



清华大学
Tsinghua University

A MWDC array for the external target experiment at HIRFL-CSR

易贻 Yi Han

Department of Physics
Tsinghua University



CONTENTS

1. Background
2. Chamber Structure
3. Pre-Amplifier
4. DAQ
5. Digital Signal Processing
6. Track Reconstruction
7. Beam Test
8. Data Analysis
9. Summary

Structure of MWDC

planar structure:

wires angle: 0° , $\pm 30^\circ$

sensitive area: 320mm*420mm

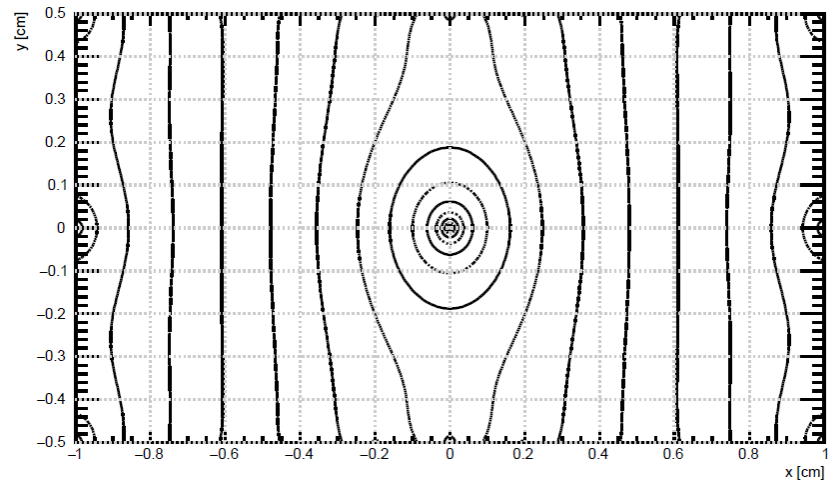
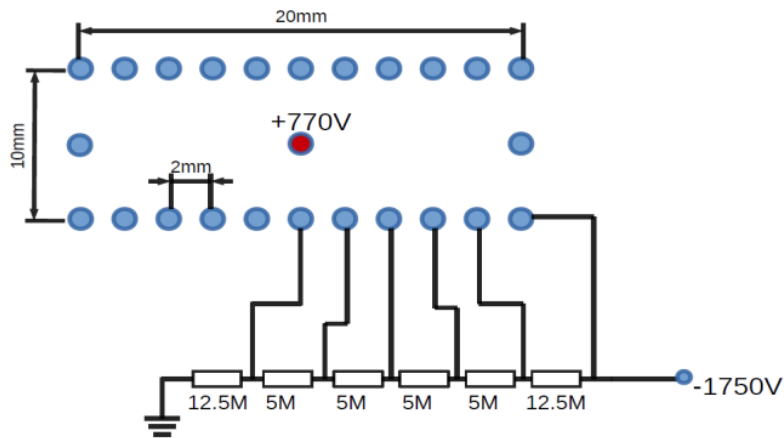
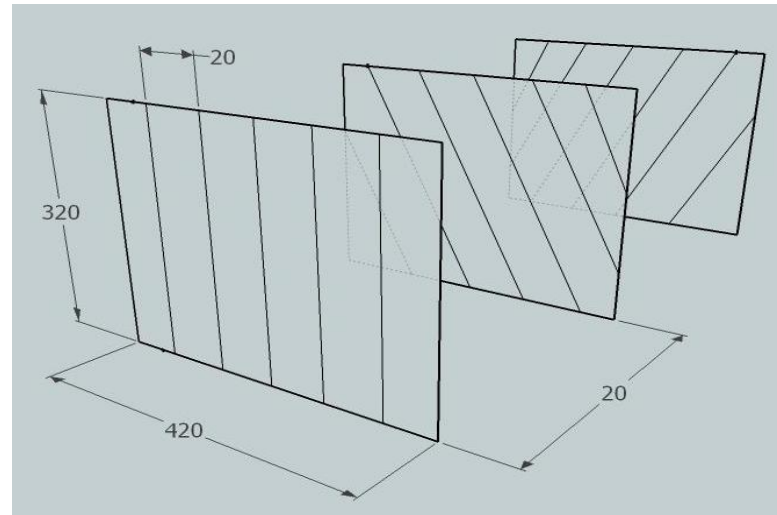
distance between anode wires: 20mm

distance between field wires : 20mm

anode wires: 20 μ m gold-plated tungsten wire

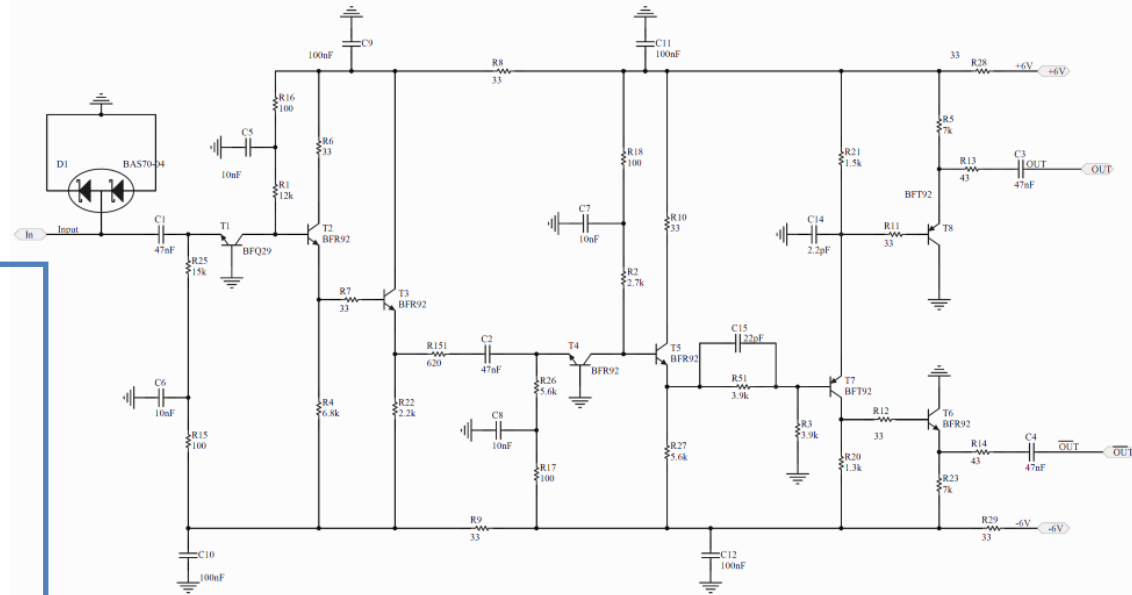
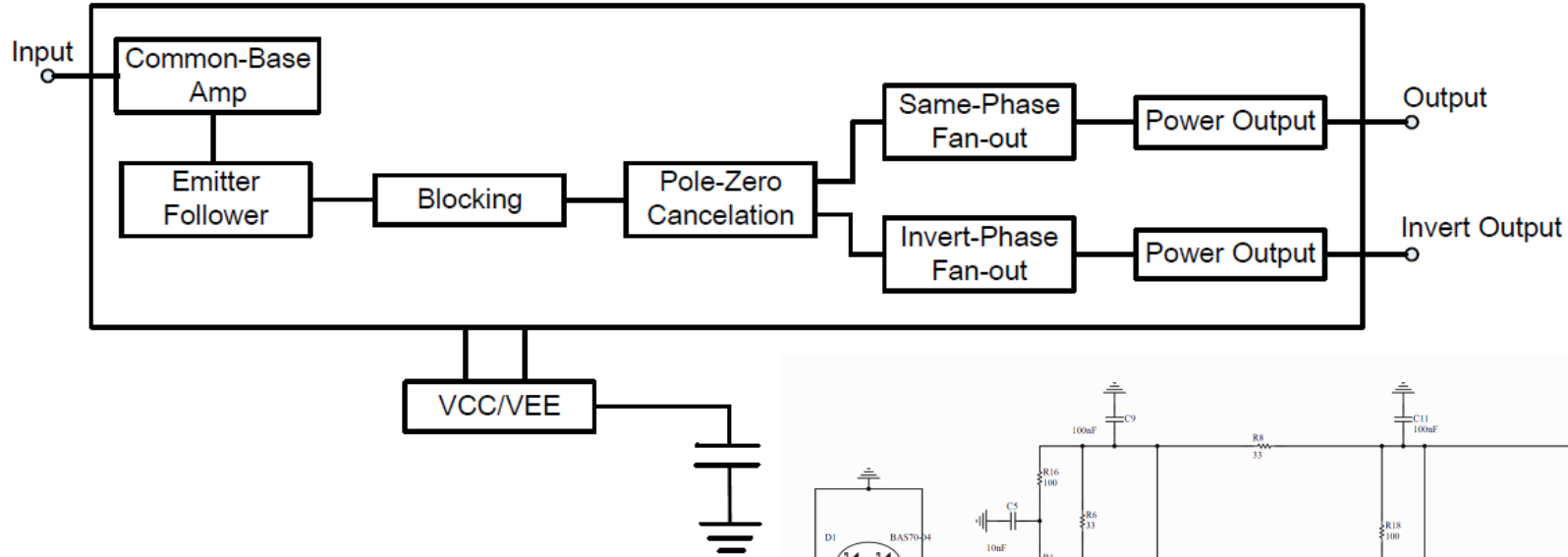
field wires: 100 μ m Be-plated copper wire

working gas: Ar/CO₂ = 85/15



Equipotential lines distribution simulated by Garfield ++.

Pre-Amplifier

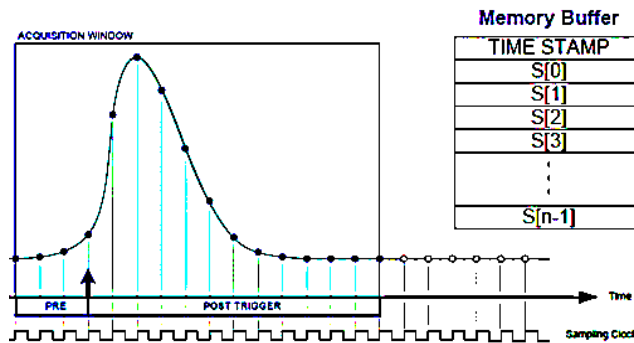
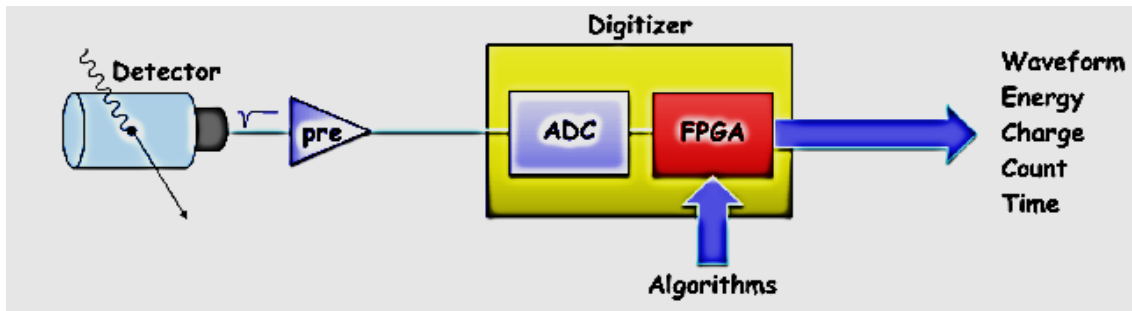


Design of Pre-Amplifier:

- 1) low power dissipation
- 2) high gain and wide bandwidth
- 3) high time resolution
- 4) high energy resolution
- 5) high signal noise ratio

Flash-ADC Data Acquisition system (DAQ)

Sampling the whole wave forms of detectors to get the time and energy information and analysis events with complex wave forms.



DAQ architecture

CAEN-V1720 module

ADC: 12bit

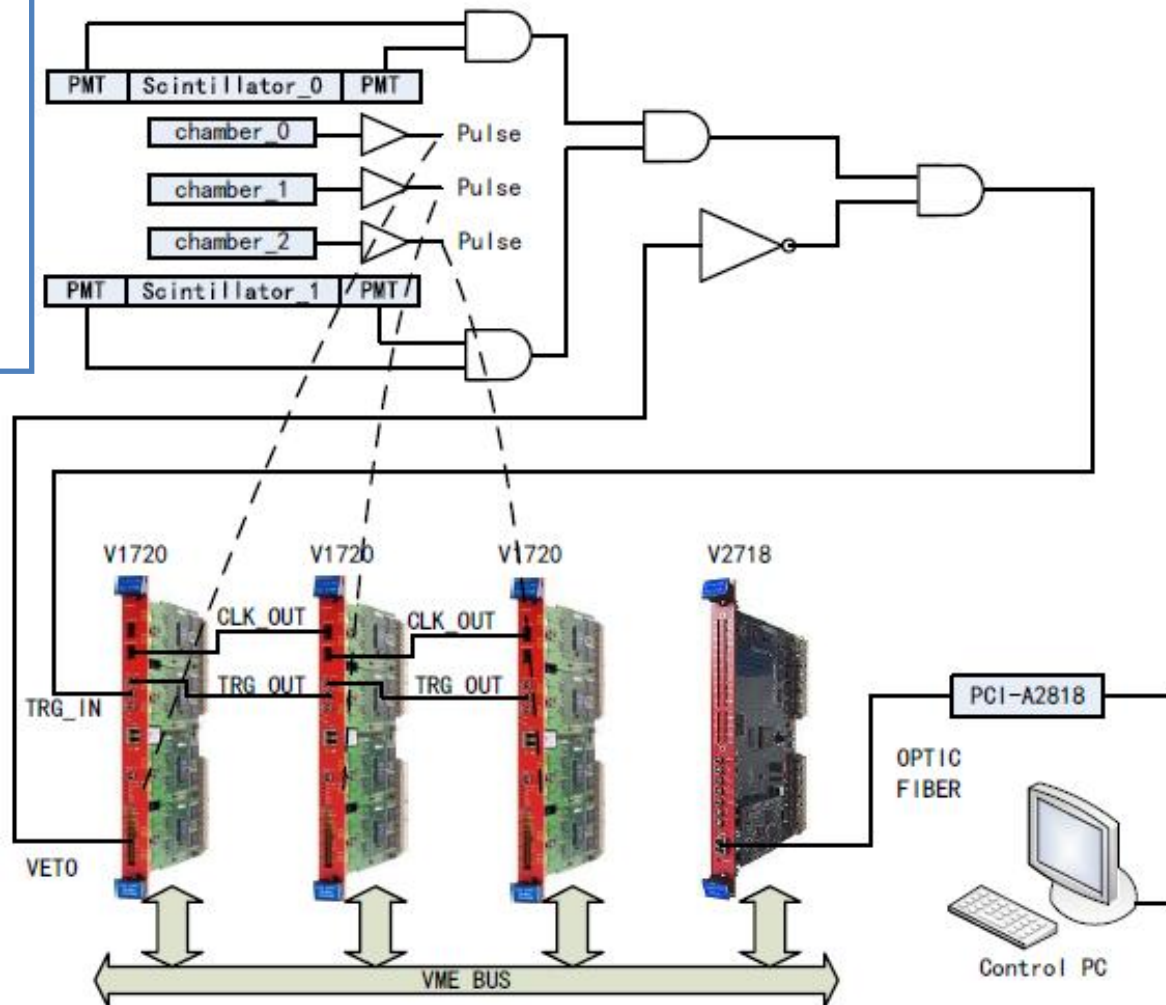
Dynamic range: 2Vpp

DC offset: $\pm 1V$

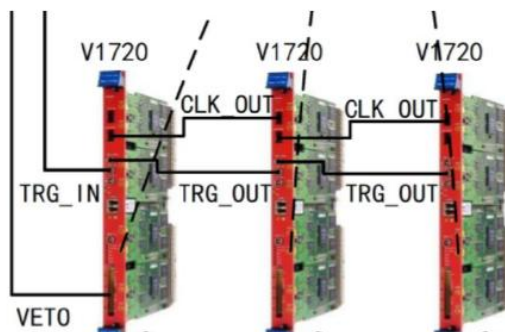
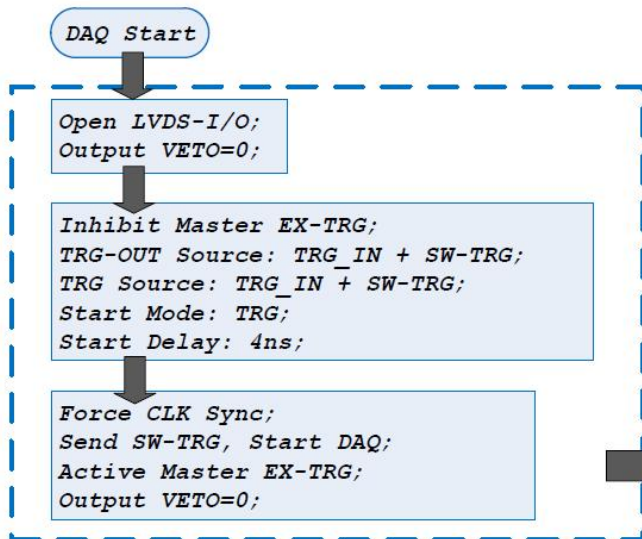
Sampling frequency: 250MHz

Data transmission: 80MB/s

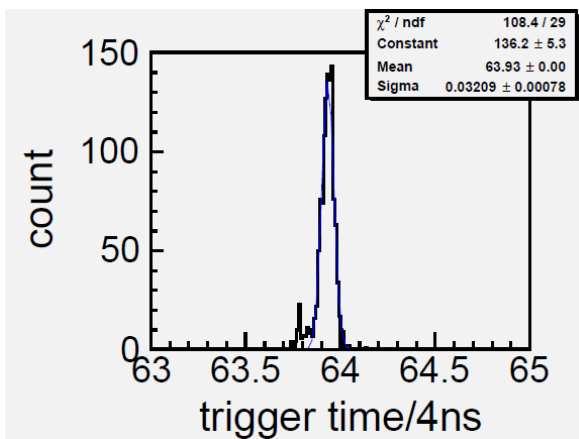
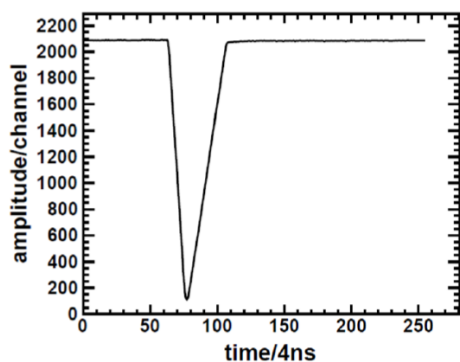
Clock signal is generated by the master and transmitted to the slaves. Trigger signal is the coincidence of the four PMTs and transmitted to the slaves through the daisy chain.



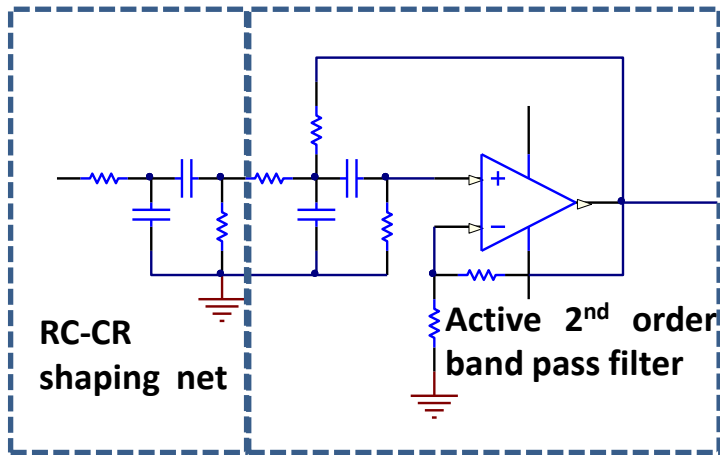
DAQ clock synchronization



Test the time walking between different boards using a test pulses. The sigma of the time walking distribution is 128ps.



Digital filter algorithm



Derive the digital filter algorithm according to the transfer function:

- 1) RC-CR shaping net;
- 2) digital active 2nd band pass filter.

Digital RC-CR shaping net recursive algorithm:

$$y(k) = \frac{A\tau_2}{\tau_2 - \tau_1} \left[\frac{\tau_1}{T} (1 - e^{-T/\tau_1}) y_1(k) - \frac{\tau_2}{T} (1 - e^{-T/\tau_2}) y_2(k) \right]$$

$$y_i(k) = \frac{T}{\tau_i} x(k) + e^{-T/\tau_i} y_i(k-1), \quad y_i(0) = \frac{T}{\tau_i} \cdot \frac{x(0)}{1 - e^{-T/\tau_i}}$$

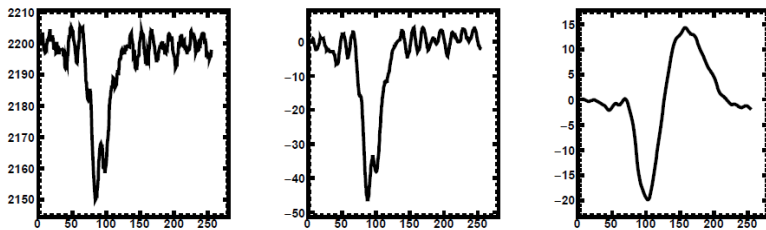
Digital band pass filter:

- 1) transfer function of analog filter:

$$H(s) = \frac{As/\omega}{1 + \frac{s/\omega}{Q} + (s/\omega)^2}$$

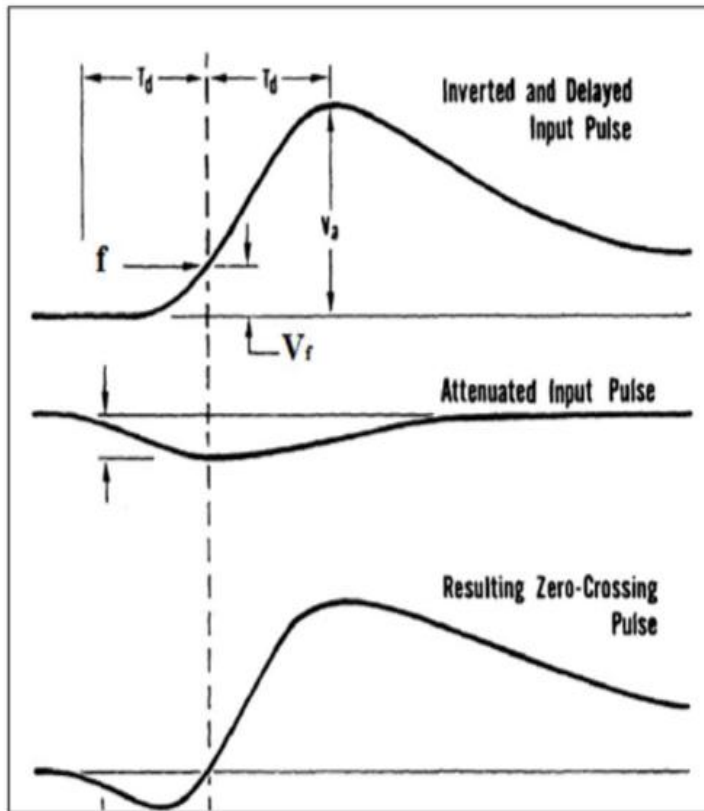
- 2) transfer function of digital filter:

$$H(z) = A\omega T \frac{1 - e^{-\alpha\omega T} (\cos\beta\omega T + \frac{\alpha}{\beta} \sin\beta\omega T) z^{-1}}{1 - 2e^{-\alpha\omega T} (\cos\beta\omega T) z^{-1} + e^{-2\alpha\omega T} z^{-2}}$$



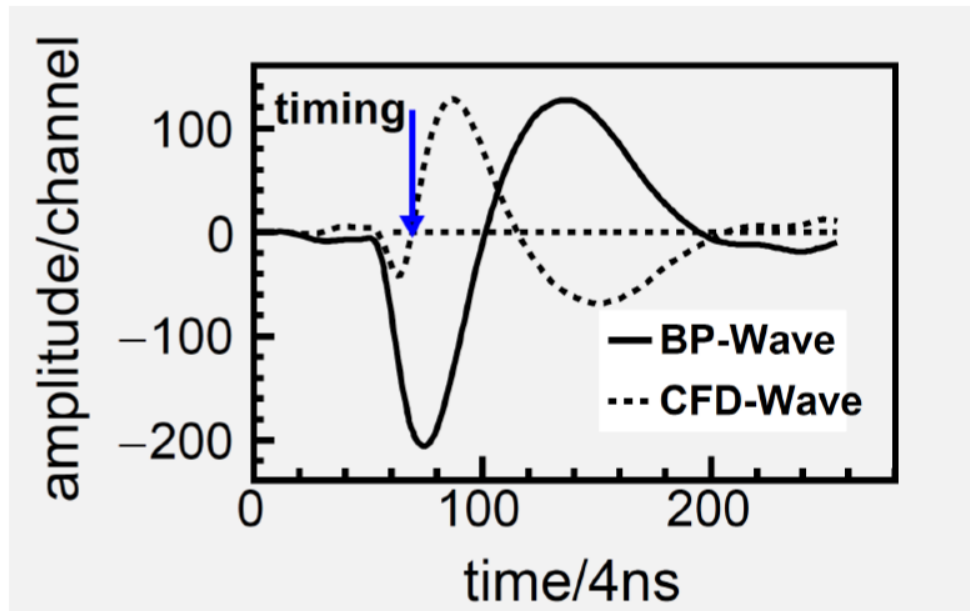
Deduce the energy and time information with the filter output waveform.

Digital CFD

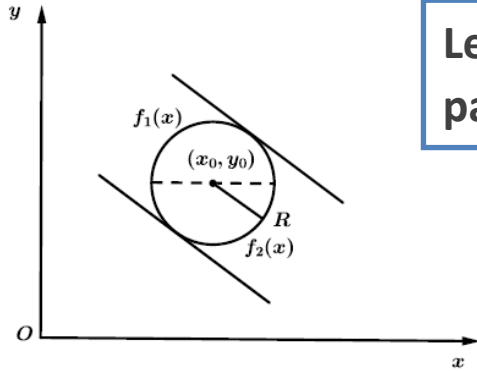


The CFD waveform is the sum of the delayed waveform and the inverted and attenuated waveform:

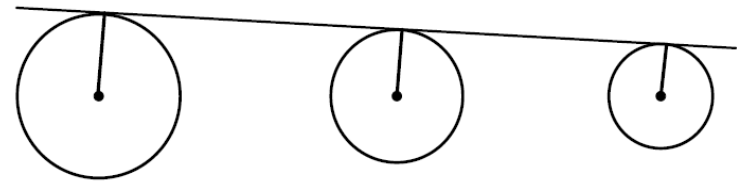
$$y(k) = x(k - d) - \gamma x(k)$$



Track finding algorithm-Legendre transformation



Legendre transformation of the upper-half and lower-half part of a circle.



$$f(x) = \begin{cases} f_1(x) = y_0 + \sqrt{R^2 - (x - x_0)^2} \\ f_2(x) = y_0 - \sqrt{R^2 - (x - x_0)^2} \end{cases}$$

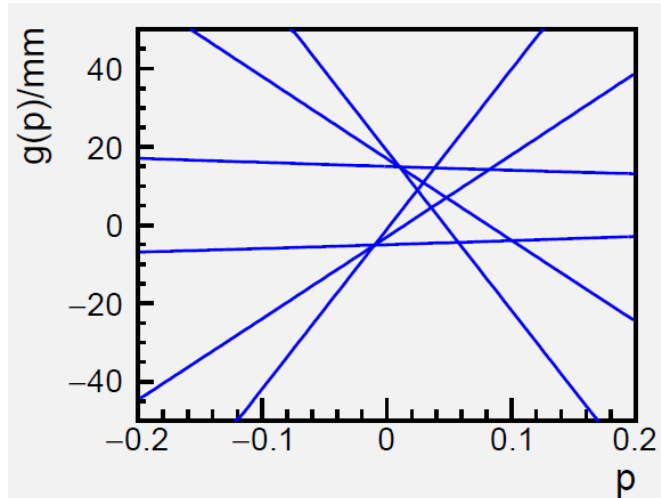
$$g_1(p) = f_1(x_0) - px_0$$

$$= y_0 - px_0 + \frac{R}{\sqrt{p^2 + 1}} + \frac{p^2 R}{\sqrt{p^2 + 1}}$$

$$= y_0 - px_0 + R\sqrt{p^2 + 1}$$

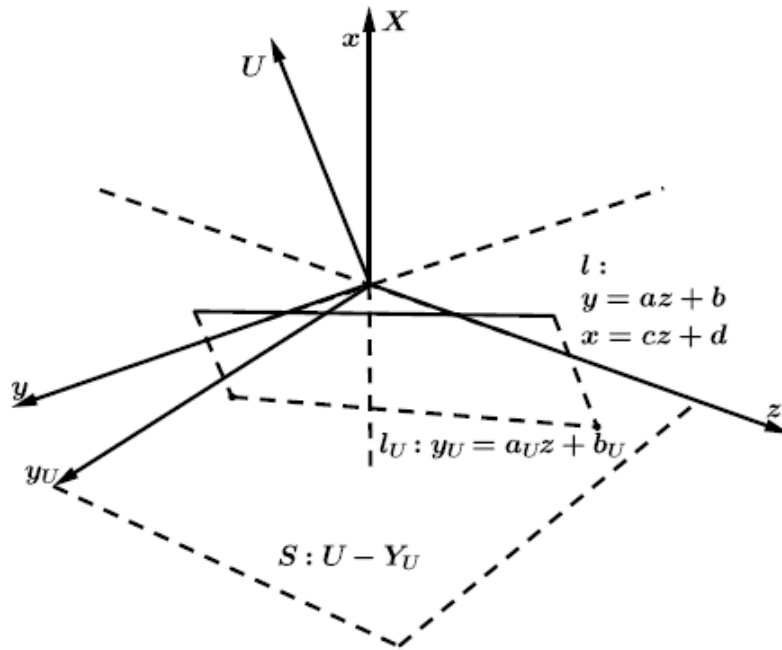
$$g_2(p) = f_2(x_0) - px_0$$

$$= y_0 - px_0 - R\sqrt{p^2 + 1}$$



Find the common point in the Legendre space to get the common tangent line in the x-y space.

Analytical solution for track reconstruction



Use Least Square method to reconstruct the track in the projection space.

$$\chi^2 = \sum_i \left(r_i - \frac{k_i z_i + b_i - y_i}{\sqrt{1 + k_i^2}} \right)^2$$

$$\chi^2 = (R - \lambda - Aq)^T (R - \lambda - Aq)$$

$$q = (A^T A)^{-1} A^T (R - \lambda)$$

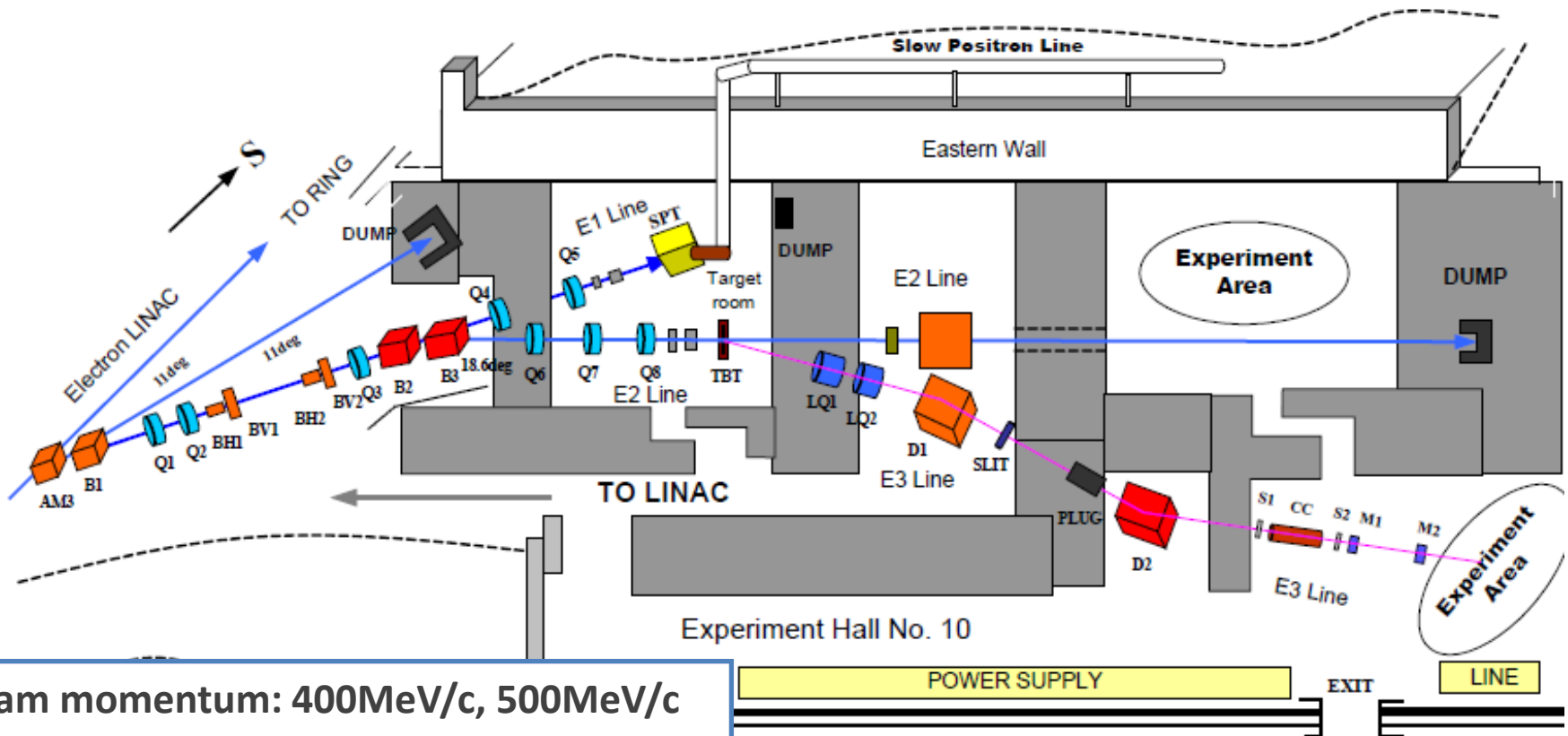
$$\begin{cases} y = az + b \\ x = cz + d \end{cases} \quad \begin{cases} d_i = \frac{k_i z_i + b_i - y_i}{\sqrt{1 + k_i^2}} \\ k_i = a \sin \theta_i + c \sin \theta_i \\ b_i = b \cos \theta_i + d \sin \theta_i \end{cases}$$

$$y_i = (a \cos \theta_i + c \sin \theta_i) z + (b \cos \theta_i + d \sin \theta_i)$$



Beam test

Beam test is done at the E3 Test Line at IHEP. The beam is guided to the test hall through the E3 line.



Beam momentum: 400MeV/c, 500MeV/c
Particle: proton, pion
Count rate: ~100/min

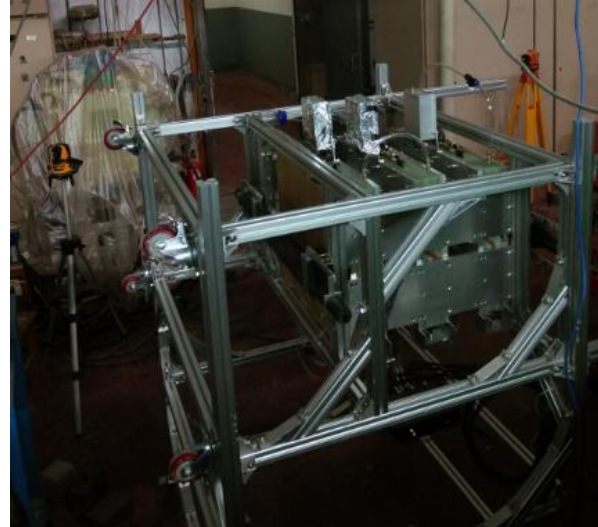
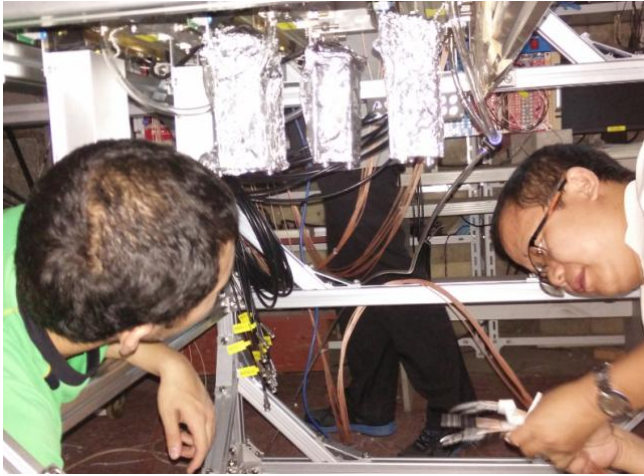
POWER SUPPLY

EXIT

LINE

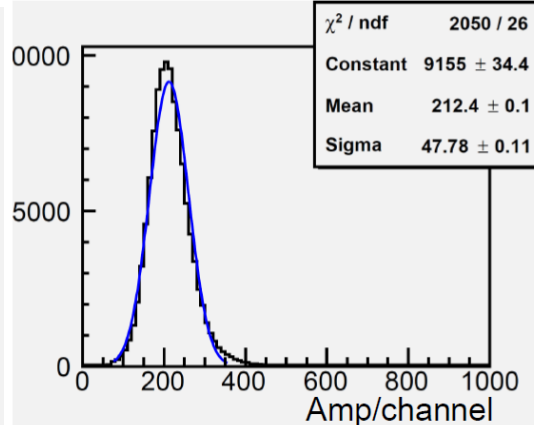
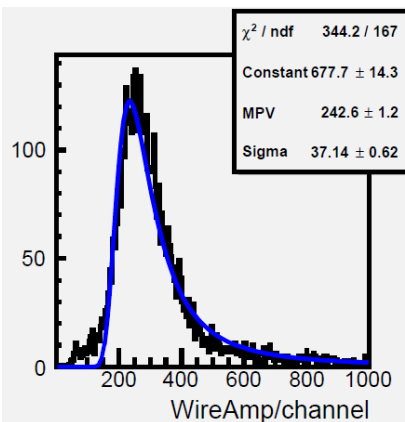
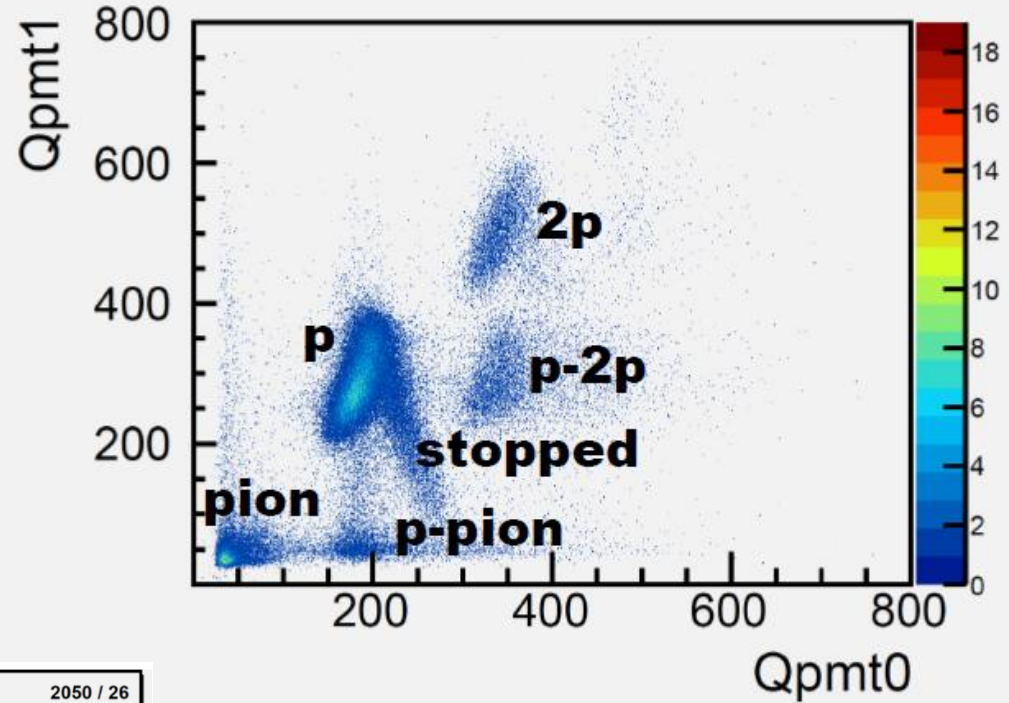
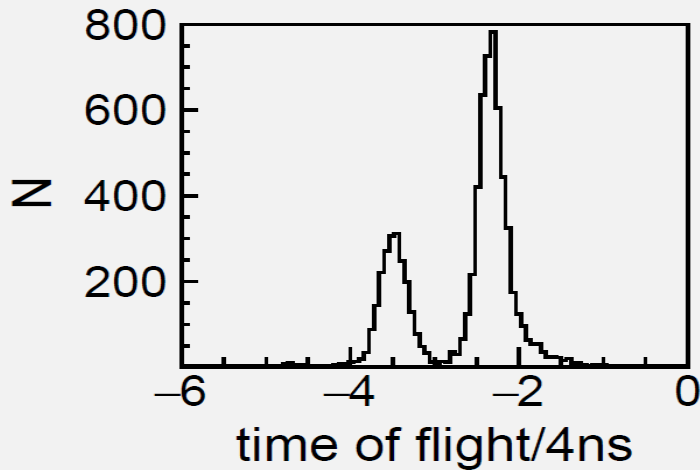
Beam test

Working photos



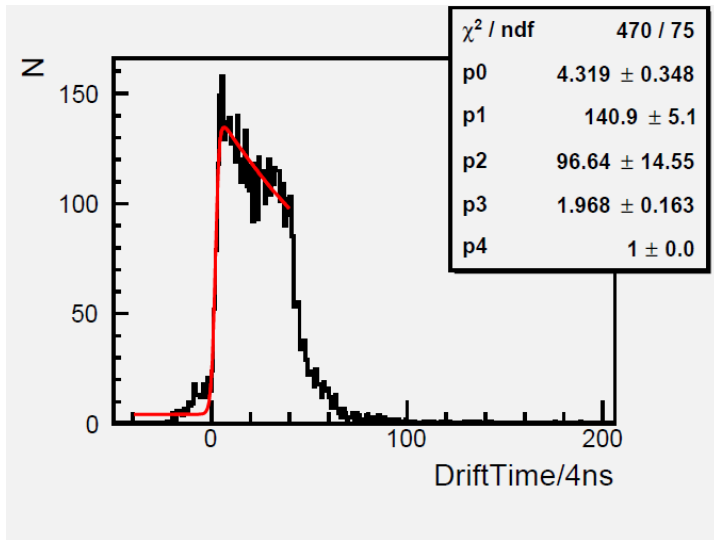
Data analysis

TOF has a time resolution of 600ps.
Select single proton event to analysis.



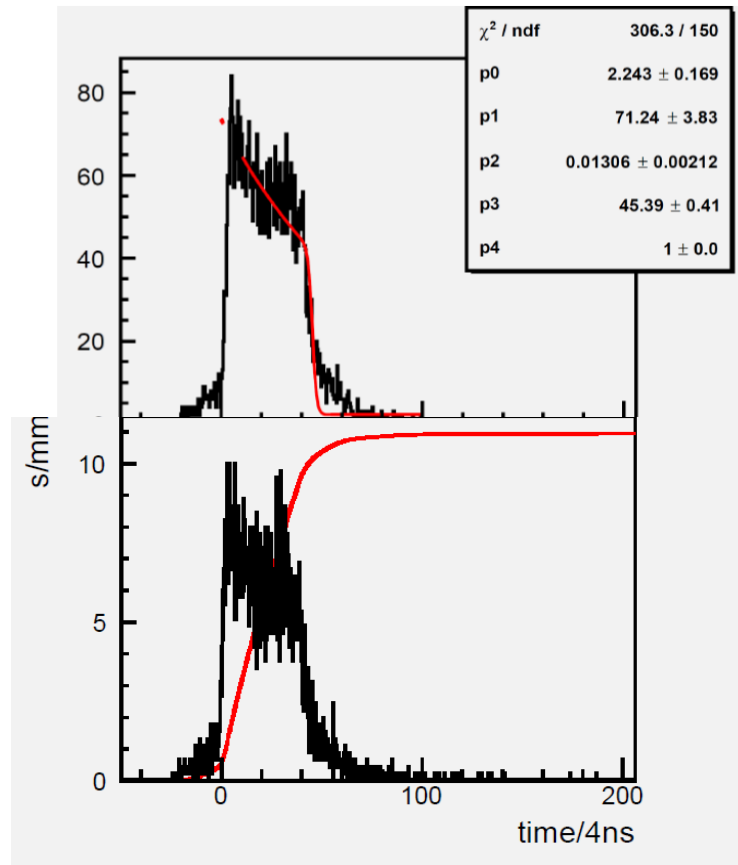
Use truncated mean method to get the energy resolution of the chamber. The relative energy resolution is 22.5%.

Fit zero point of drift time distribution and get the space-time relation



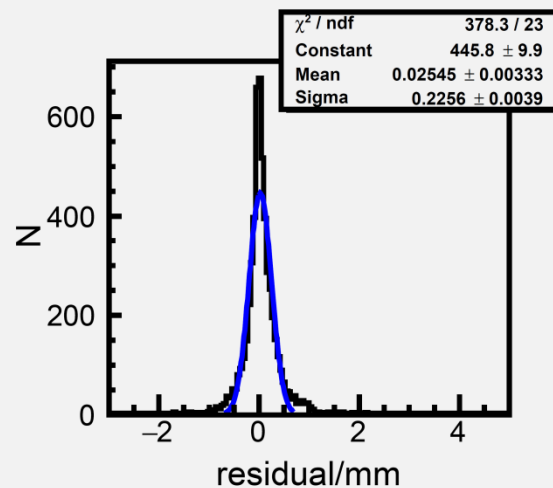
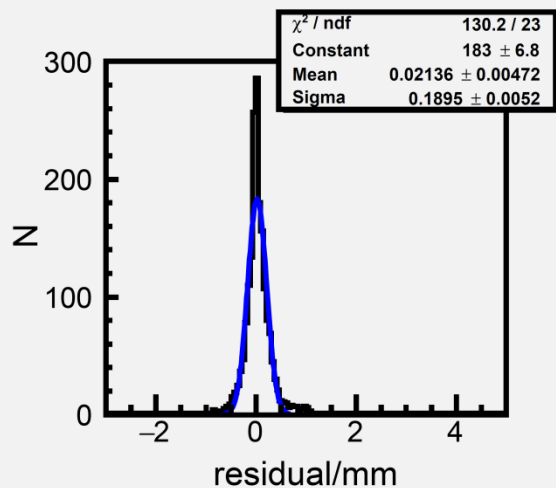
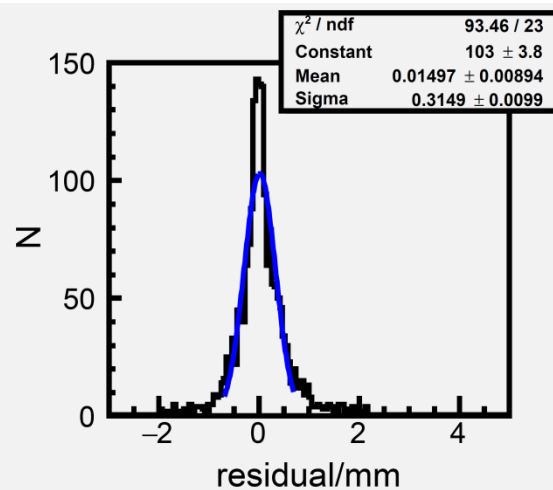
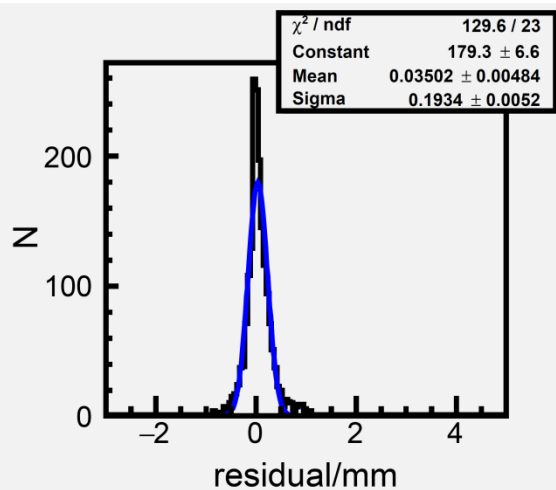
Function that used for fitting:

$$N = B + A \frac{e^{-t/\tau_1}}{1 + e^{(t-T_0)/\tau_2}}$$



Get the space-time relation by integral the drift time distribution.

Low dimension space resolution

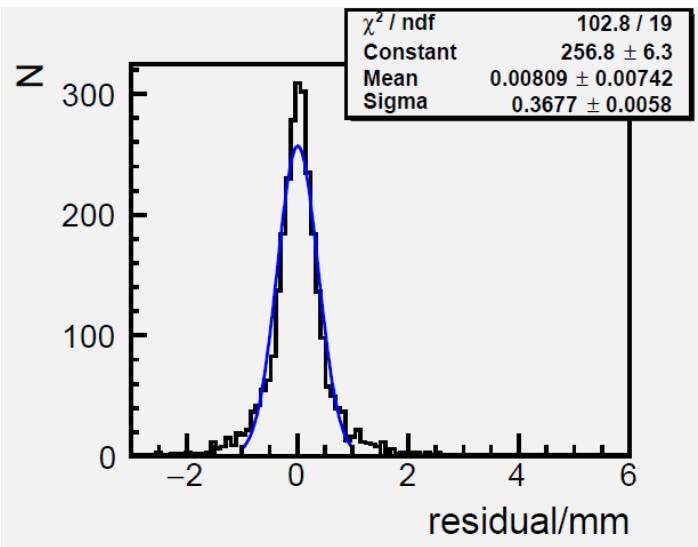


Do track reconstruction with data of wires in the one direction.

The low dimension resolution is $226\mu\text{m}$.

Three dimension space resolution

Do three dimension track reconstruction. The resolution is $368\mu\text{m}$.



$$\sigma^2 = \sigma_{TOF}^2 + \sigma_{STR}^2 + \sigma_{T_0}^2 + \sigma_{Timing}^2 + \sigma_I^2 + \sigma_{Mech}^2 + \sigma_{DAQ}^2$$

System errors:

TOF error σ_{TOF} : $30\mu\text{m}$

STP error σ_{STR} : $100\mu\text{m}$

DAQ clock error σ_{DAQ} : $1.6\mu\text{m}$

T0 error σ_{T_0} : $10\mu\text{m}$

initial resolution σ_{TOF} : $100\mu\text{m}$

mechanical error σ_{Mech} : $335\mu\text{m}$

Timing error: $50\mu\text{m}$

■ summary

- A MWDC array is built and tested.
- The Pre-Amplifier is designed.
- The DAQ is developed.
- Digital filter and track reconstruction algorithm is developed.
- The current space resolution is $368\mu\text{m}$.



清华大学
Tsinghua University

Thank you !

