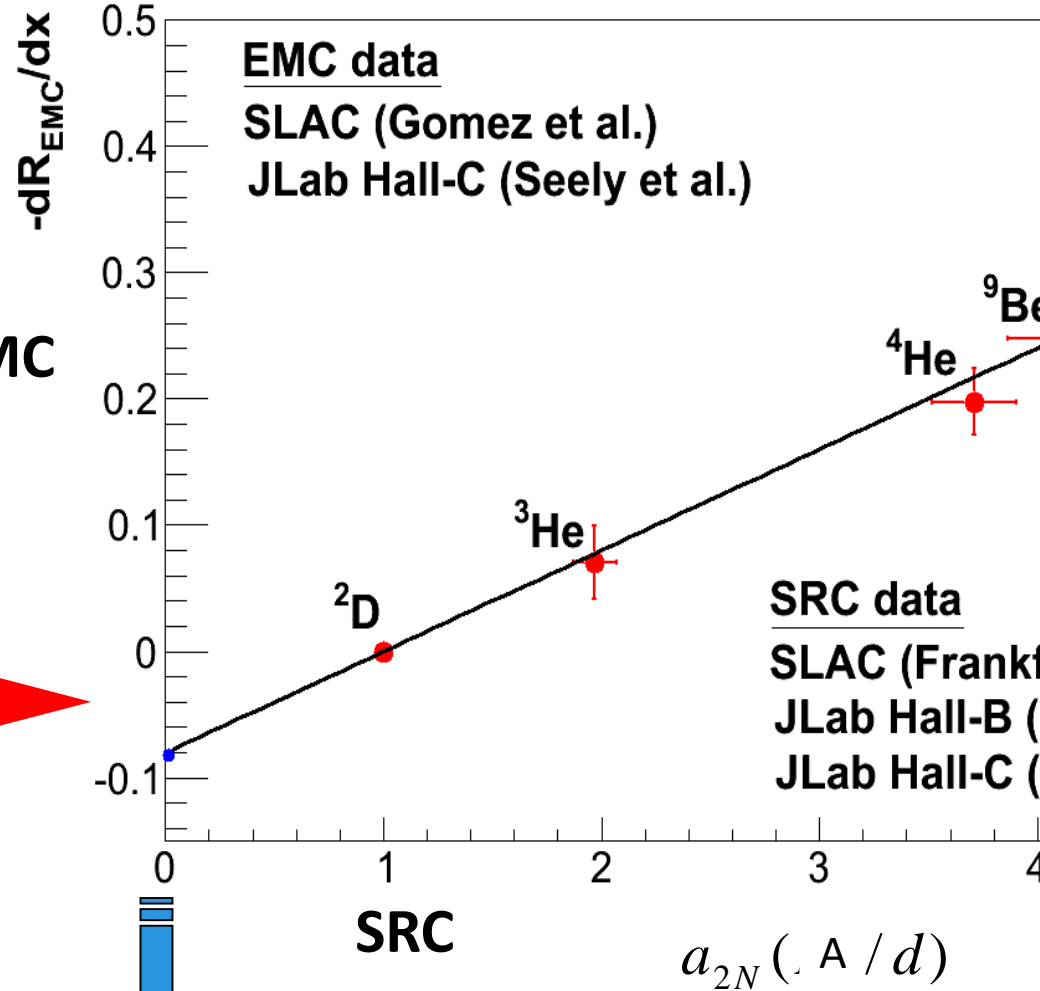
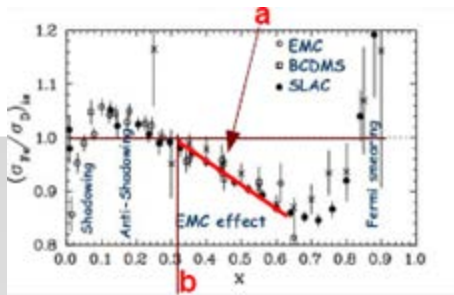
EMC

The slopes for  $0.35 \leq X_B \leq 0.7$

$0.09 \pm 0.01$



$$\frac{\sigma_d}{\sigma_p + \sigma_n}(x=0.6) \approx 0.98$$

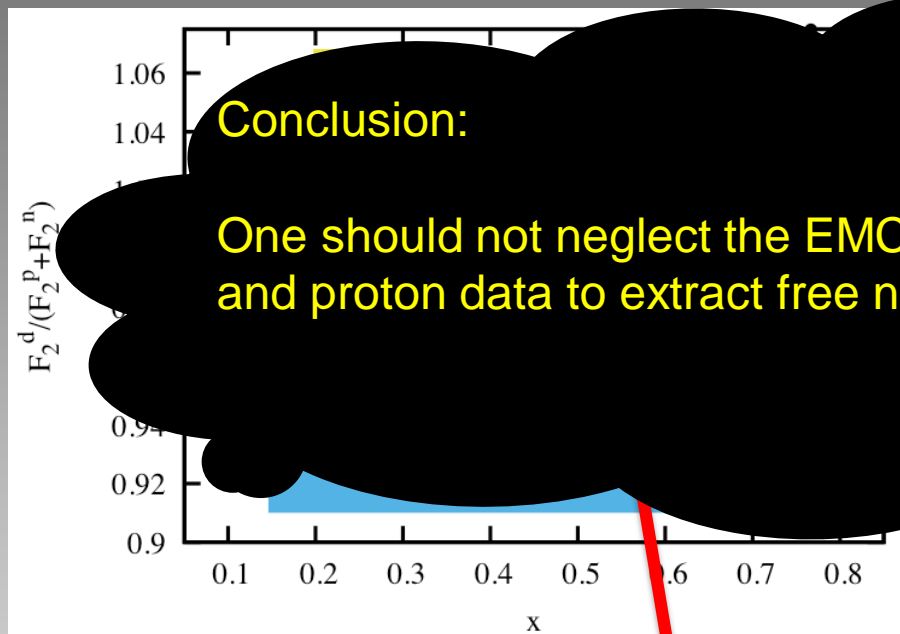


SRC=0 free nucleons

# EMC/SRC prediction Agrees with BONUS

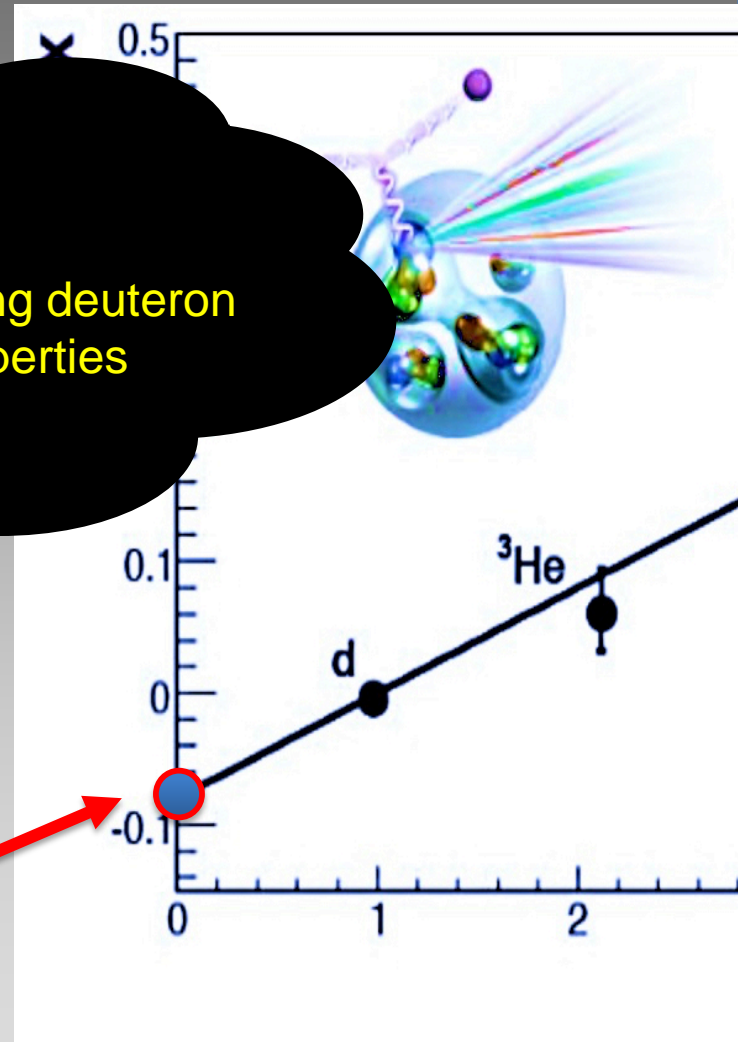
## EMC effect in the Deuteron

K. Griffioen *et al.* [BONUS collaboration] preliminary result.



**Conclusion:**

One should not neglect the EMC effect using deuteron and proton data to extract free neutron properties



Slope:

BONUS:  $-0.10(5)$

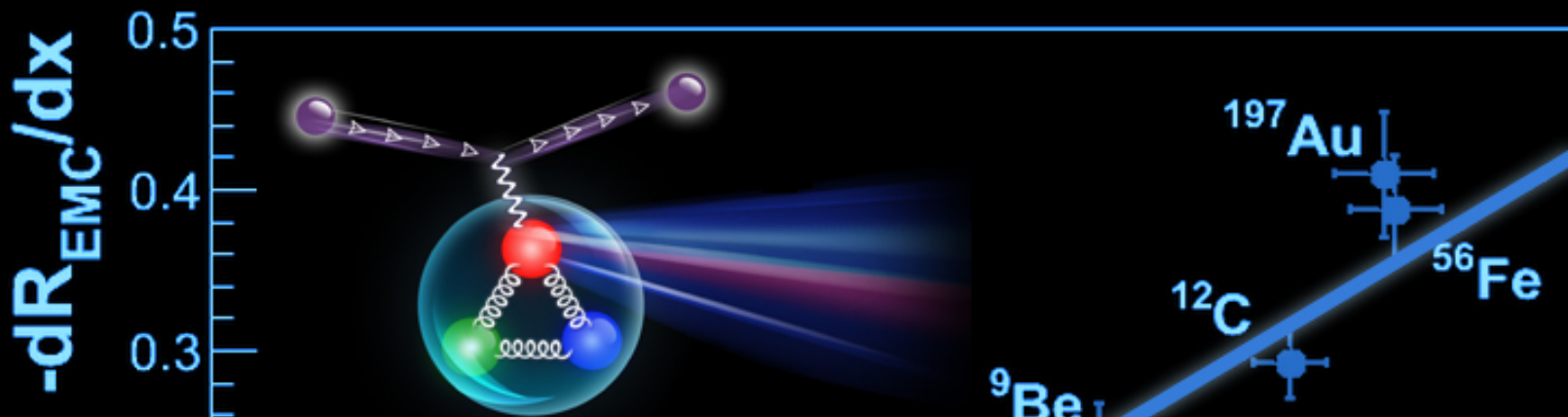
EMC/SRC:  $-0.09(1)$

CIPANP 2015: May 19-24, 2015 (Vail, CO)

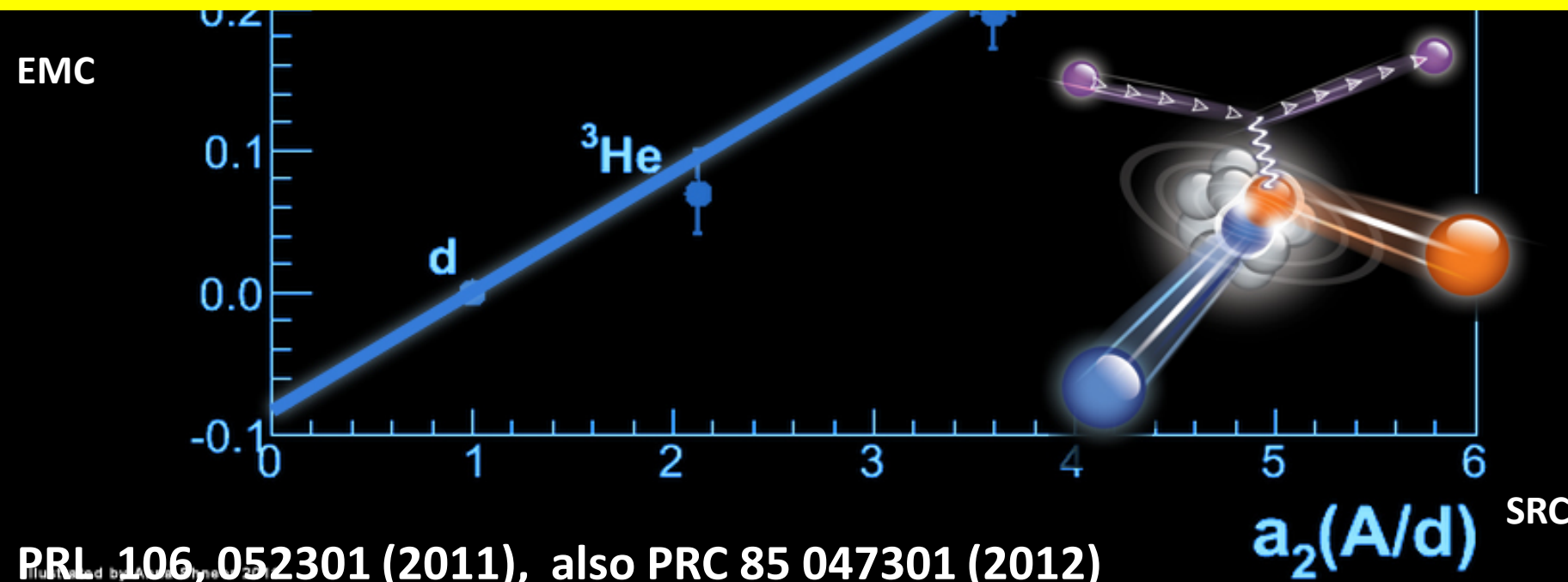
arXiv:1506.0087

Weinstein *et al.* PRL 106, 052301 (2011)

*O. Hen* *et al.*, Phys. Rev. C 85, 047301 (2012)



the EMC effect is associated with large virtuality ( $\nu = p^2 - m^2$ )

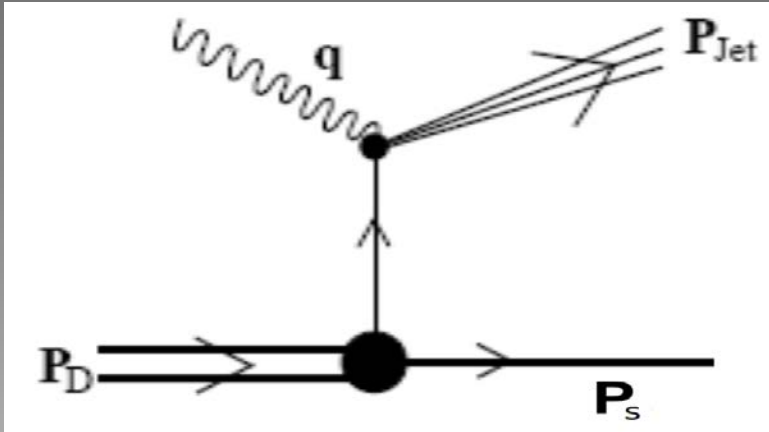
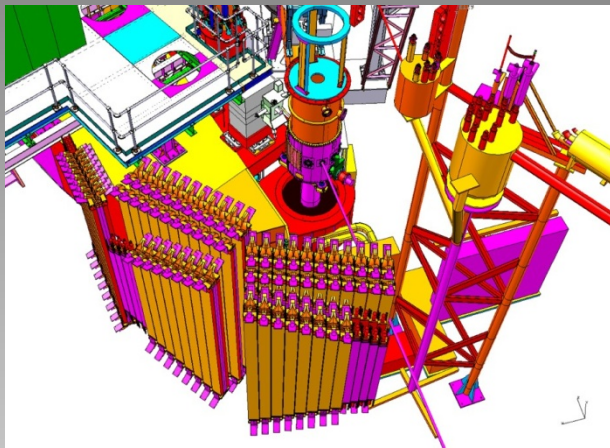


# Hypothesis can be checked by measuring DIS off Deuteron tagged with high momentum recoil nucleon

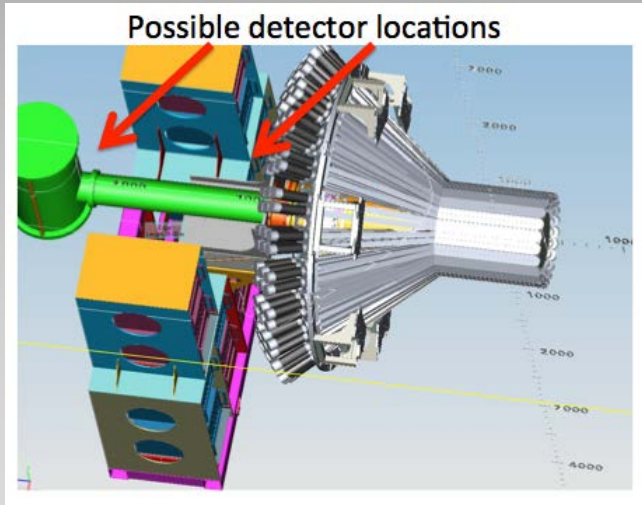
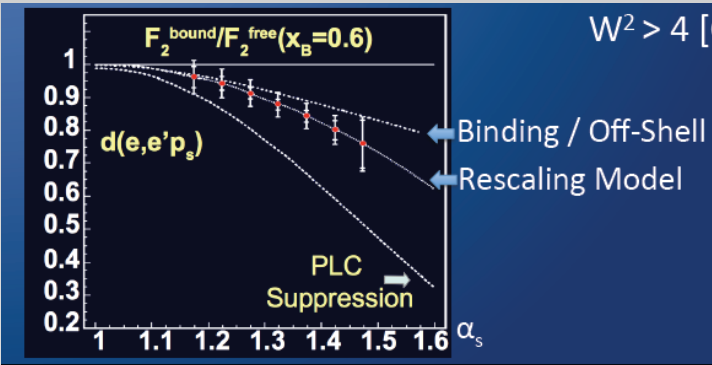
**spectator tagging**



**large effect**



**12 GeV JLab approved experiment E 12-11-107**



**12 GeV approved experiment CLAS E12-11-003a**

# Short distance structure of nuclei



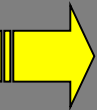
1

The probability for a nucleon to have momentum  $\geq 300$  MeV / c in medium nuclei is  $\sim 25\%$

2

More than  $\sim 90\%$  of all nucleons with momentum  $\geq 300$  MeV / c belong to 2N-SRC.

1



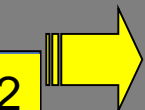
Most of kinetic energy of nucleon in nuclei is carried by nucleons in 2N-SRC.

2

3

Probability for a nucleon with momentum 300-600 MeV / c to belong to np-SRC is  $\sim 18$  times larger than to belong to pp-SRC.

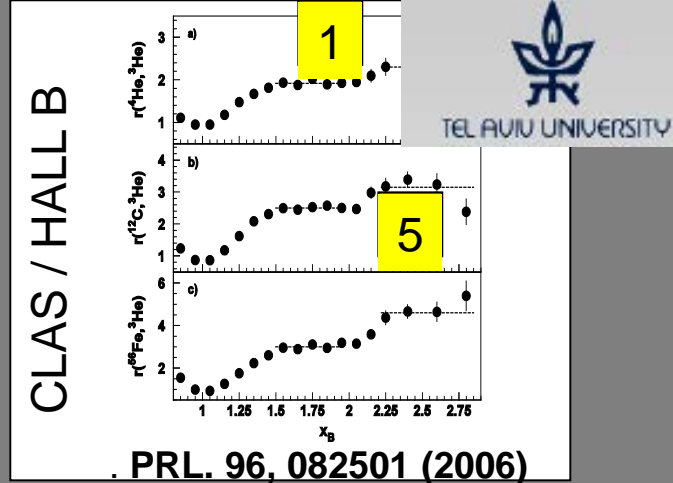
1



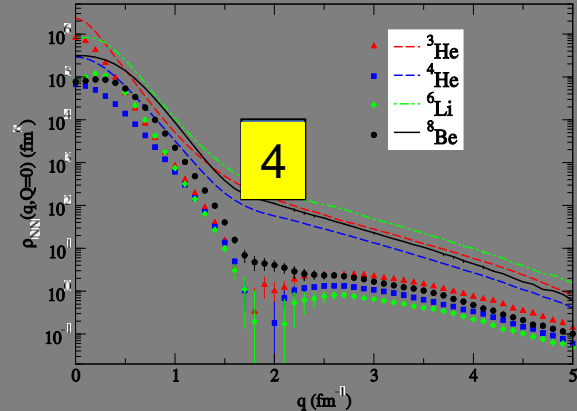
In light asymmetric nuclei :

$$\langle k_{minority} \rangle > \langle k_{majority} \rangle$$

In heavy asymmetric nuclei ?

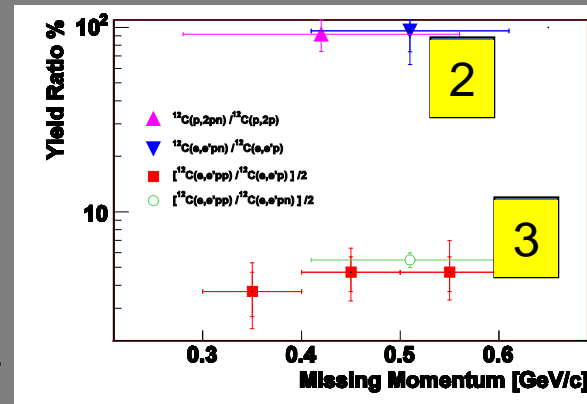


PRL 96, 082501 (2006)



PRL 98, 132501 (2007).

EVA / BNL and Jlab / HALLA



PRL 162504(2006); Science 320, 1476 (2008).

# Short distance structure of nuclei

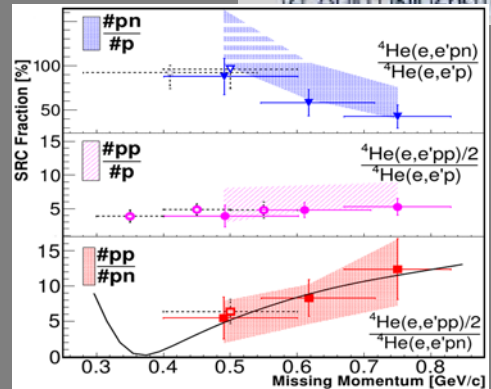


4

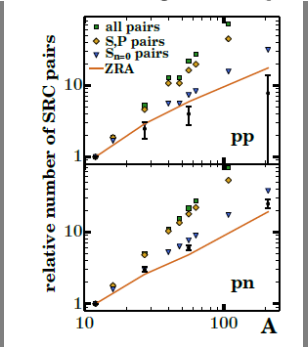
Dominant NN force in the 2N-SRC is tensor force.

The high momentum tail (300-600 MeV/c) is dominated by  
 $L=0,2 \quad S=1 \quad np$  -SRC pairs.

These pairs are produced from  $S_n=0$  IPM pairs



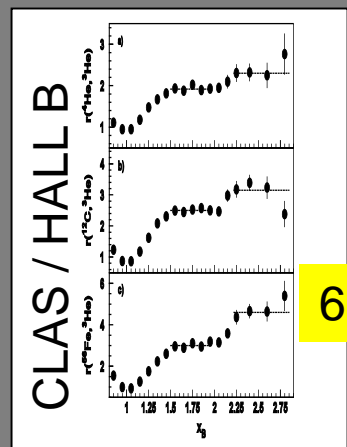
4



6

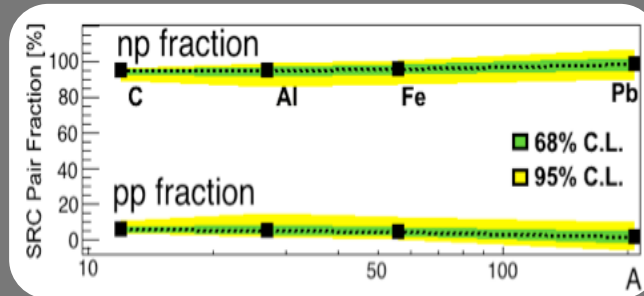
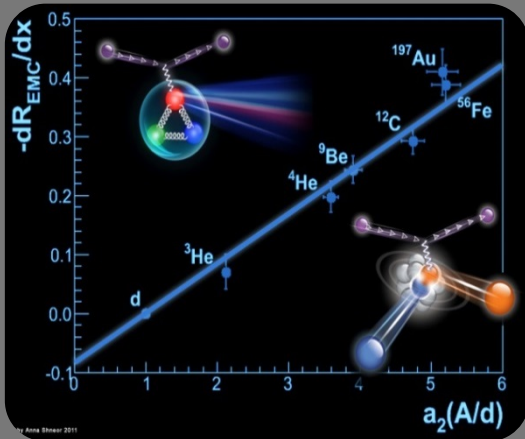
Three nucleon SRC are present in nuclei. They contribute about an order of magnitude less than the 2N\_SRC

Isospin structure ? Geometry ? Abundance ?

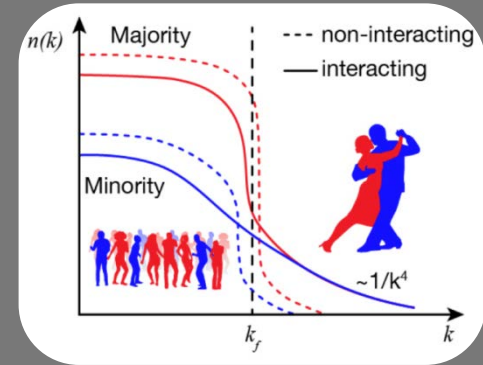


6

# Summary – relevant of Correlations

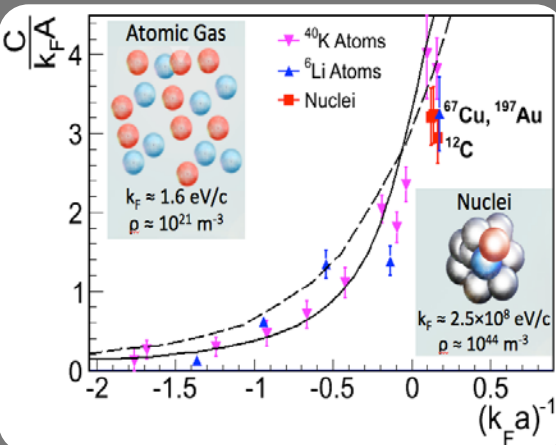


## Nuclear



## Particle

## Atomic



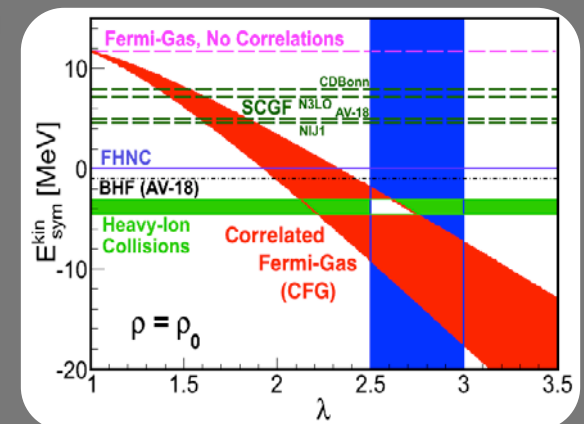
Contact term

## Astro

Symmetry energy



3N-SRC







# Acknowledgment

I would like to thank the organizers for the invitation.



## Collaborators:

Or Hen, Larry Weinstein, Shalev Gilad, Doug Higinbotham, Steve Wood, John Watson

Misak Sargsian, Mark Strikman, Leonid Frankfurt, Gerald Miller







# Some do not like them

From the perspective of nuclear many-body calculations short-range correlations are not a desired feature but pose a severe problem. †

Short-range correlations in nuclei with similarity renormalization group transformations

T. Neff,<sup>1,\*</sup> H. Feldmeier,<sup>1,2</sup> and W. Horiuchi<sup>3</sup>

arXiv:1506.02237v1 [nucl-th] 7 Jun 2015

Some theoreticians denied their existence

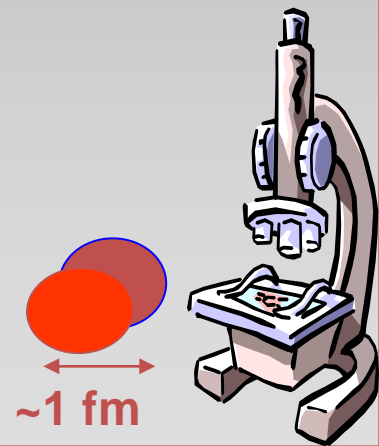


# Short range correlations

“The **structure of correlated many-body systems**, particularly at distance scales small compared to the radius of the constituent nucleons, **presents a formidable challenge to both experiment and theory**”

(Nuclear Science: A Long Range Plan, The DOE/NSF Nuclear Science Advisory Committee, Feb. 1996 [1].)

**This long standing challenge for nuclear physics can experimentally be effectively addressed thanks to high intensity and high momentum transfer reached by present facilities.**

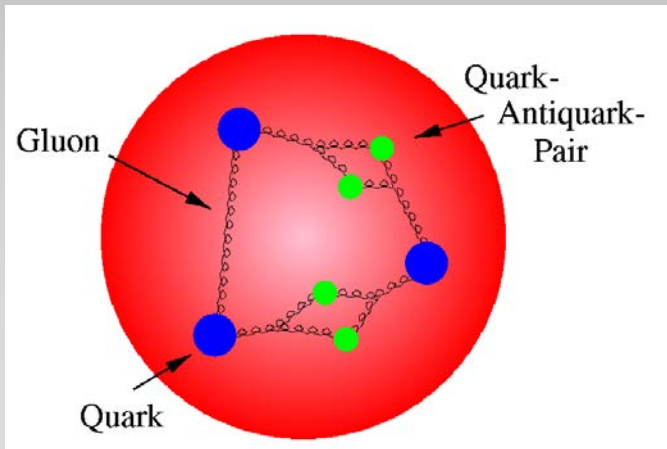
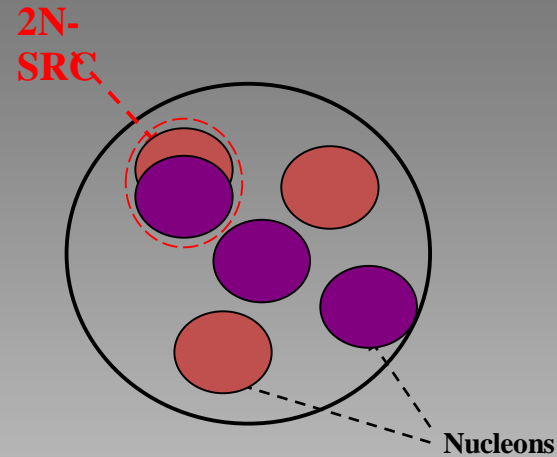


Hard scattering is of particular interest because it has the resolving power required to probe the internal (partonic) structure of a complex target

## Hard nuclear reactions

hadronic structure of nuclei

Scale:  
several GeV

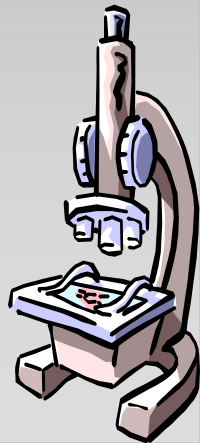


DIS

Scale:  
several tens of GeV

partonic structure  
of hadrons

~1 fm





# SRC Outreach

## Particle Physics

The EMC Effect.  
Neutrino-Nucleus Scattering.  
The NuTeV Anomaly.

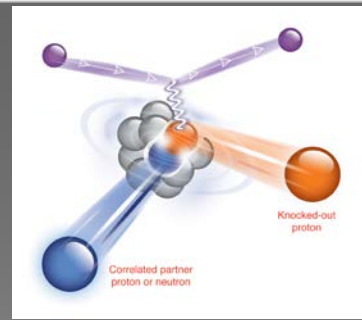
## Astrophysics

Neutron Stars.  
Nuclear Symmetry Energy.

## Quantum \ Atomic Physics

Energy Sharing in Imbalance Fermi Systems.  
Contact Interaction in Universal Fermi Systems.

# Number of hard triple coincidence events (World data)



experiment	pp pairs	np pairs	nn pairs
EVA/BNL	-	18	-
E01-015/JLab	263	179	-
E07-006/JLab	50	223	-
CLAS/JLab	1533	-	-
Total	<2000	<450	0

$^{12}\text{C}(p, 2pn)$

$^{12}\text{C}(e, e' pn)$   $^{12}\text{C}(e, e' pp)$

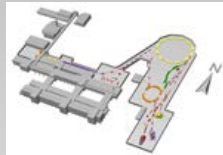
$^4\text{He}(e, e' pn)$   $^4\text{He}(e, e' pp)$

C, Al, Fe, Pb ( $e, e' pp$ )

**5 GeV/c  $10^9$  protons/sec fixed target**



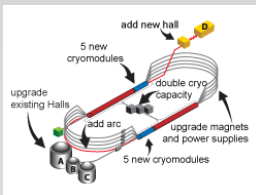
**Nuclotron**



**J-PARC**  
Japan Proton Accelerator

**→ >10k events/100 Hr**

**12 GeV electrons at JLab fixed target**



**X5-10 Mott cross section**

**X10 Luminosity in CLAS12**

# Why several GeV and up protons are good probes of SRC ?

☀ They have Small deBroglie wavelength:

$$\lambda = h/p = hc/pc = 2\pi \cdot 0.197 \text{ GeV-fm}/(6 \text{ GeV}) \approx 0.2 \text{ fm.}$$

☀ Large momentum transfer is possible

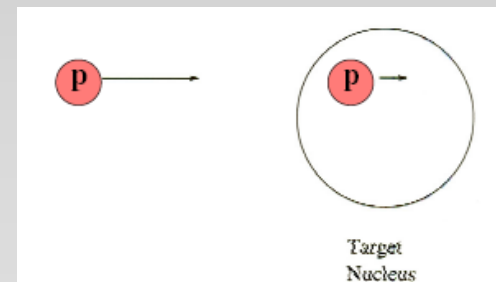
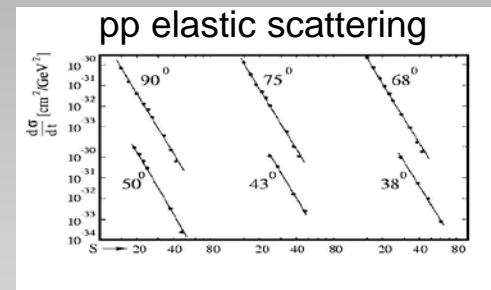
With wide angle scattering

☀ The  $s^{-10}$  dependence of the p-p elastic scattering preferentially selects high momentum nuclear protons.

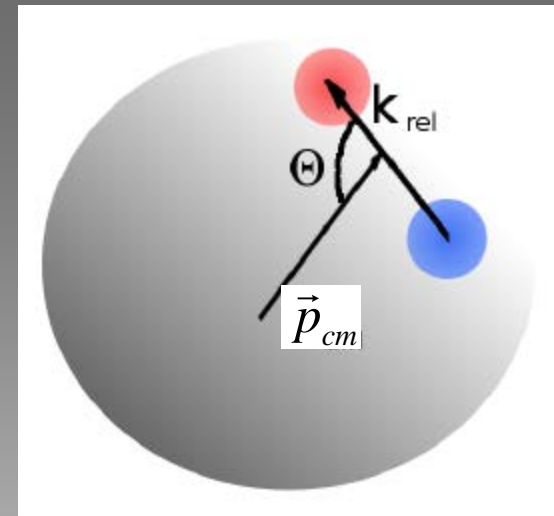
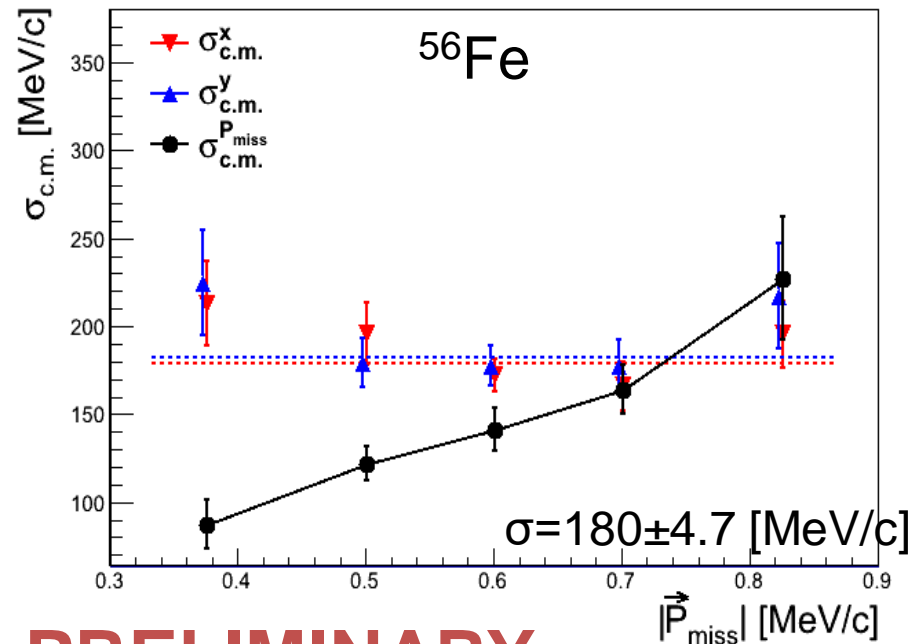
For pp elastic scattering near  $90^\circ$  cm

$$\frac{d\sigma}{dt} \propto s^{-10}$$

QE pp scattering near  $90^\circ$  have a very strong preference for reacting with forward going high momentum nuclear protons

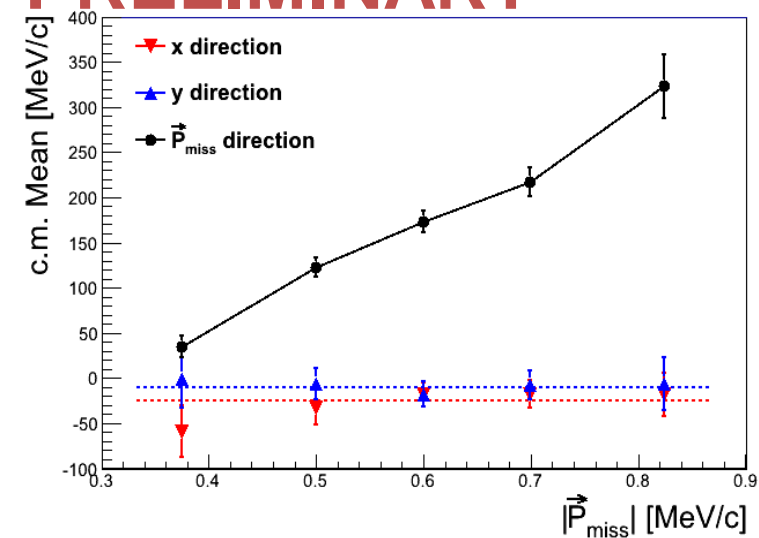


# C.M. motion of the pair



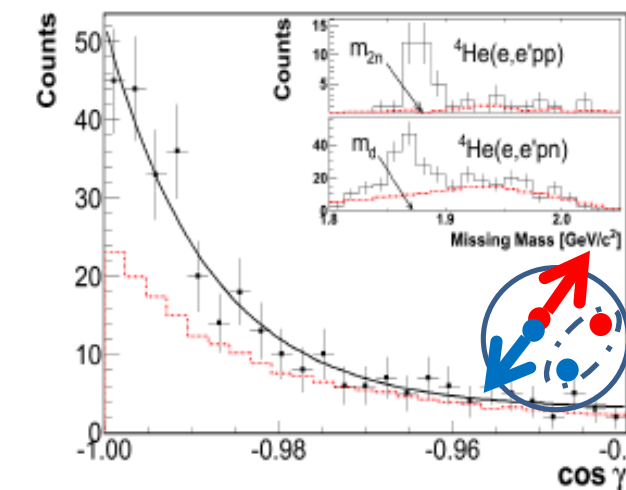
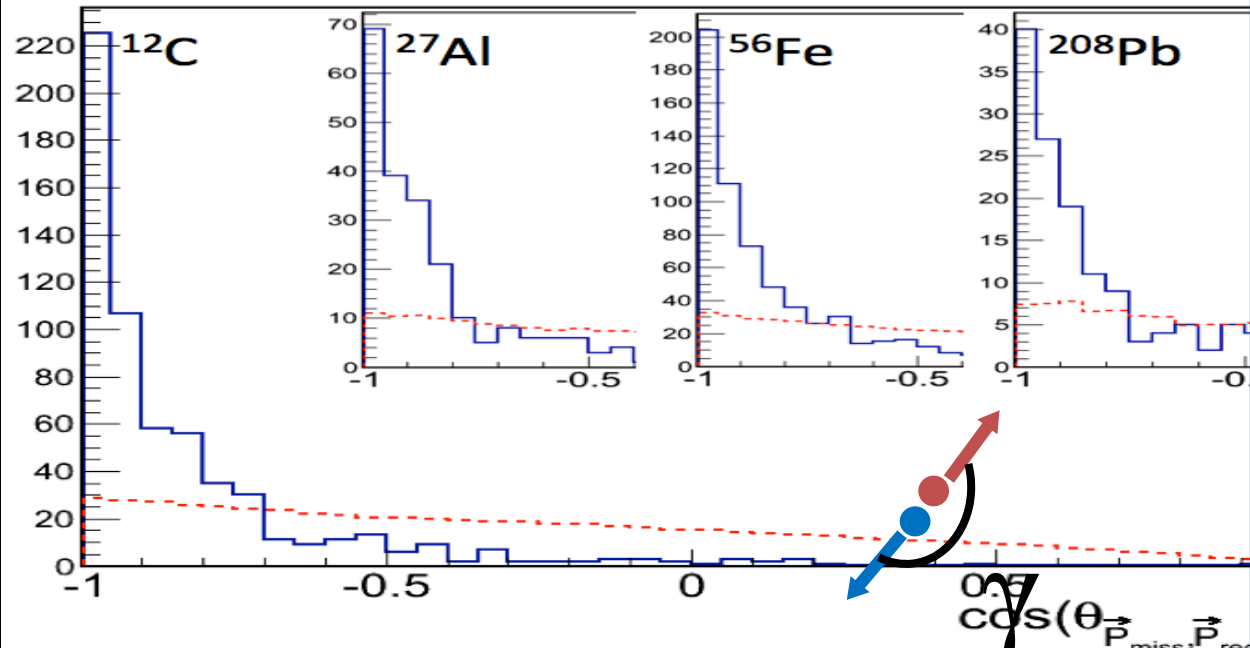
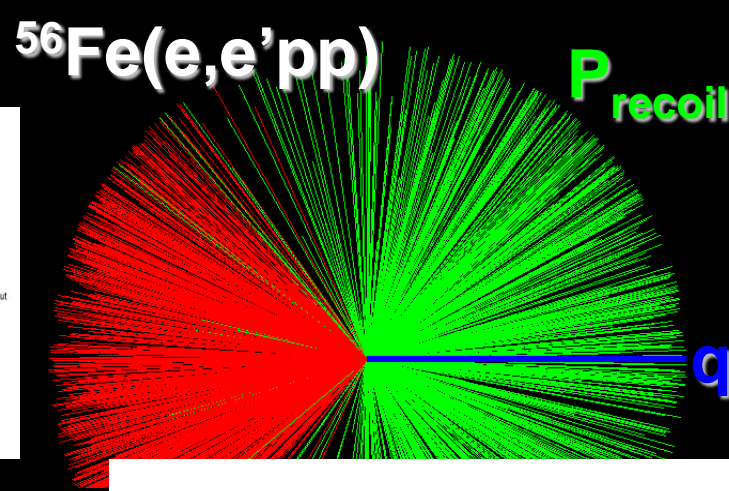
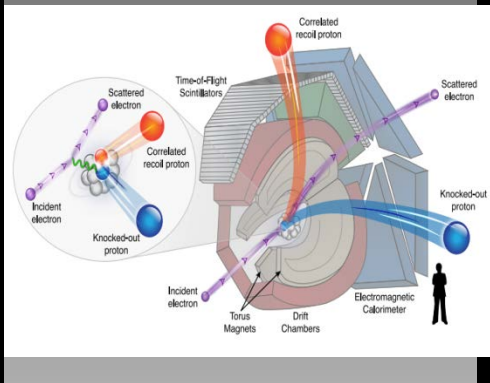
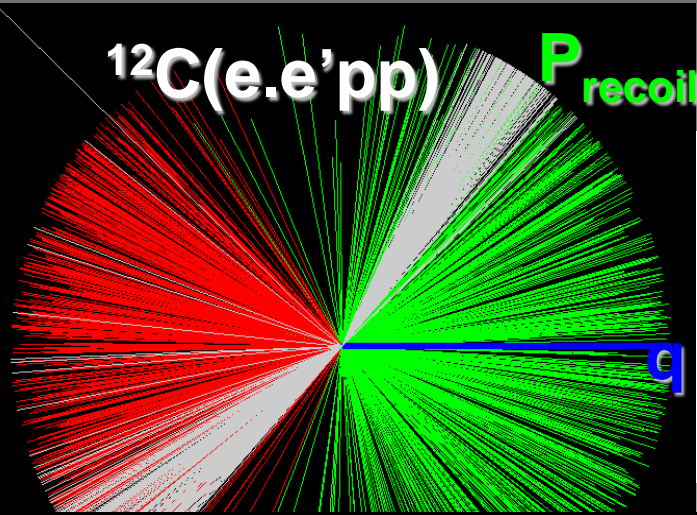
$$\vec{p}_{cm} = \vec{p}_{miss} + \vec{p}_{recoil}$$

**PRELIMINARY**



	$\sigma_x$	$\sigma_y$
$^{12}\text{C}$	$169 \pm 7$	$164 \pm 6$
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$^{56}\text{Fe}$	$179 \pm 6$	$182 \pm 7$
$^{208}\text{Pb}$	$208 \pm 18$	$186 \pm 16$

# JLab / CLAS, Data Mining, EG2 data set

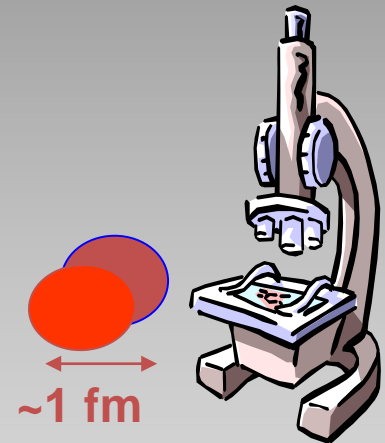


$^4\text{He}(e,e'pp)$   $^4\text{He}(e,e'pn)$   
JLab /Hal A Exp 07-0

“The **structure of correlated many-body systems**, particularly at distance scales small compared to the radius of the constituent nucleons, **presents a formidable challenge to both experiment and theory**”

(Nuclear Science: A Long Range Plan, The DOE/NSF Nuclear Science Advisory Committee, Feb. 1996 [1].)

This long standing challenge for nuclear physics can experimentally be effectively addressed thanks to high intensity and high momentum transfer reached by present facilities.



**5-10 GeV/c  $10^9$  protons/sec fixed target**

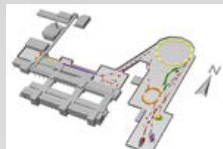
**→ >10k events/100 Hr**



CSR  
Lanzhou



Dubna



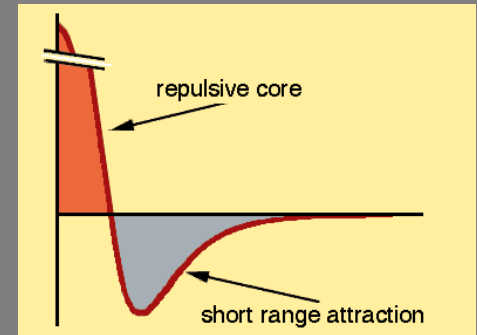
GSI / FAIR



# Nuclear Physics 101

- Many-Body Hamiltonian:

$$H = \sum_{i=1}^A \frac{p_i^2}{2m_N} + \sum_{i<j=1}^A V_{2N}(i, j) + \sum_{i<j<k=1}^A V_{3N}(i, j, k) +$$

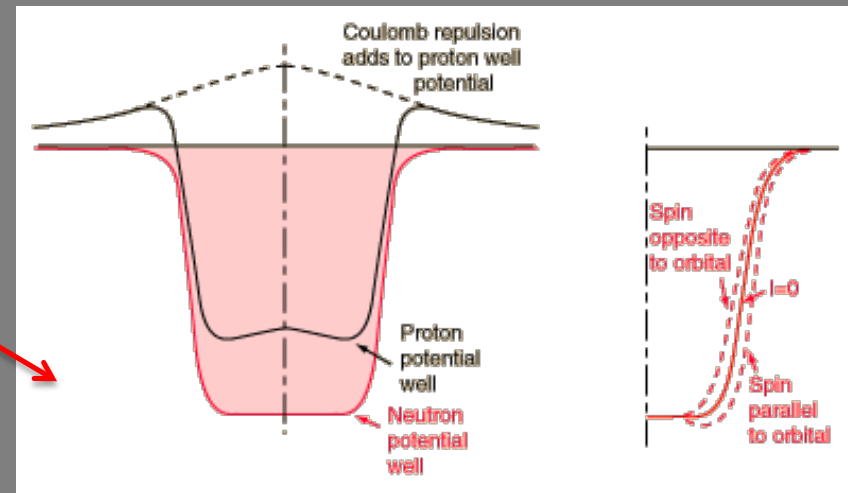


- Mean-Field Approximation:

$$H = \sum_{i=1}^A \frac{p_i^2}{2m_N} + \sum_{i=1}^A V(i)$$

Results in an “atom-like” shell model:

- Ground state energies
- Excitation Spectrum
- ...



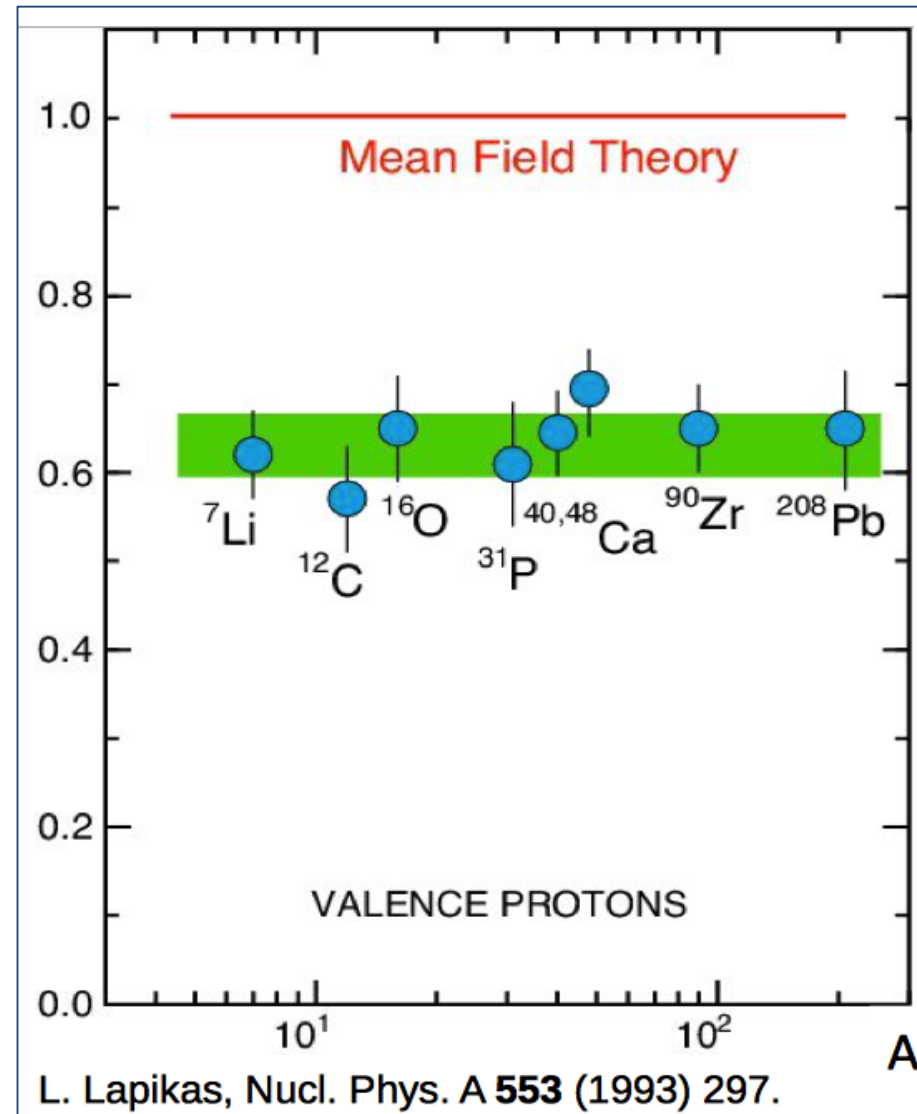
E. Wigner, M. Mayer, and J. Janssen  
1963 Nobel Prize

## Beyond the Shell-Model: NN Correlations

# Beyond the Shell-Model: NN Correlations

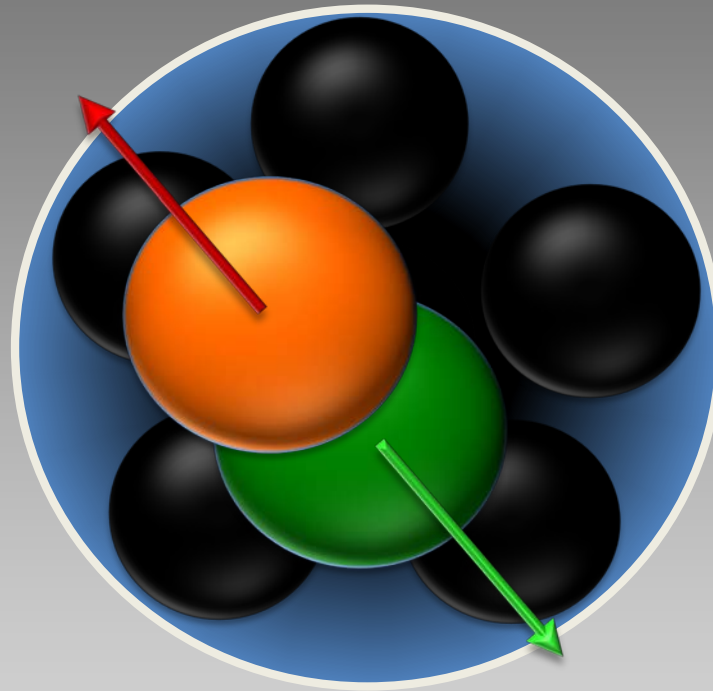
- Spectroscopic factors extracted from  $A(e, e'p)$  measurements yield only 60-70% of the expected single-particle strength

- Missing:
  - ~20%: Long-Range Correlations
  - ~20%: Short-Range Correlations (SRC)





# Hard exclusive triple – coincidence measurements

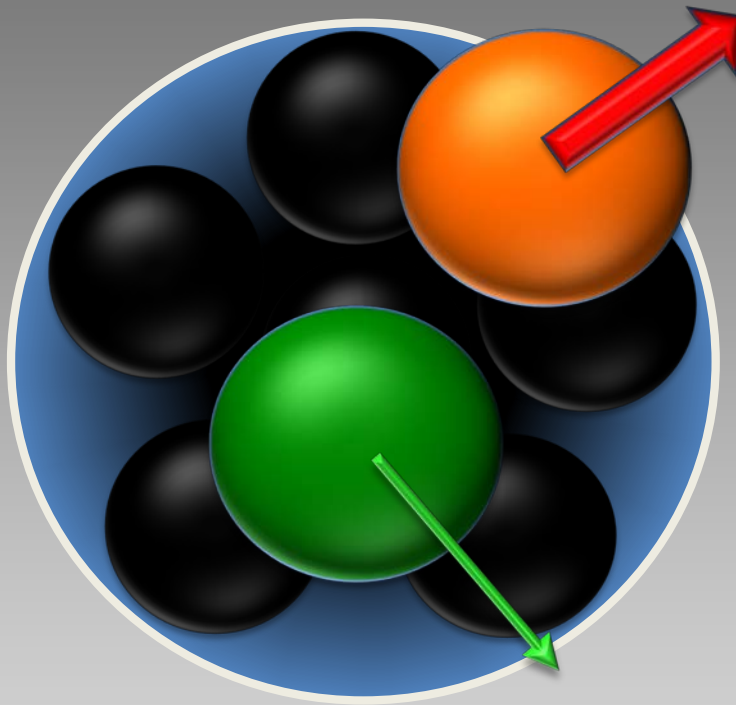


**Quasi-Free scattering off a nucleon  
in a short range correlated pair**

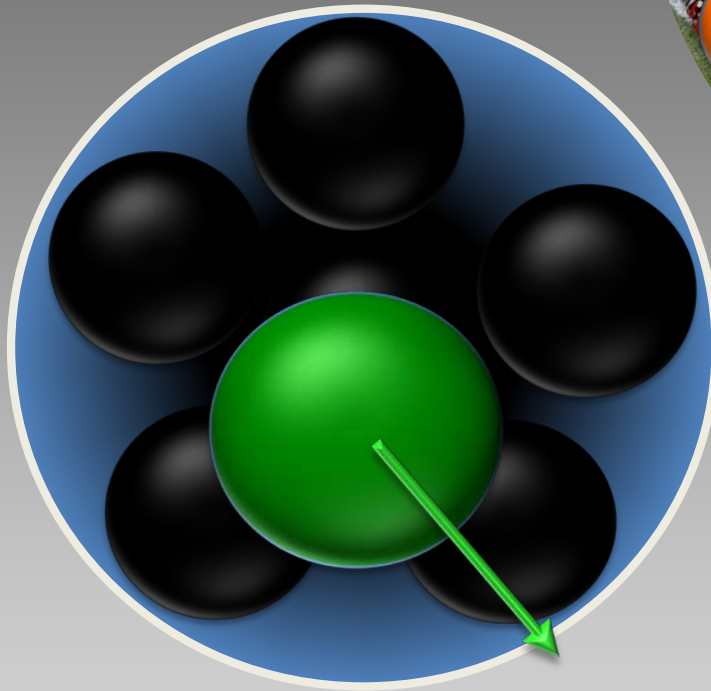
# triple – coincidence measurements



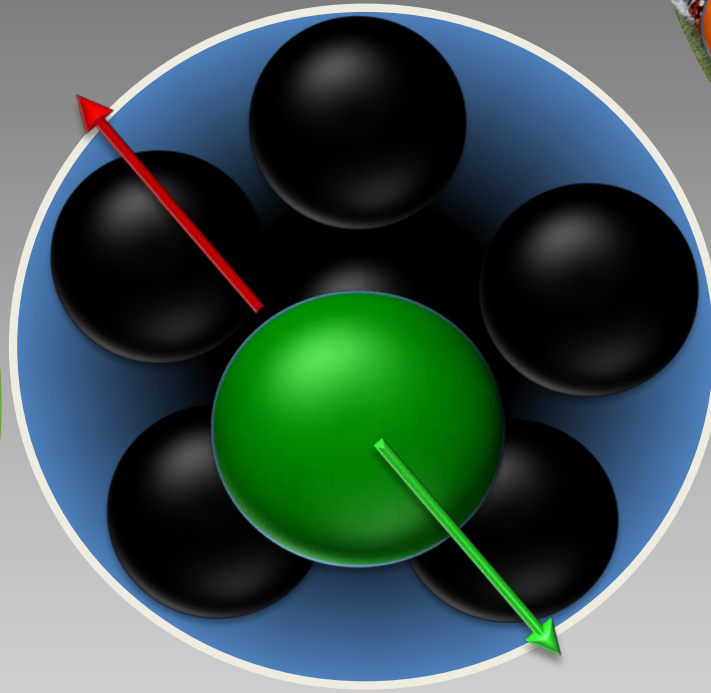
# triple – coincidence measurements



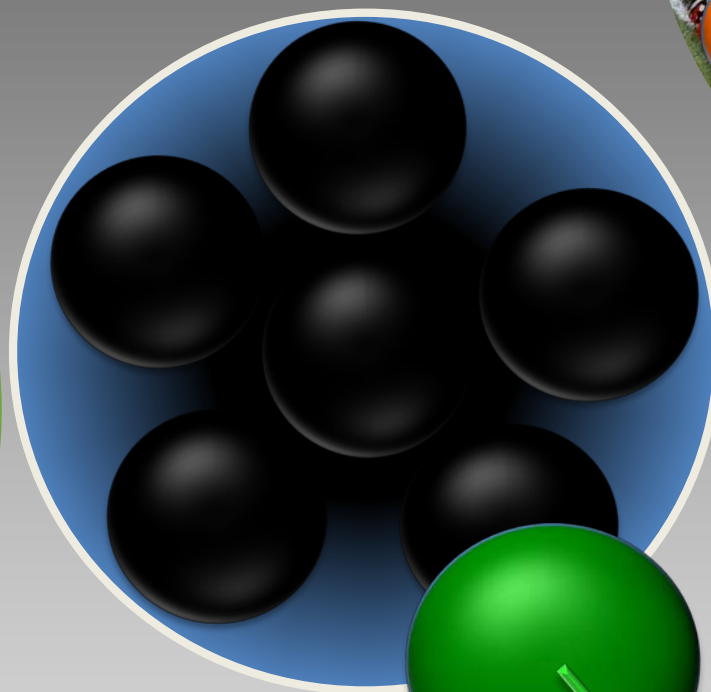
# triple – coincidence measurements



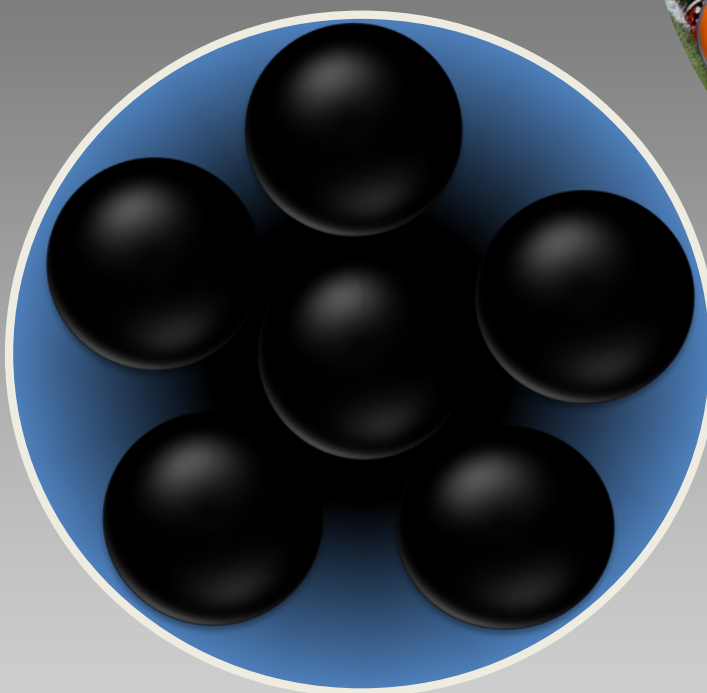
# triple – coincidence measurements



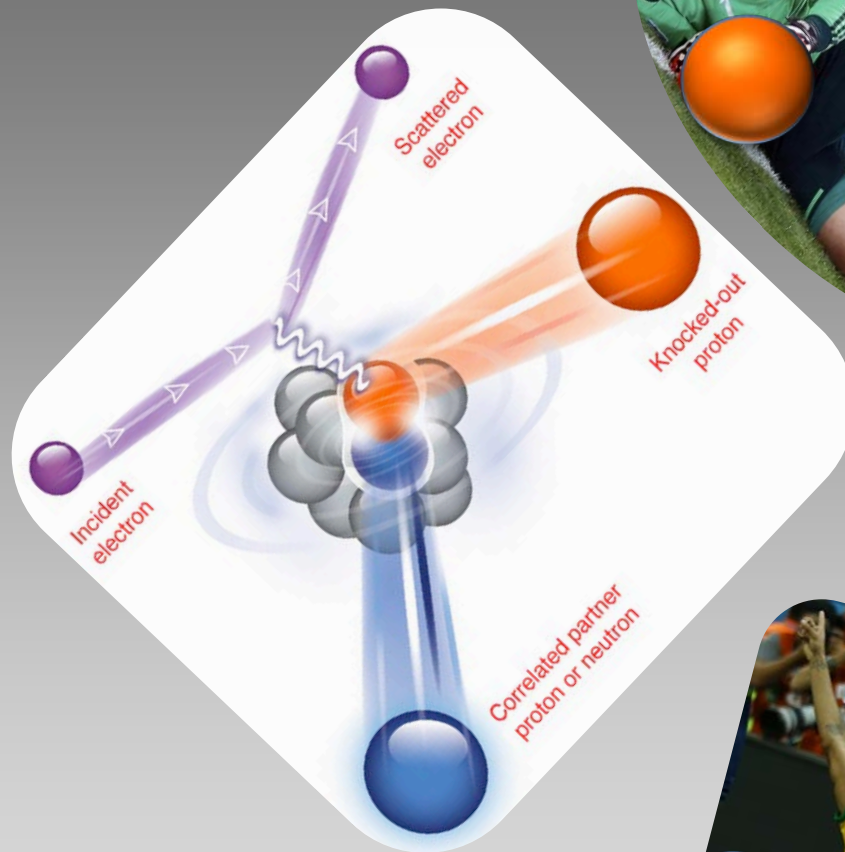
# triple – coincidence measurements



# triple – coincidence measurements



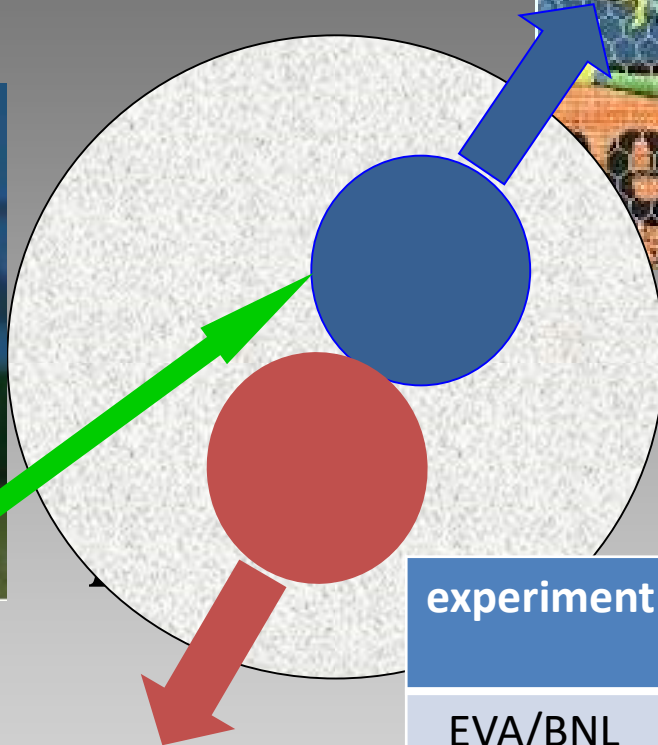
# triple – coincidence measurements



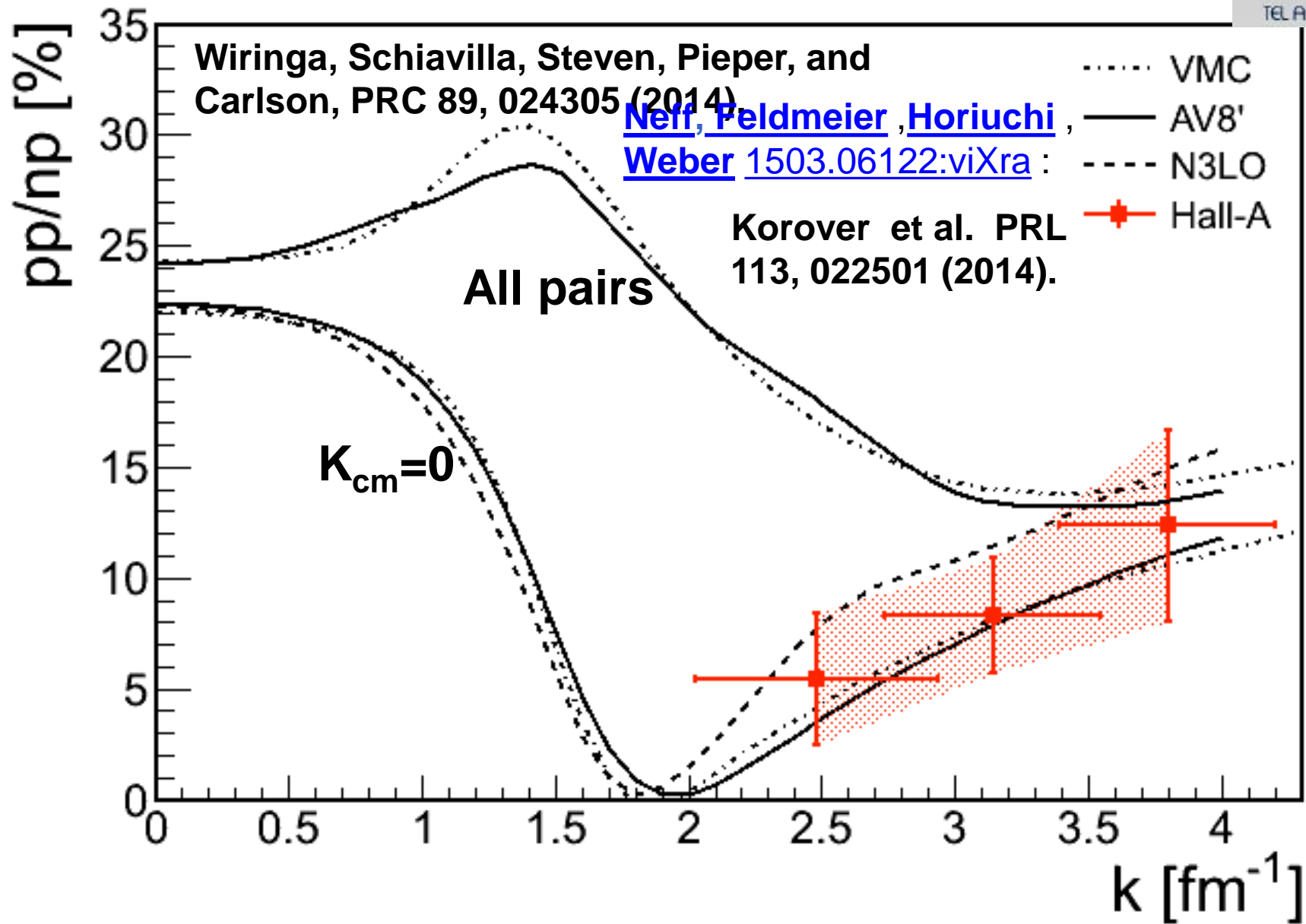


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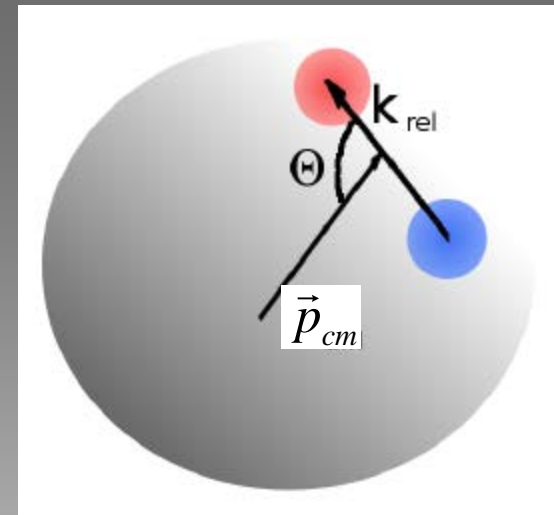
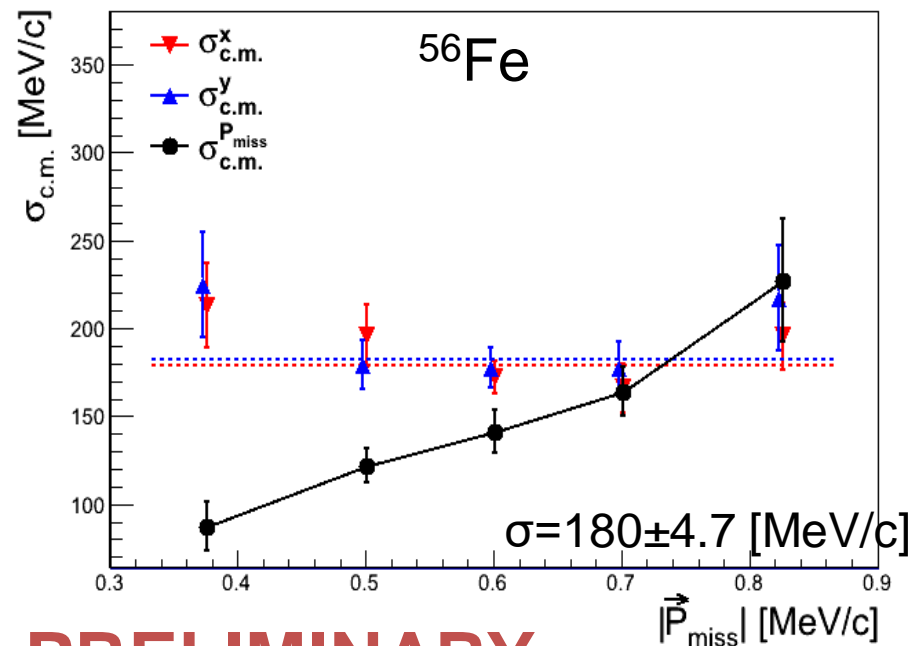
Hard exclusive triple – coincidence measurements



experiment	nuclei	pairs	$P_{miss}$ [MeV/c]
EVA/BNL	$^{12}\text{C}$	pp only	300-600
E01-015/ Jlab	$^{12}\text{C}$	pp and np	300-600
E07-006/ JLab	$^4\text{He}$	pp and np	400-850
CLAS/JLab	C, Al, Fe, Pb	pp only	300-700

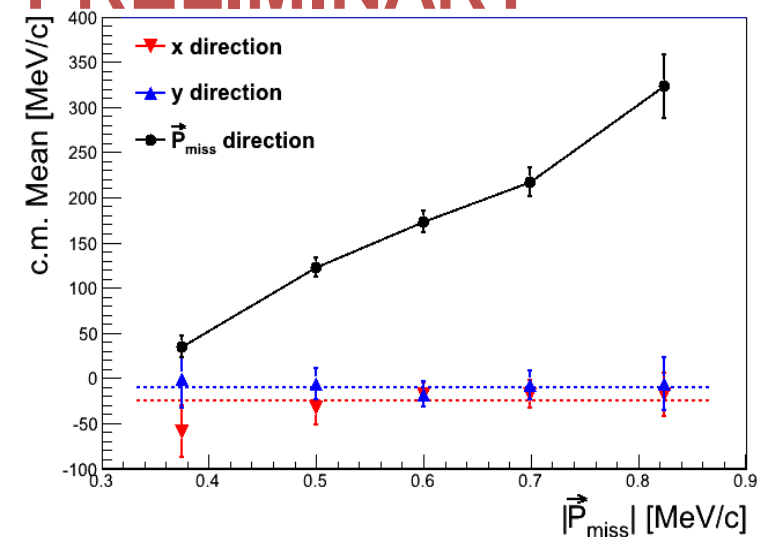


# C.M. motion of the pair



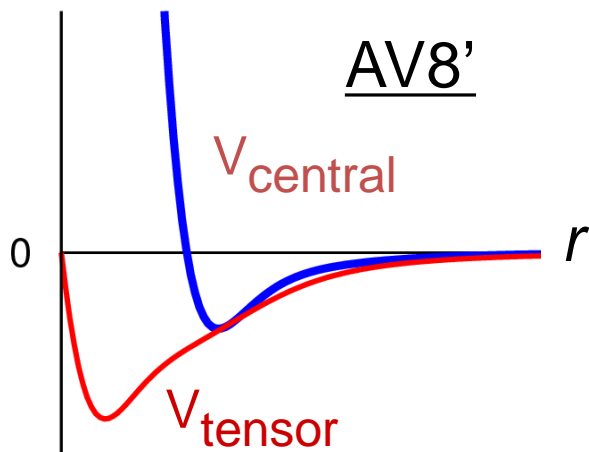
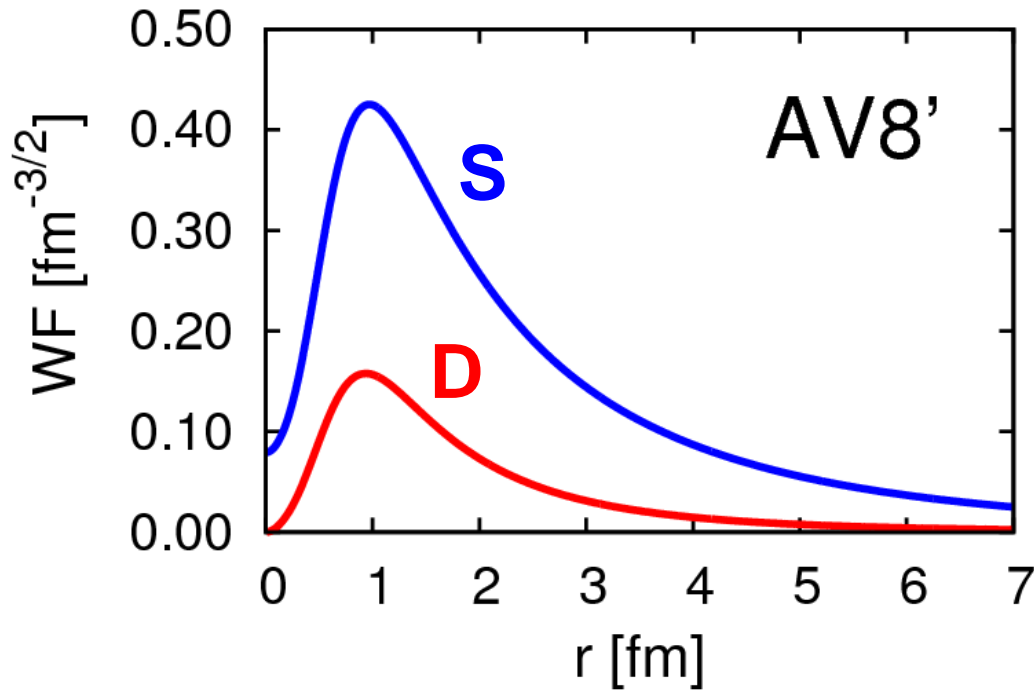
$$\vec{p}_{cm} = \vec{p}_{miss} + \vec{p}_{recoil}$$

**PRELIMINARY**



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$^{208}\text{Pb}$	$208 \pm 18$	$186 \pm 16$

# Deuteron properties & tensor force



$$R_m(s) = 2.00 \text{ fm}$$

$$R_m(d) = 1.22 \text{ fm}$$

Energy	-2.24 MeV
Kinetic	19.88
Central	-4.46
<b>Tensor</b>	<b>-16.64</b>
LS	-1.02
P(L=2)	5.77%
Radius	1.96 fm

*d*-wave is  
**“spatially compact”**  
 (high momentum)

# E01-015: A customized Experiment to study 2N-SRC

$$Q^2 = 2 \text{ GeV}/c, \quad x_B \sim 1.2, \quad P_m = 300-600 \text{ MeV}/c, \quad E_{2m} < 140 \text{ MeV}$$

$$\text{Luminosity} \sim 10^{37-38} \text{ cm}^{-2}\text{s}^{-1}$$

## Kinematics optimized to minimize the competing processes

### High energy, Large $Q^2$

The large  $Q^2$  is required to probe the small size SRC configuration.

MEC are reduced as  $1/Q^2$ .

Large  $Q^2$  is required to probe high  $P_{\text{miss}}$  with  $x_B > 1$ .

FSI can be treated in Glauber approximation.

### $x_B > 1$

Reduced contribution from isobar currents.

### Large $p_{\text{miss}}$ , and $E_{\text{miss}} \sim p_{\text{miss}}^2/2M$

### Large $P_{\text{miss } z}$

## FSI

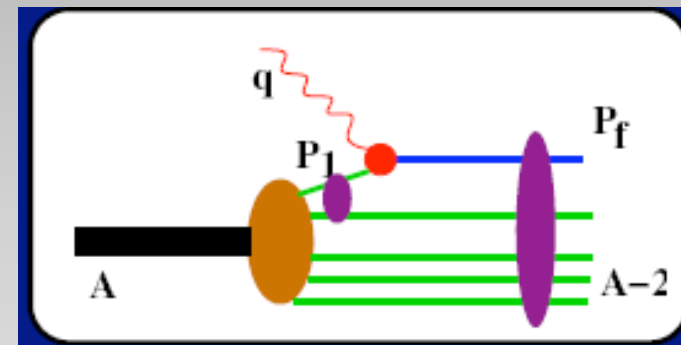
### FSI with the A-2 system:

- ★ Small (10-20%) .
  - Kinematics with a large component of  $p_{\text{miss}}$  in the virtual photon direction.
  - Pauli blocking for the recoil particle.
  - Geometry,  $(e, e'p)$  selects the surface.
- ★ Can be treated in Glauber approximation.
- ★ Canceled in some of the measured ratios.

### FSI in the SRC pair:

These are not necessarily small, BUT:

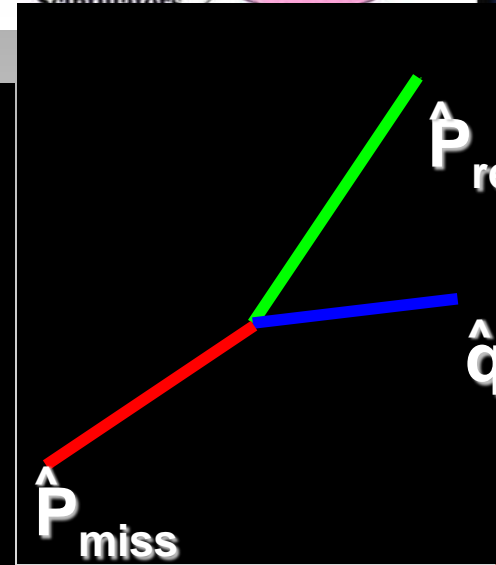
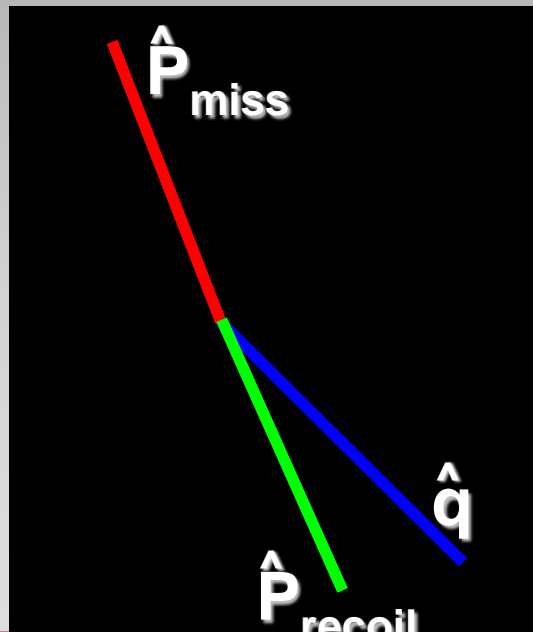
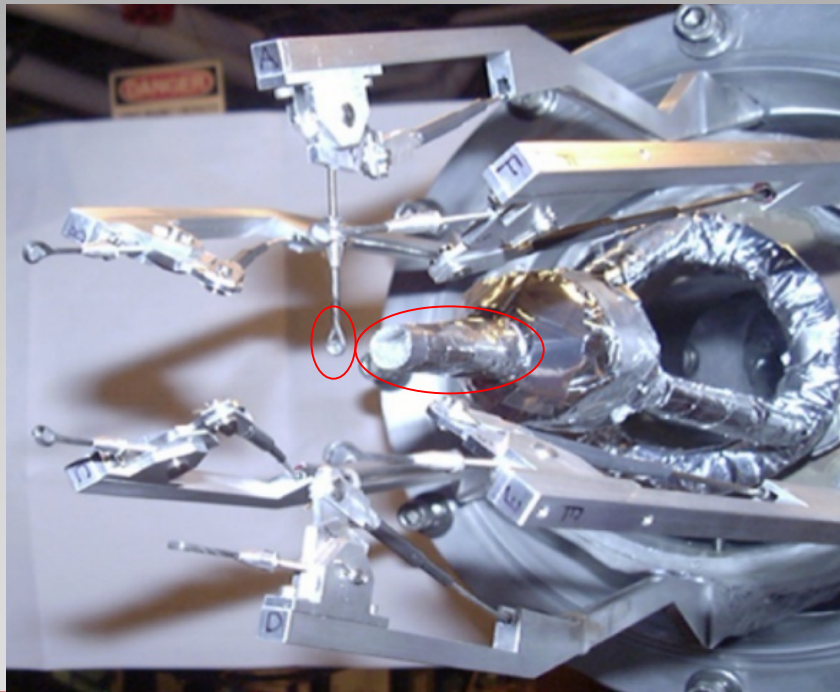
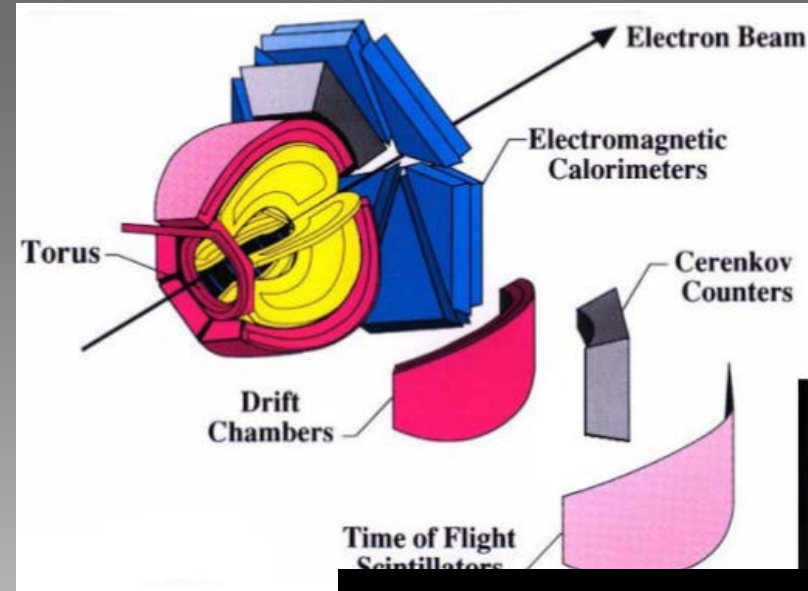
- ★ Conserve the isospin structure of the pair .
- ★ Conserve the CM momentum of the pair.



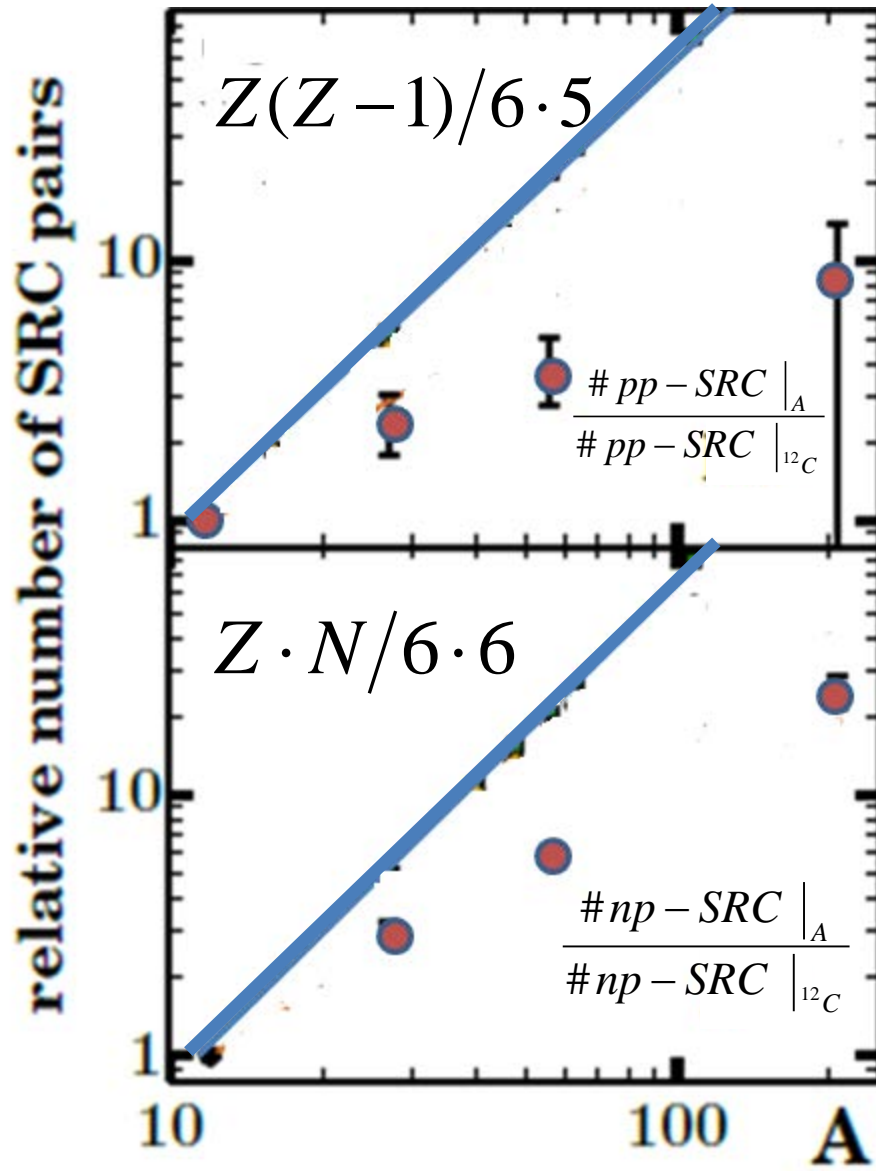
EG2 data set

- Run at 2004 in Hall-B of Jefferson Lab
- 5 GeV electron beam
- Deuterium + Solid target simultaneously

$^{12}\text{C} / ^{56}\text{Fe} / ^{208}\text{Pb}$



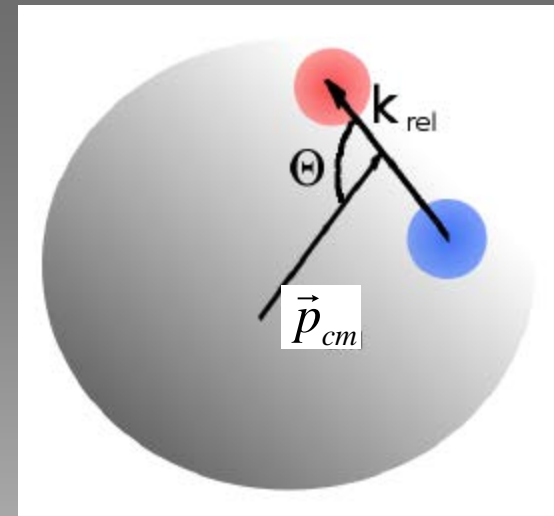
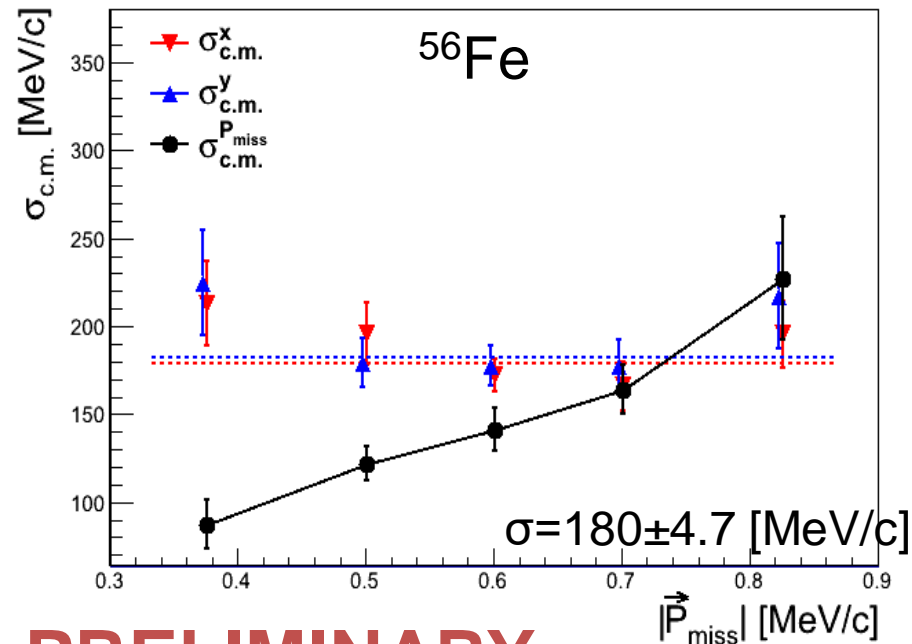
# The mass dependence of the SRC pairs



CLAS JLab data see C. Colle et al.  
<http://arxiv.org/abs/arXiv:1503.06050>

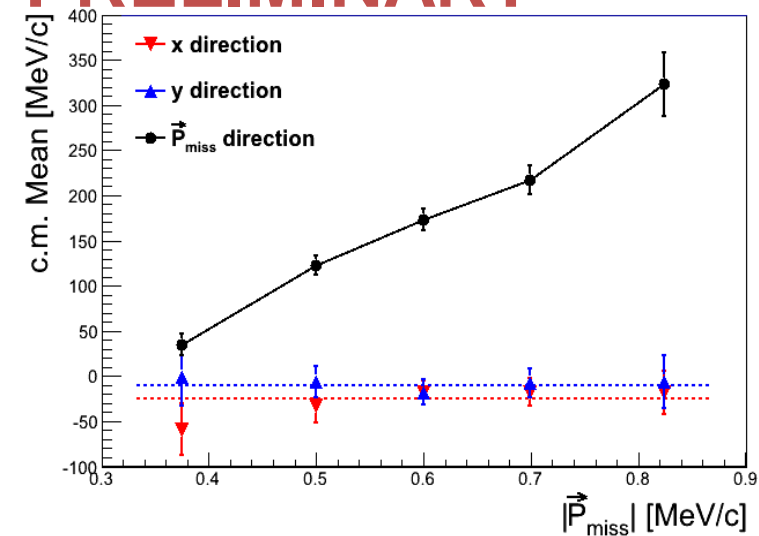


# C.M. motion of the pair

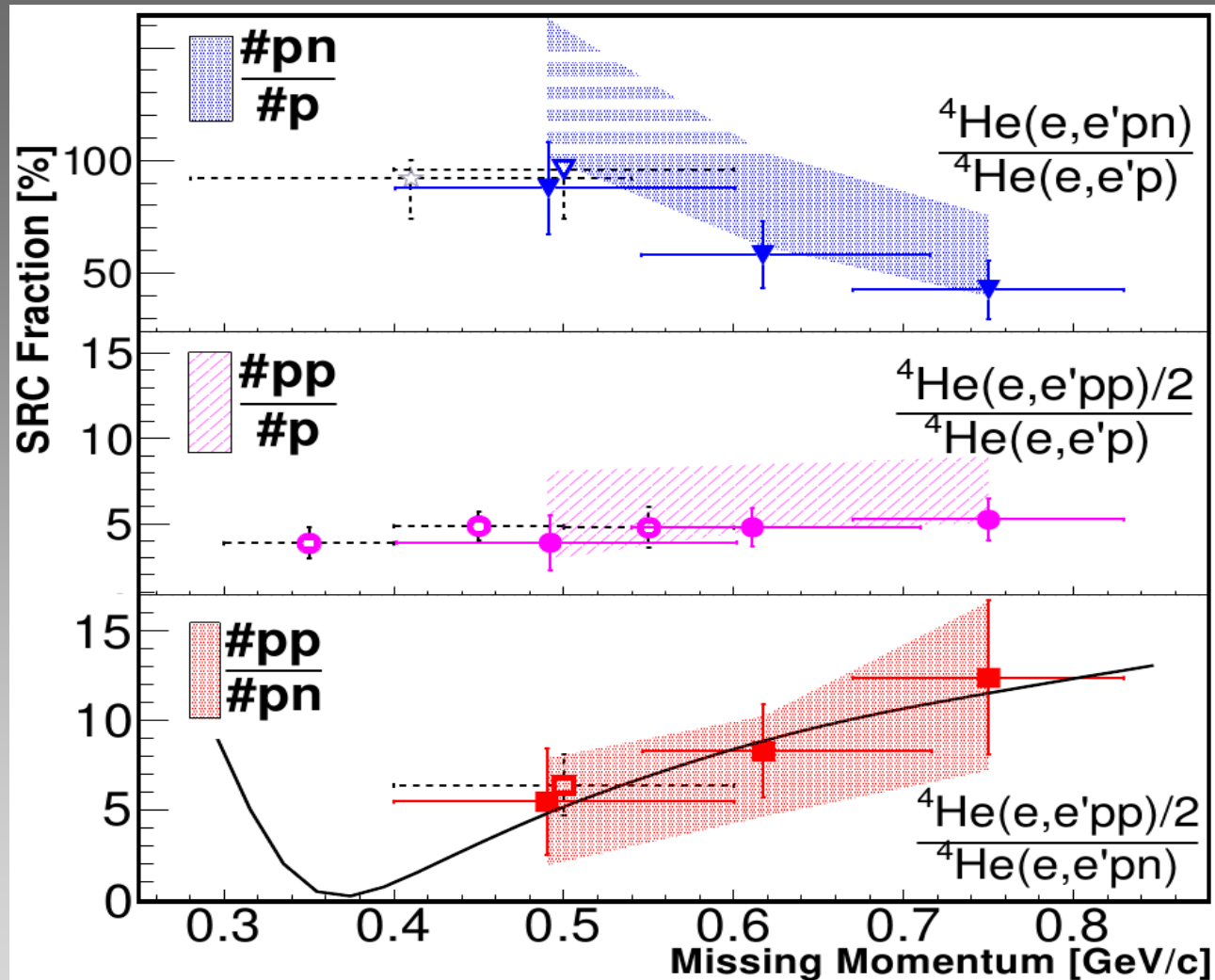


$$\vec{p}_{cm} = \vec{p}_{miss} + \vec{p}_{recoil}$$

**PRELIMINARY**

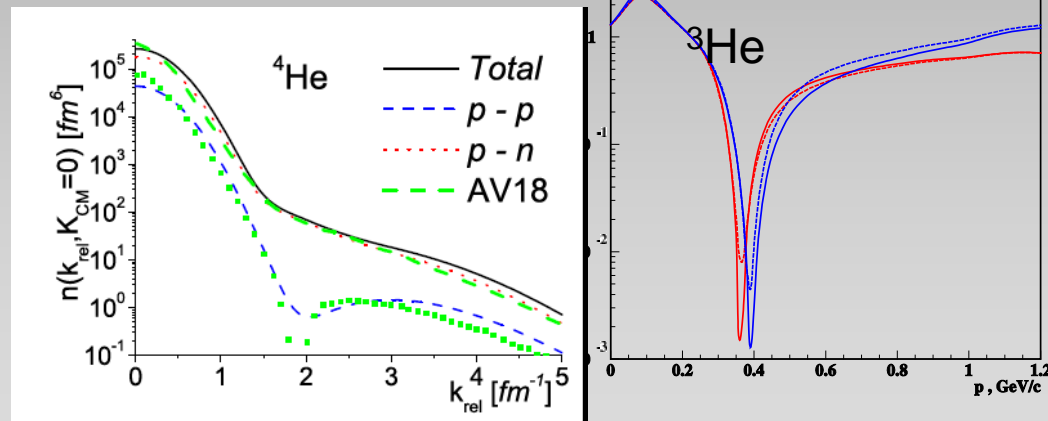
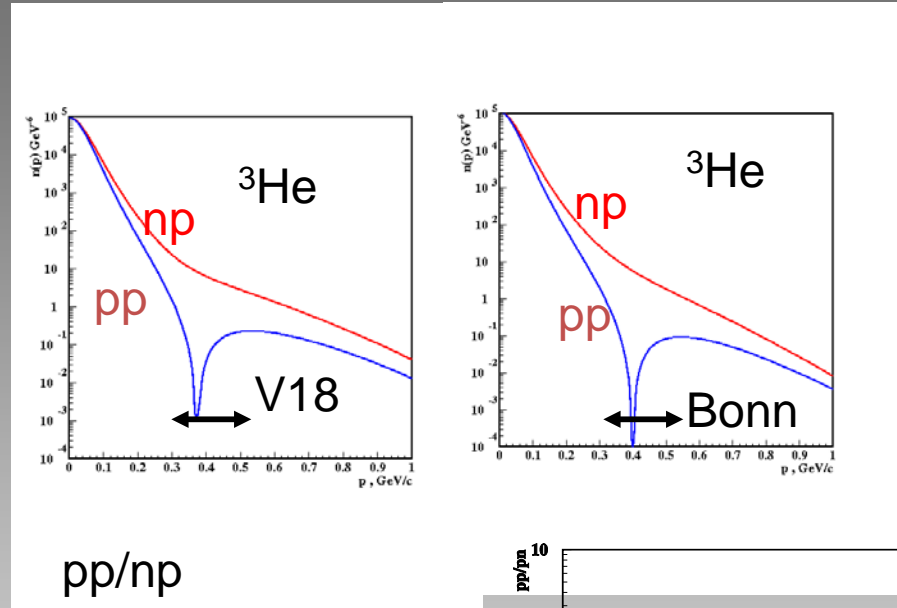
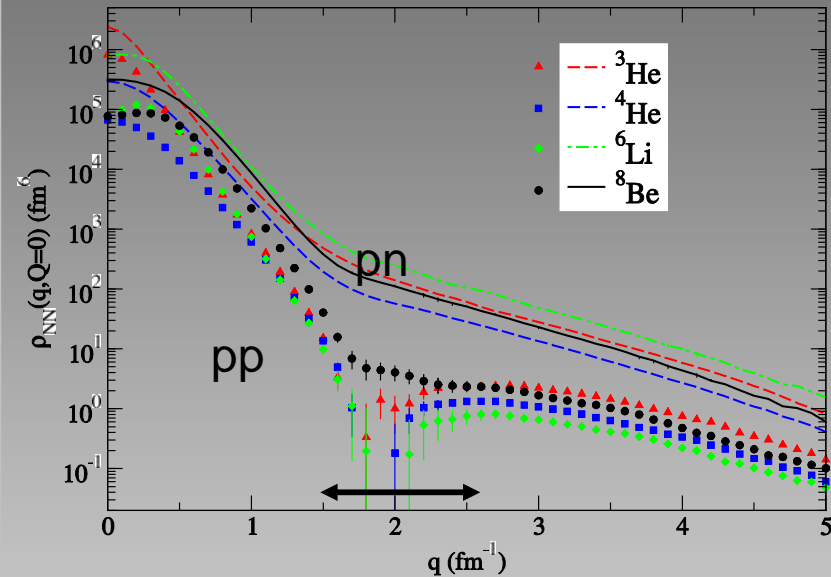


	$\sigma_x$	$\sigma_y$
$^{12}\text{C}$	$169 \pm 7$	$164 \pm 6$
$^{27}\text{Al}$	$162 \pm 10$	$180 \pm 13$
$^{56}\text{Fe}$	$179 \pm 6$	$182 \pm 7$
$^{208}\text{Pb}$	$208 \pm 18$	$186 \pm 16$

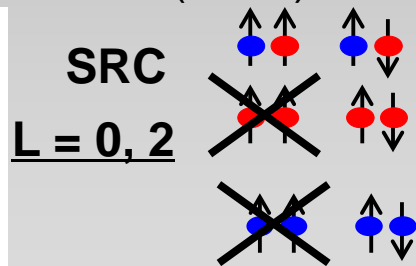
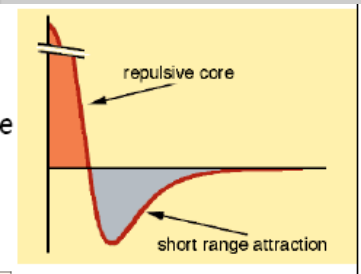


I. Korover et al. Phys. Rev. Let. 113, 022501 (2015)

At 300-600 MeV/c there is an excess strength in the np momentum distribution due to the strong correlations induced by the tensor NN potential.



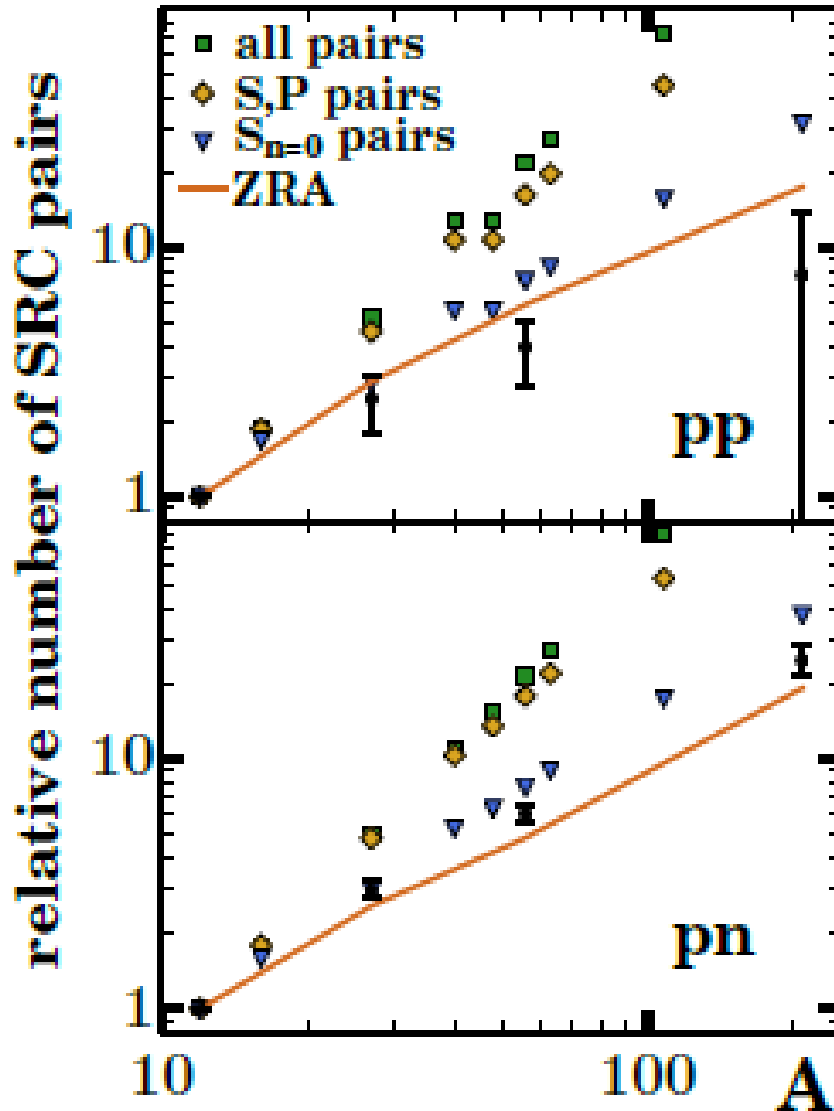
Schiavilla, Wiringa, Pieper, Carson, PRL 98, 132501 (2007).



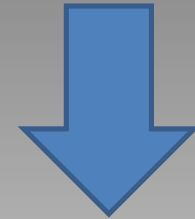
Ciofi and Alvioli  
PRL 100, 162503 (2008).

Sargsian, Abrahamyan, Strikman  
Frankfurt PR C71 044615 (2005)

# The mass dependence of the SRC pairs



**N=0 (nodeless) L=0  
IPM pairs**

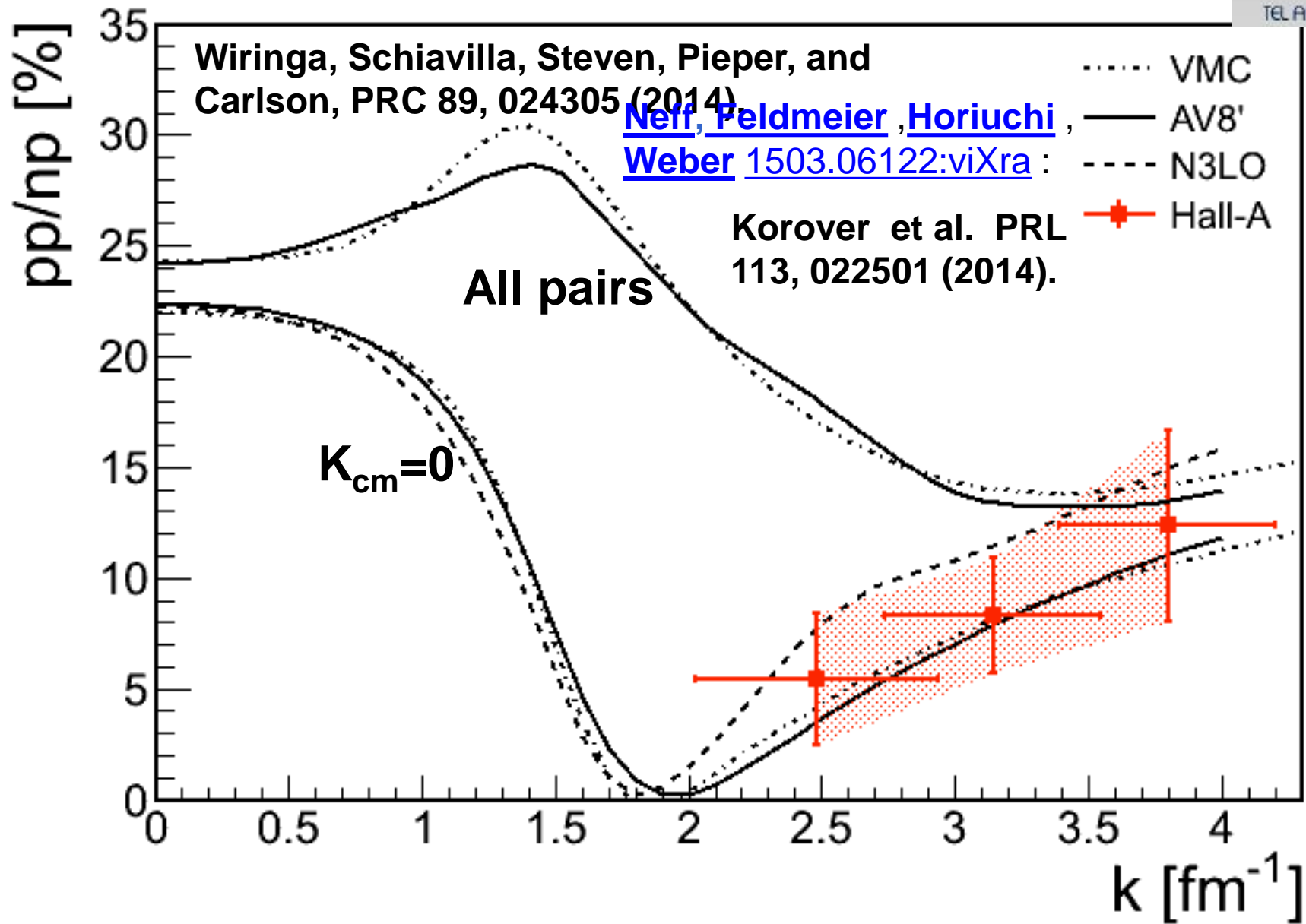


Predominantly:  
**L=0,2 T=0 S=1**  
(deuteron like) **pairs**

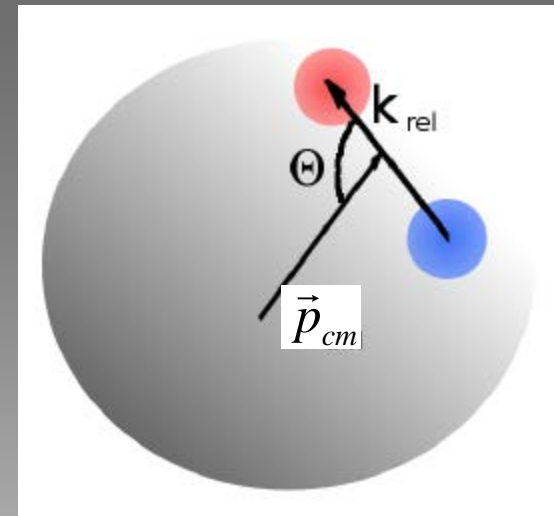
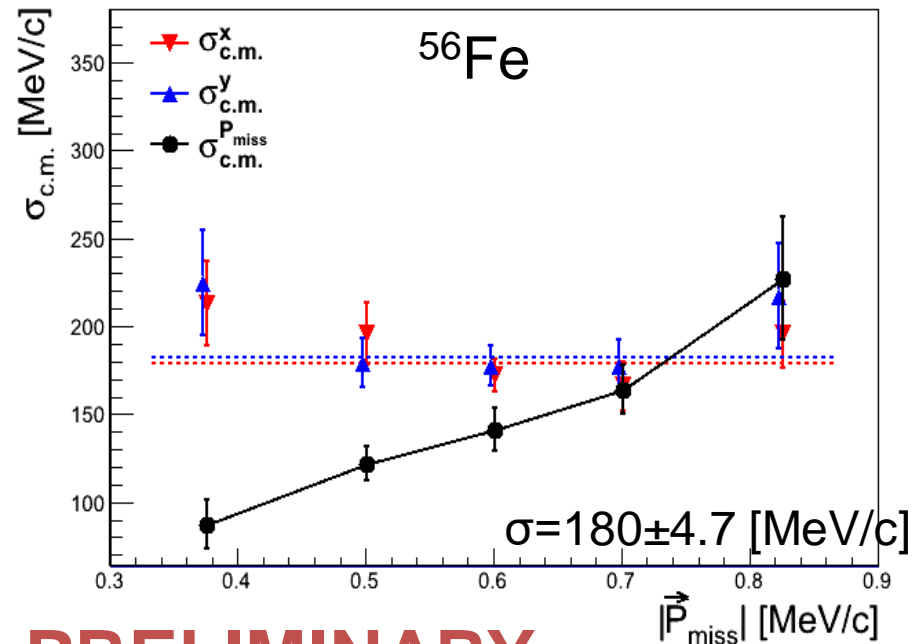
Extracting the Mass Dependence and Quantum Numbers of Short-Range Correlated Pairs from  $A(e, e'p)$  and  $A(e, e'pp)$  Scattering

C. Colle,<sup>1</sup> O. Hen,<sup>2</sup> W. Cosyn,<sup>3</sup> I. Korover,<sup>3</sup> E. Piasetzky,<sup>3</sup> J. Ryckebusch,<sup>3</sup> and L.B. Weinstein<sup>3</sup>

<http://arxiv.org/abs/arXiv:1503.06050>

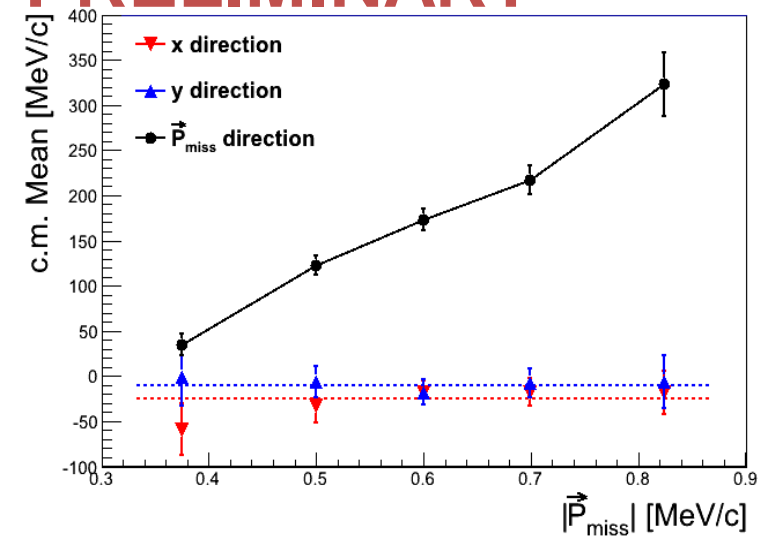


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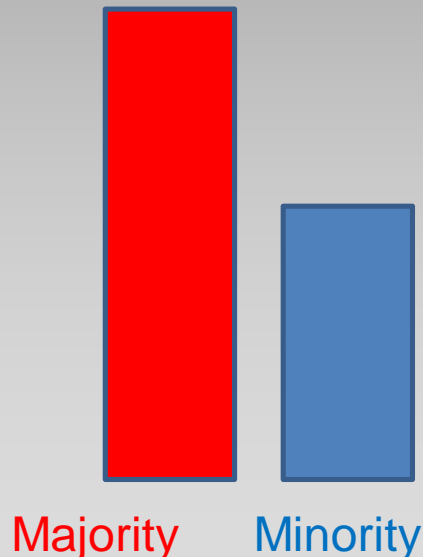


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# Momentum sharing in Asymmetric (imbalanced) two components Fermi systems

non interacting Fermions

Pauli exclusion principle →



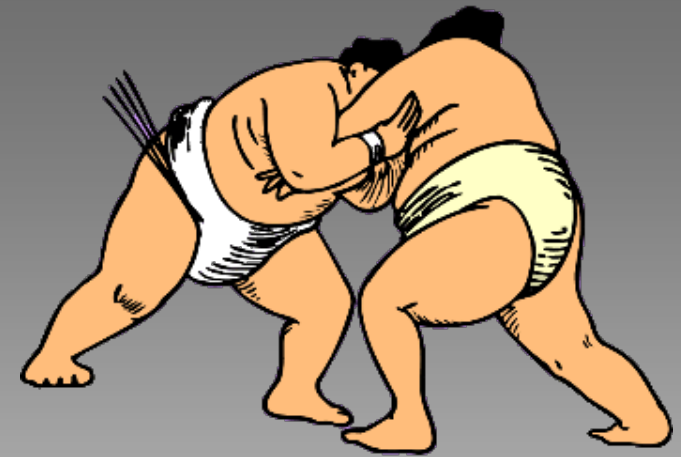
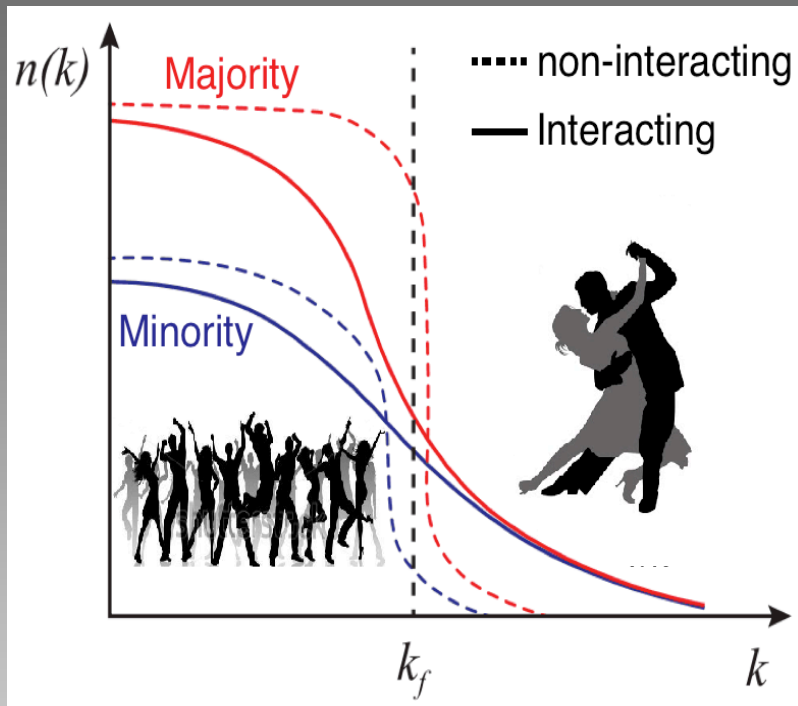
$$k_F^{Majority} > k_F^{Minority}$$

$$\langle T_{Majority} \rangle > \langle T_{Minority} \rangle$$

$$\langle k_{Majority} \rangle > \langle k_{Minority} \rangle$$



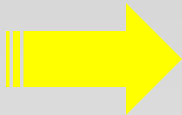
with short-range interaction : strong between unlike fermions, weak between same kind.



# Who wins?

**Universal property**

A minority fermion have a greater probability than a majority fermion to be above the Fermi sea  $k > k_F$



**Possible inversion of the momentum sharing :**

$$\langle k_{\text{minority}} \rangle > \langle k_{\text{majority}} \rangle$$



# Protons move faster than neutrons in N>Z nuclei

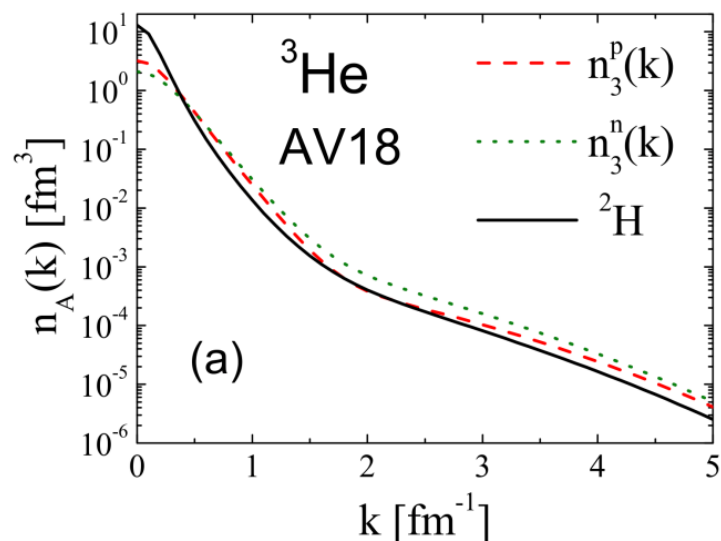
( protons move faster than neutrons in N>Z nuclei )

## Light nuclei A<11

Variational Monte Carlo  
calculations by the  
Argonne group

Wiringa et al.  
phys. Rev. C89, 034305 (2014).

	$\frac{ N-Z }{A}$	$\langle KE \rangle_p$	$\langle KE \rangle_n$	$\langle KE \rangle_{p-n}$
$^8\text{He}$	0.50	30.13	18.60	11.53
$^6\text{He}$	0.33	27.66	19.06	8.60
$^9\text{Li}$	0.33	31.39	24.91	6.48
$^3\text{He}$	0.33	14.71	19.35	-4.64
$^3\text{H}$	0.33	19.61	14.96	4.65
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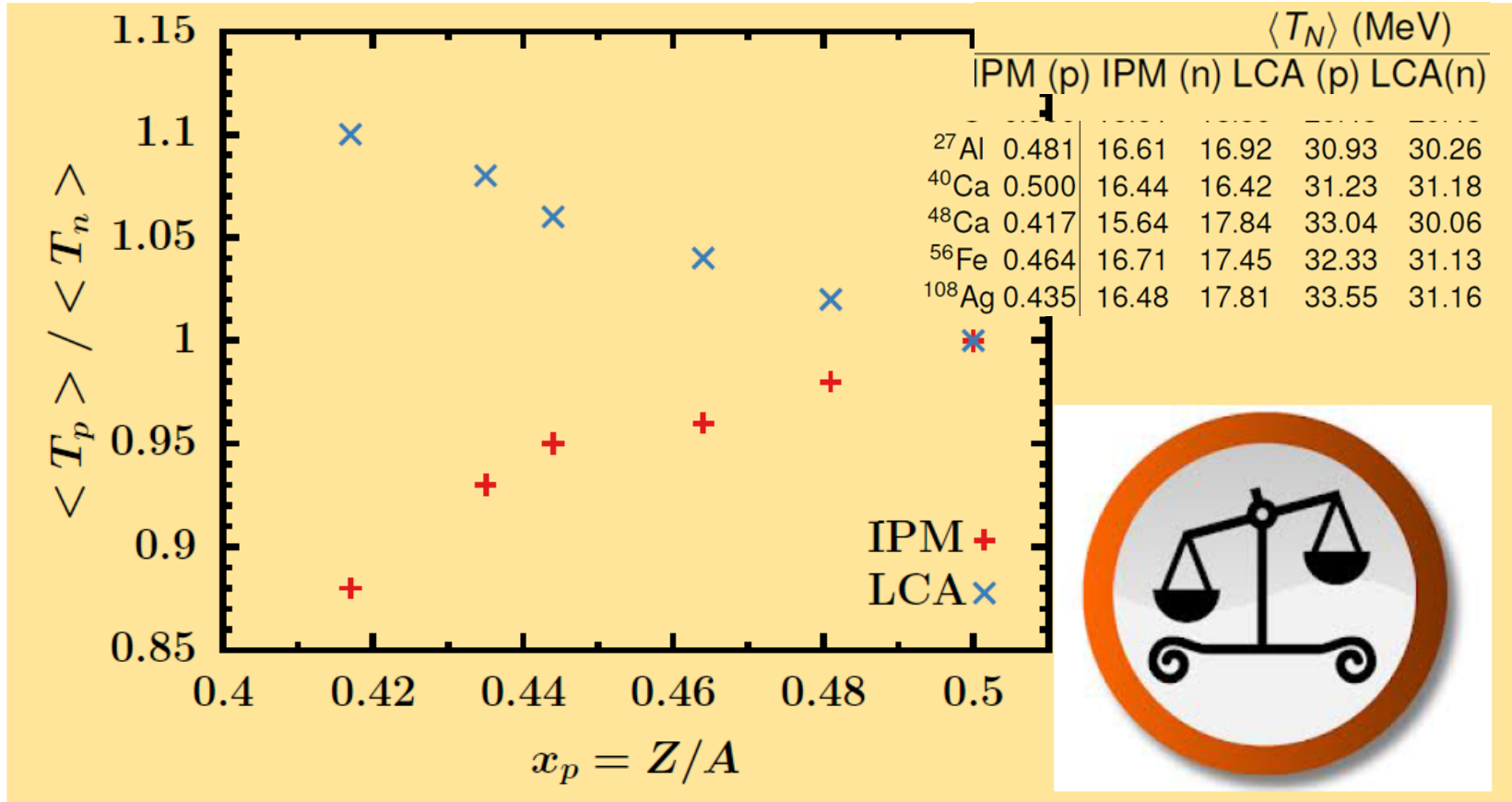


$$\frac{n_n(k > 1)}{n_n(k < 1)} > \frac{n_p(k > 1)}{n_p(k < 1)}$$



# Predictions for $\langle T_p \rangle / \langle T_n \rangle$ ratio

Average kinetic energy per nucleon

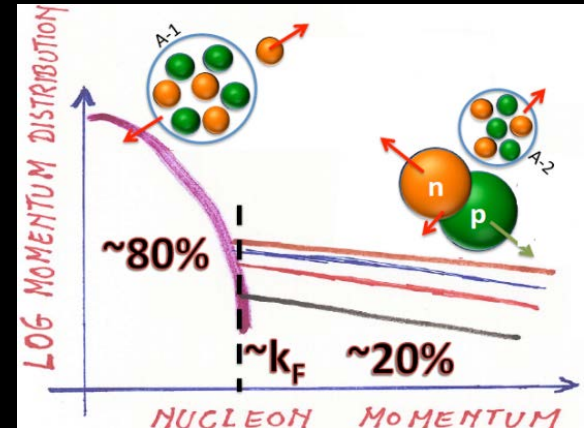


## Nuclei:

Identified triple coincidence SRC pairs  
in: ( $^3\text{He}$ , )  $^4\text{He}$ ,  $^{12}\text{C}$ ,  $^{27}\text{Al}$ ,  $^{56}\text{Fe}$ , and  $^{208}\text{Pb}$

High momentum tail In nuclei  
dominated by SRC pairs

np-SRC dominance

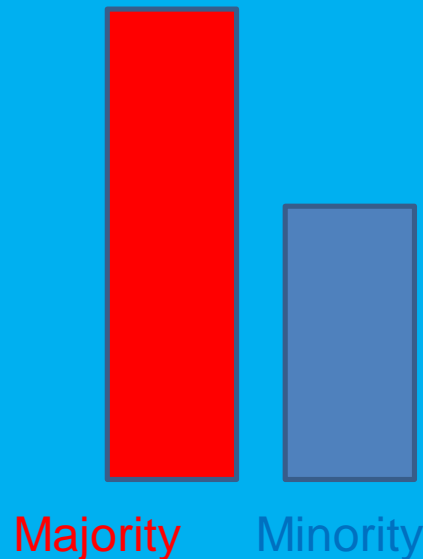


Compact Astronomical Systems ?

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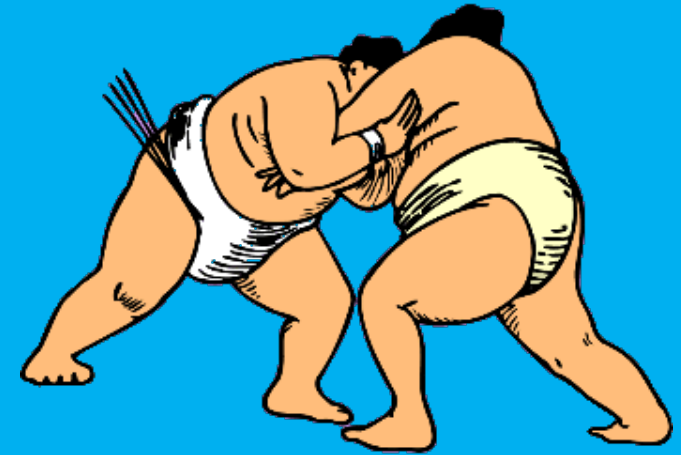
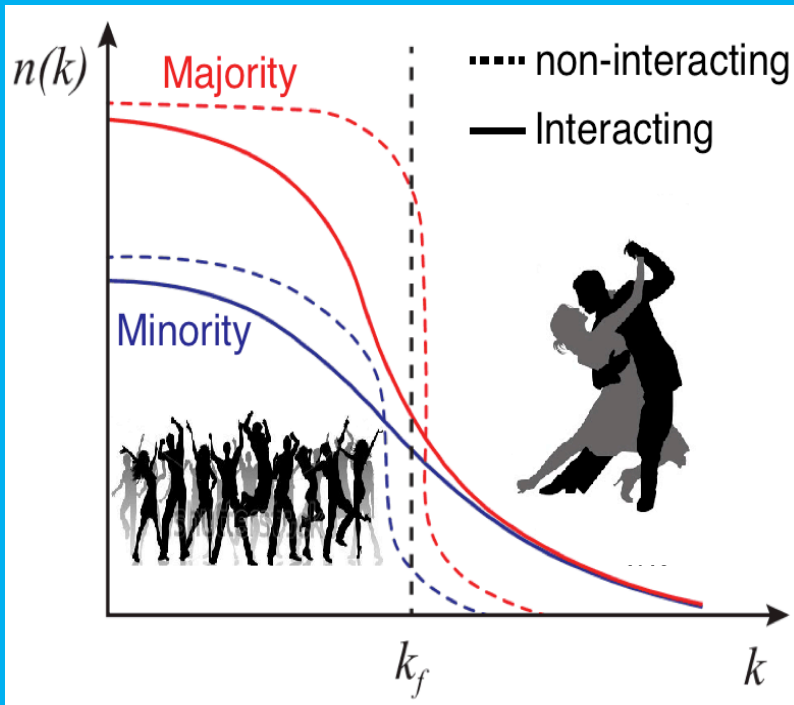
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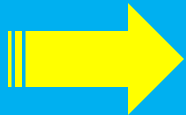
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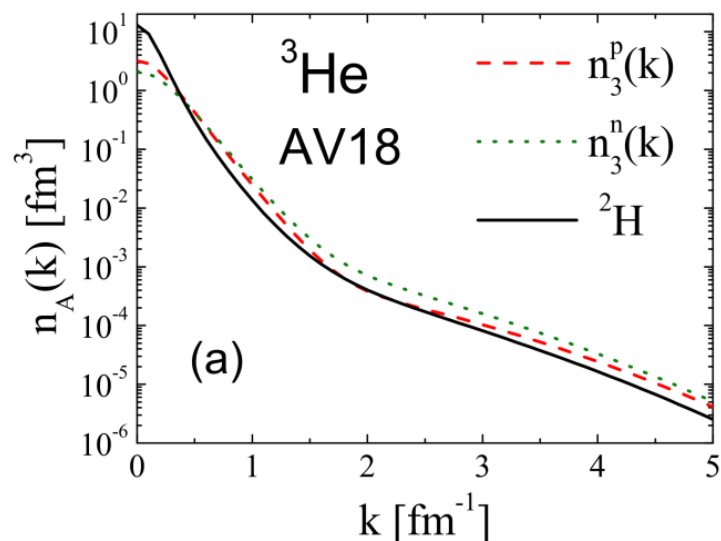
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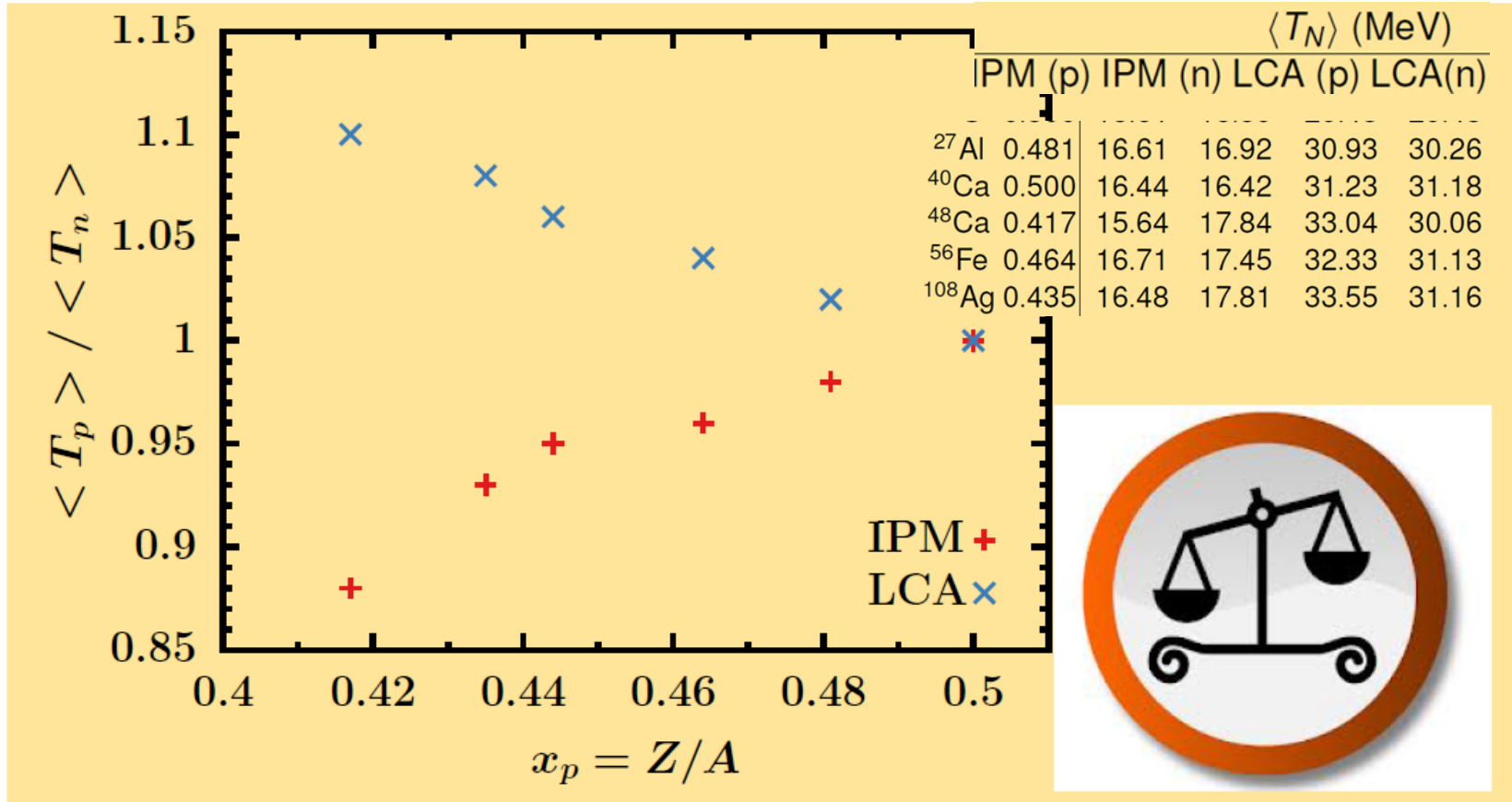


$$\frac{n_n(k > 1)}{n_n(k < 1)} > \frac{n_p(k > 1)}{n_p(k < 1)}$$

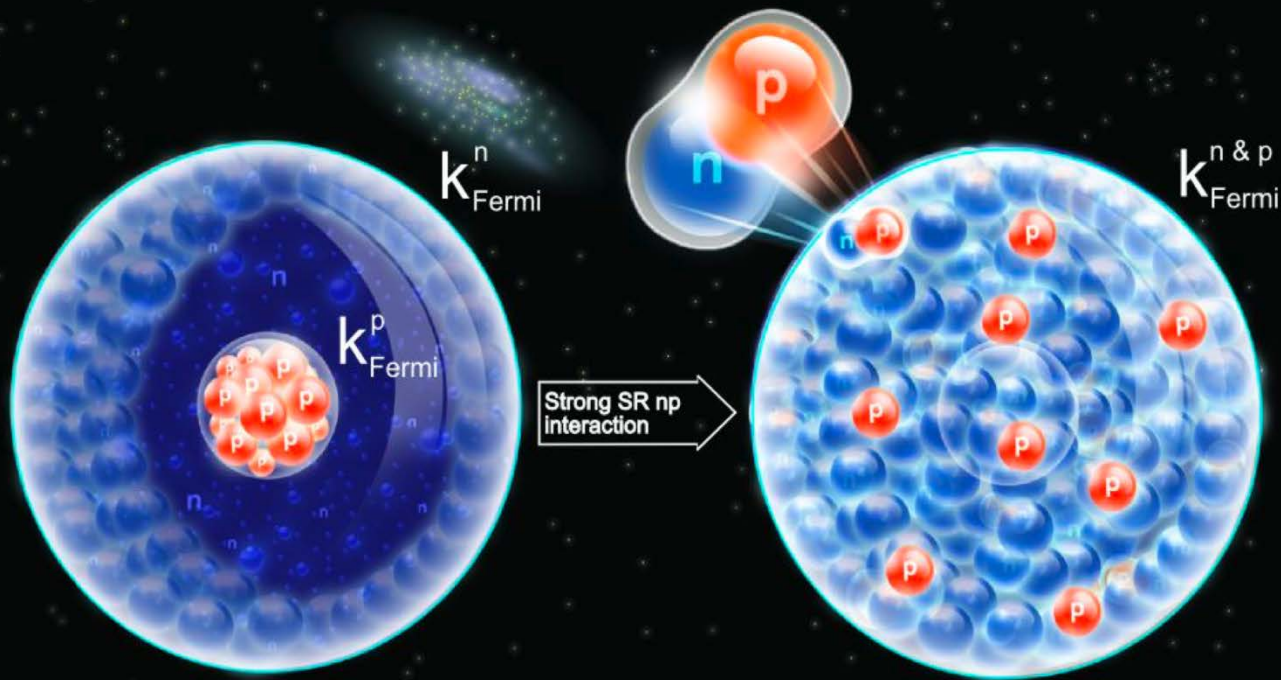


# Predictions for $\langle T_p \rangle / \langle T_n \rangle$ ratio

Average kinetic energy per nucleon



# Implications for Neutron Stars



Adapted from: D.Higinbotham,  
E. Piasetzky, M. Strikman  
CERN Courier 49N1 (2009) 22

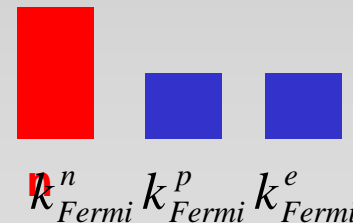
• At the core of neutron stars, most accepted models assume :

~95% neutrons, ~5% protons and ~5% electrons ( $\beta$ -stability).

• Neglecting the np-SRC interactions, one can assume three separate Fermi gases (n p and e).

• strong np interaction

the n-gas heats the p-gas.



See estimates in Frankfurt and Strikman : [Int.J.Mod.Phys.A23:2991-3055,2008.](#)



# SRC in nuclei: implication for neutron stars



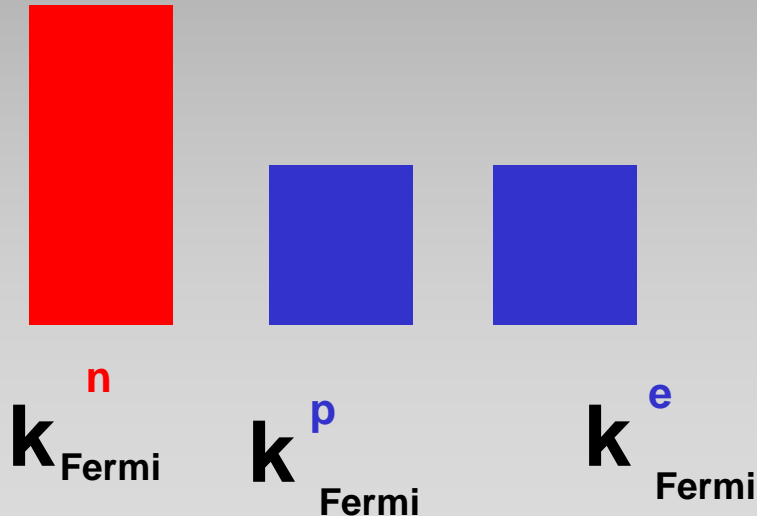
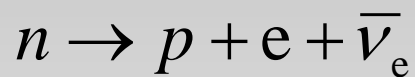
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- Neglecting the np-SRC interactions, one can assume three separate Fermi gases (n p and e).

$$\text{At } T=0 \quad k_{Fermi}^n = k_{Fermi}^p + k_{Fermi}^e \quad k_{Fermi}^p = k_{Fermi}^e = \left(\frac{N_p}{N_n}\right)^{1/3} k_{Fermi}^n$$

$$\text{For } \rho = 5\rho_0, \quad k_{Fermi}^n \approx 500 \text{ MeV}/c, \quad k_{Fermi}^p = k_{Fermi}^e \approx 250 \text{ MeV}/c$$

Pauli blocking prevent  
direct n decay



Strong SR np  
interaction

# SRC in nuclei: implication for neutron stars

Strong SR np  
interaction



**At  $T=0$**

**Holes in the n p e Fermi seas**

**Create (n-p-e) neutral SRC**

**Remove Pauli Blocking of the direct n decay**

**Cause instability of the neutron star**

**At  $T \neq 0$**

**Faster neutrino cooling**

**Short life time of hyperon stars**

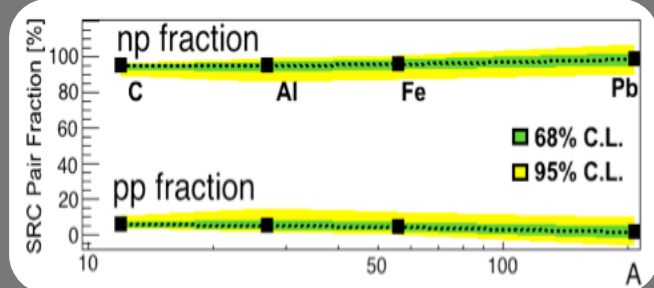
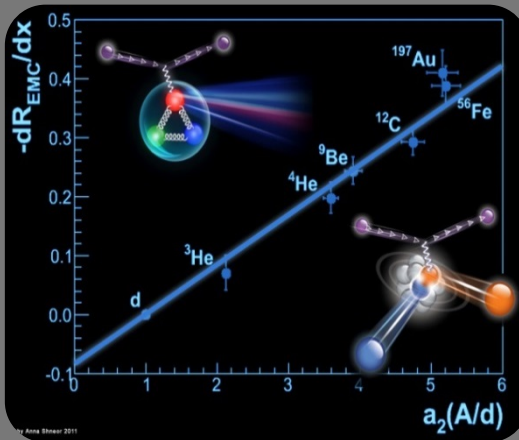


TEL AVIV UNIVERSITY

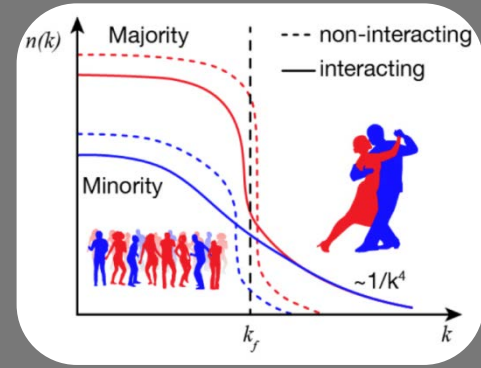
See estimates in Frankfurt and Strikman [rXiv:0806.0997](https://arxiv.org/abs/0806.0997)

Also: [Int.J.Mod.Phys.A23:2991-3055,2008.](https://arxiv.org/abs/0806.4412) [arXiv:0806.4412](https://arxiv.org/abs/0806.4412)

# Summary – relevant of Correlations

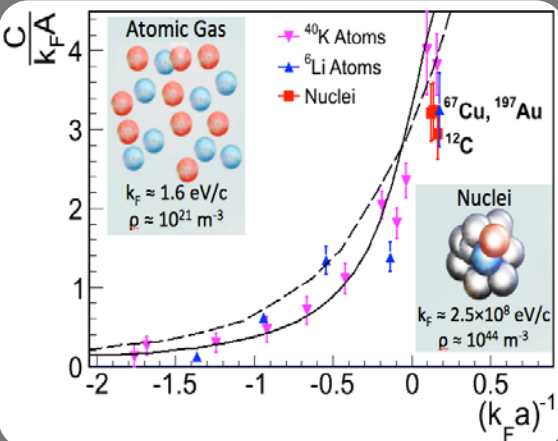


## Nuclear

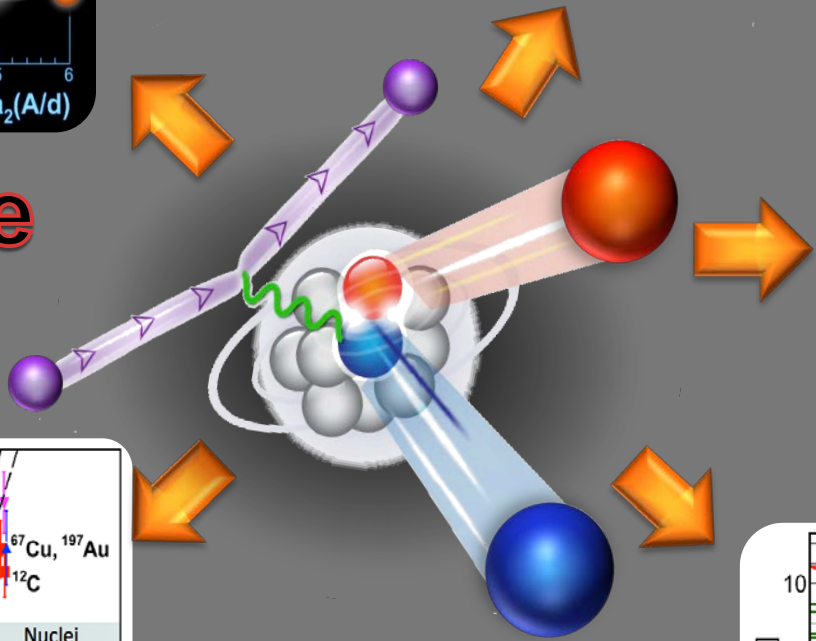


## Particle

## Atomic



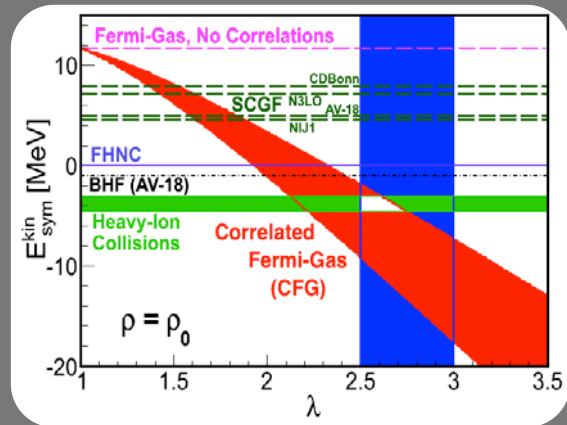
Contact term



## Astro Symmetry energy

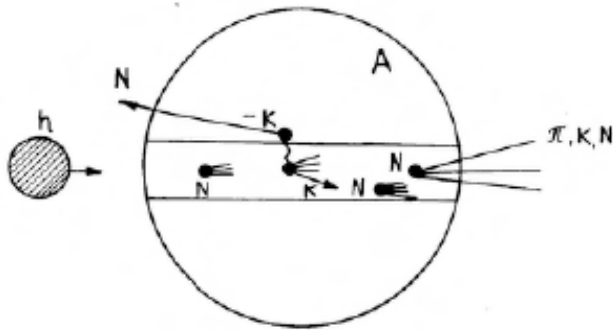
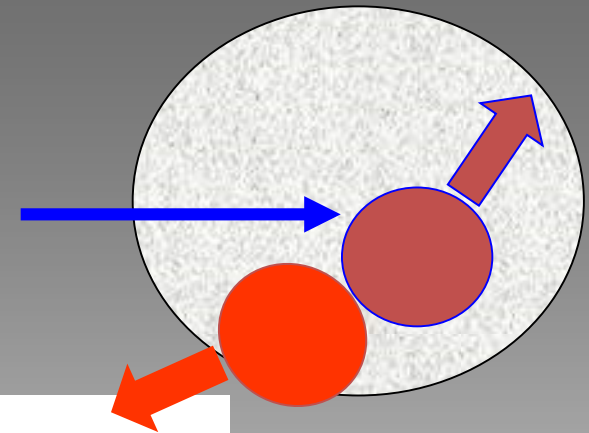


3N-SRC



The story of studying SRC in nuclei using high energy probes **started here** with the measurements of Fast Backward Production at ITEP Moscow ( $p, \pi$ ) and YerPhi (real and virtual photons).

The universality of the fast backward emitted spectrum led Strikman Frankfurt to postulate that it is due to SRC



Production of a fast backward nucleon in the hadron - nucleus scattering

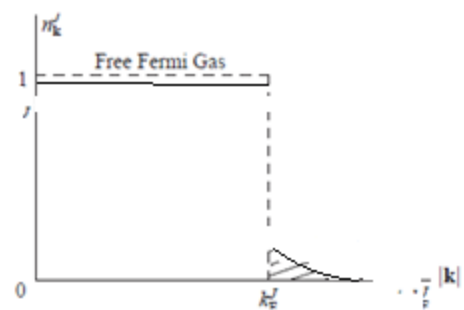
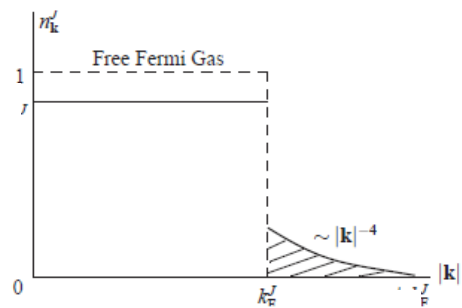
16

**Published:** *Physics of Atomic Nuclei*, Vol. 61, No. 2, 1998, pp. 207-213.

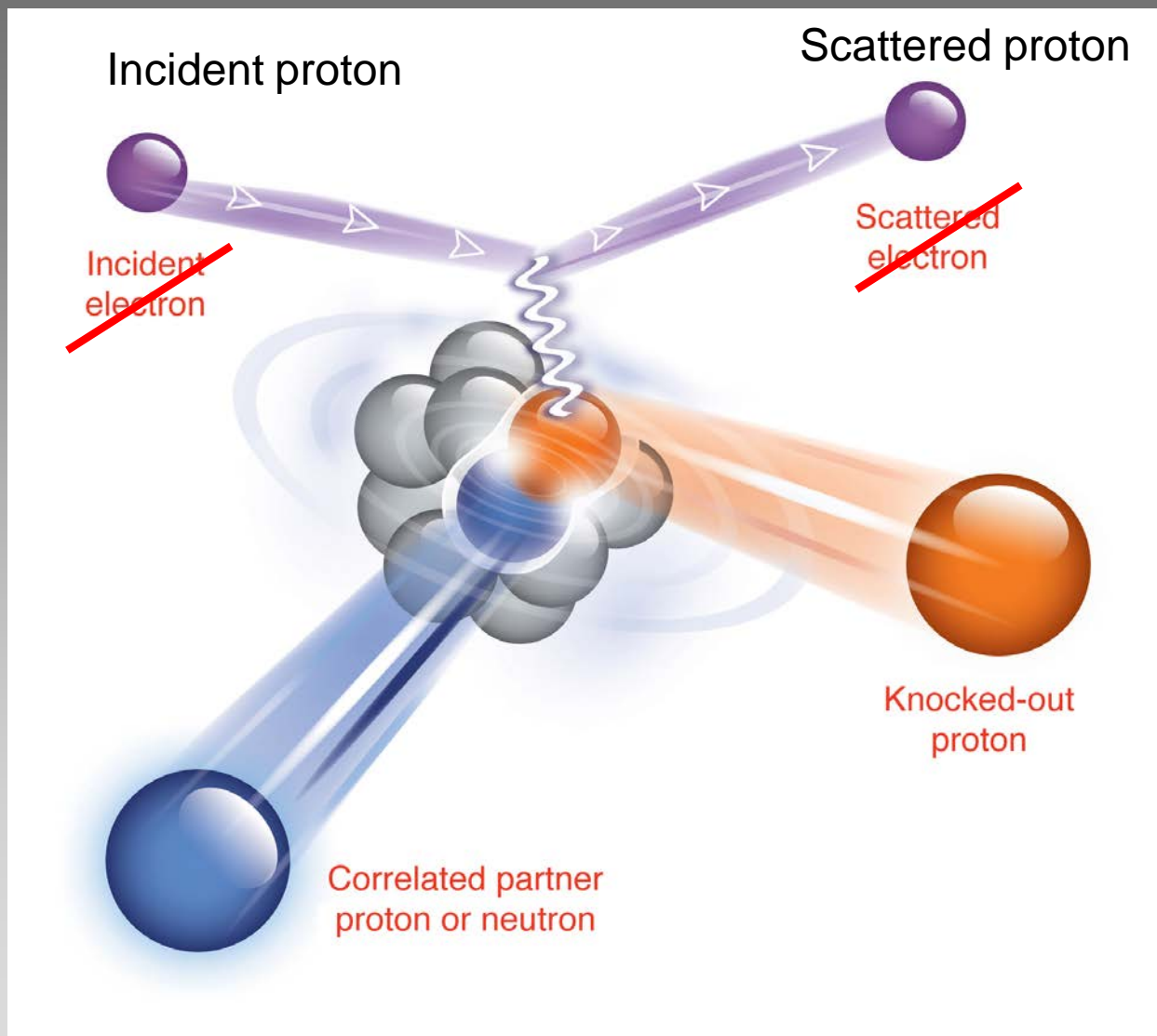
**Emission of Cumulative Protons in the Reaction  $^{12}\text{C}(e, e'p)$**

K. V. Alanakyan, M. J. Amaryan, G. A. Asryan, R. A. Demirchyan, K. Sh. Egiyan, M. S. Ohanjanyan, M. M. Sargsyan, S. G. Stepanyan, and Yu. G. Sharabyan

*Yerevan Physics Institute, ul. Brat'ev Alikhanian 2, Yerevan, 375036 Armenia*



# First Triple coincidence $^{12}\text{C}$ (p, p p n) measurements at EVA / BNL



Complementary to JLab study with electrons