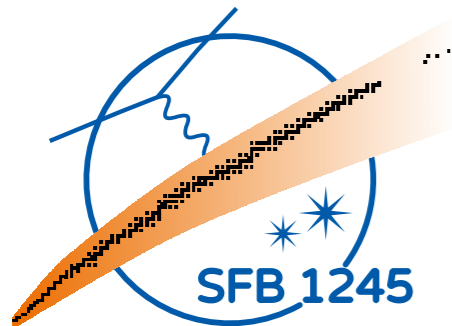


Symmetry energy, neutron skin and neutron star radius constraints from chiral EFT interactions

Kai Hebeler

Beijing, June 15, 2016



TECHNISCHE
UNIVERSITÄT
DARMSTADT

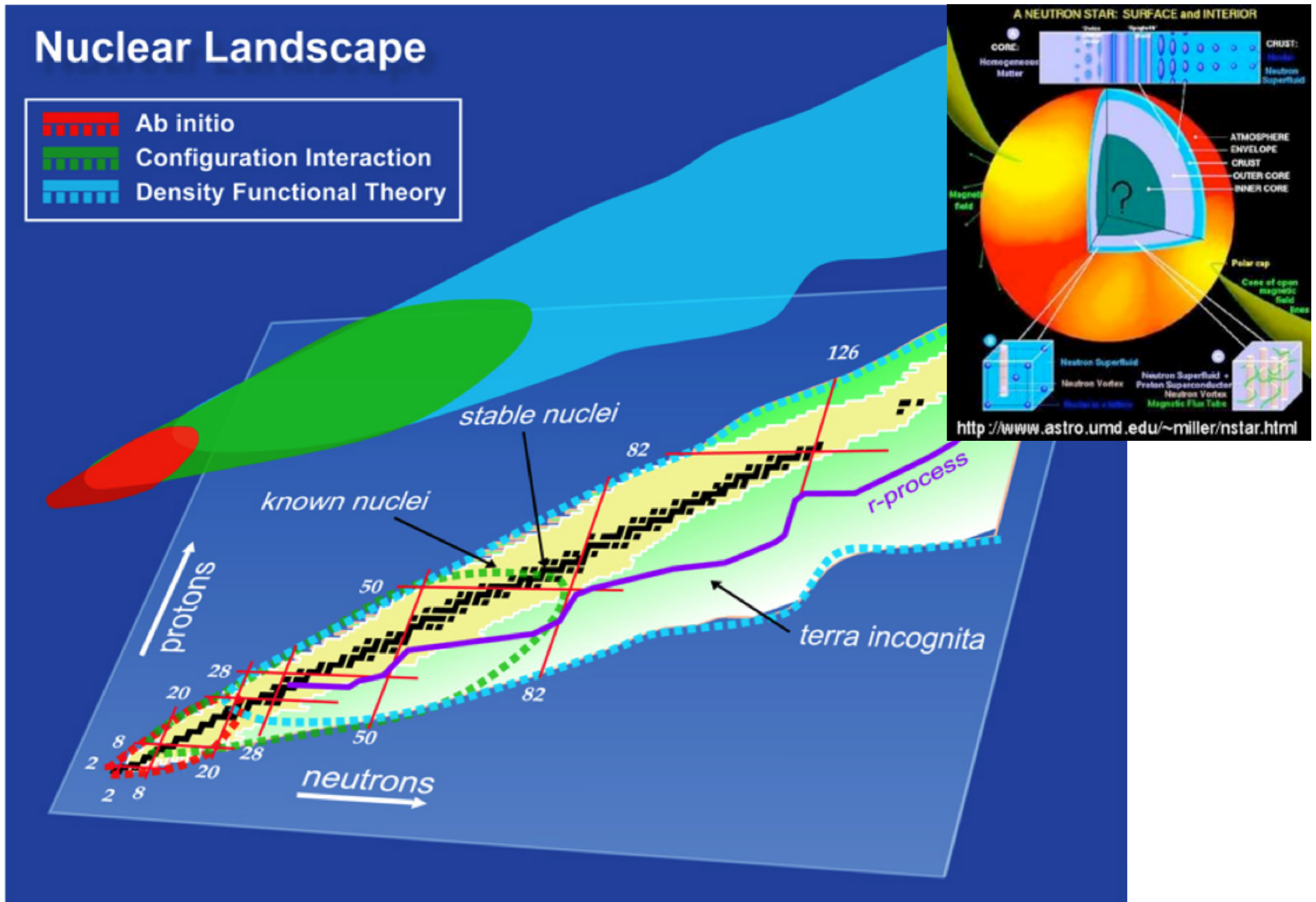


European Research Council

Established by the European Commission

6th international symposium on Nuclear Symmetry Energy

The theoretical nuclear landscape several years ago...



Ab initio nuclear structure theory

**nuclear structure and
reaction observables**



Quantum Chromodynamics

Ab initio nuclear structure theory

**nuclear structure and
reaction observables**

Lattice QCD

- requires extreme amounts of computational resources
- currently limited to 1- or 2-nucleon systems
- current accuracy insufficient for precision nuclear structure

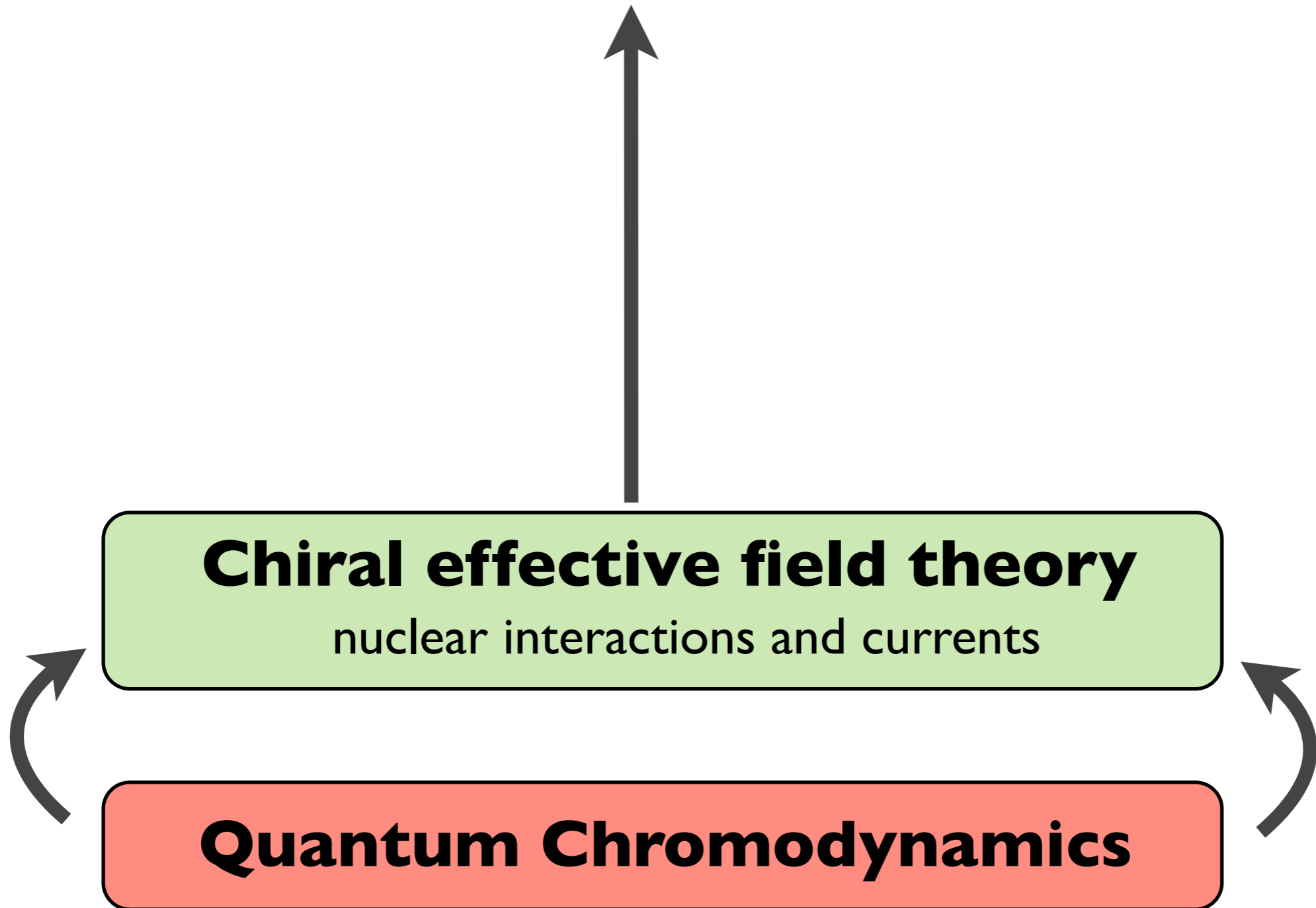
Quantum Chromodynamics

Ab initio nuclear structure theory

**nuclear structure and
reaction observables**

Chiral effective field theory
nuclear interactions and currents

Quantum Chromodynamics



Ab initio nuclear structure theory

**nuclear structure and
reaction observables**



ab initio many-body frameworks

Faddeev, Quantum Monte Carlo, no-core shell model, coupled cluster ...

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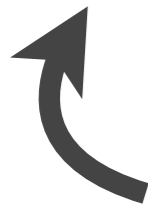
Faddeev, Quantum Monte Carlo, no-core shell model, coupled cluster ...

Renormalization Group methods

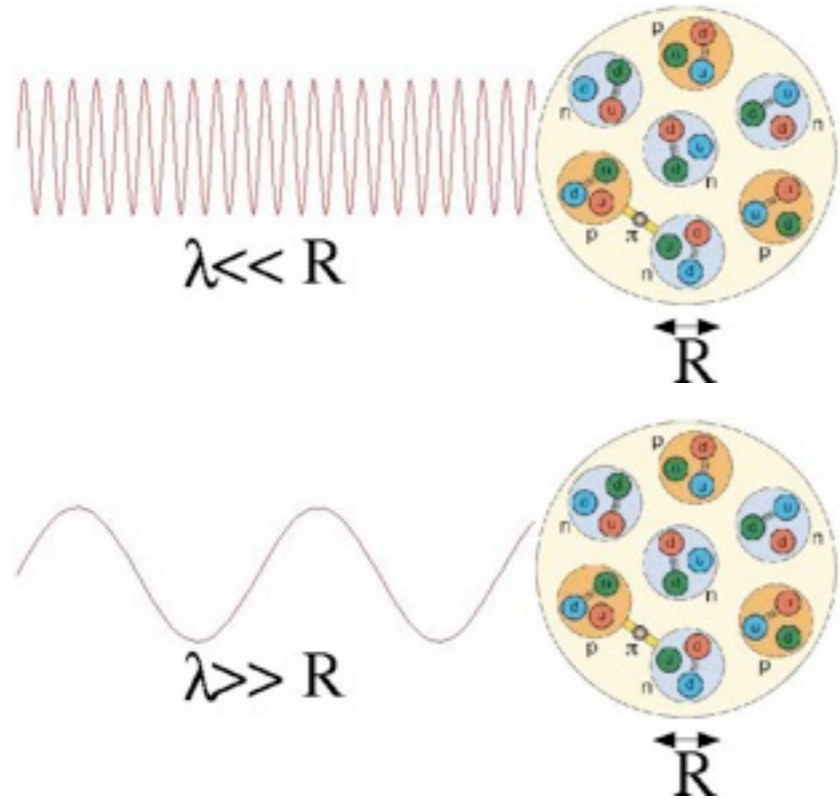
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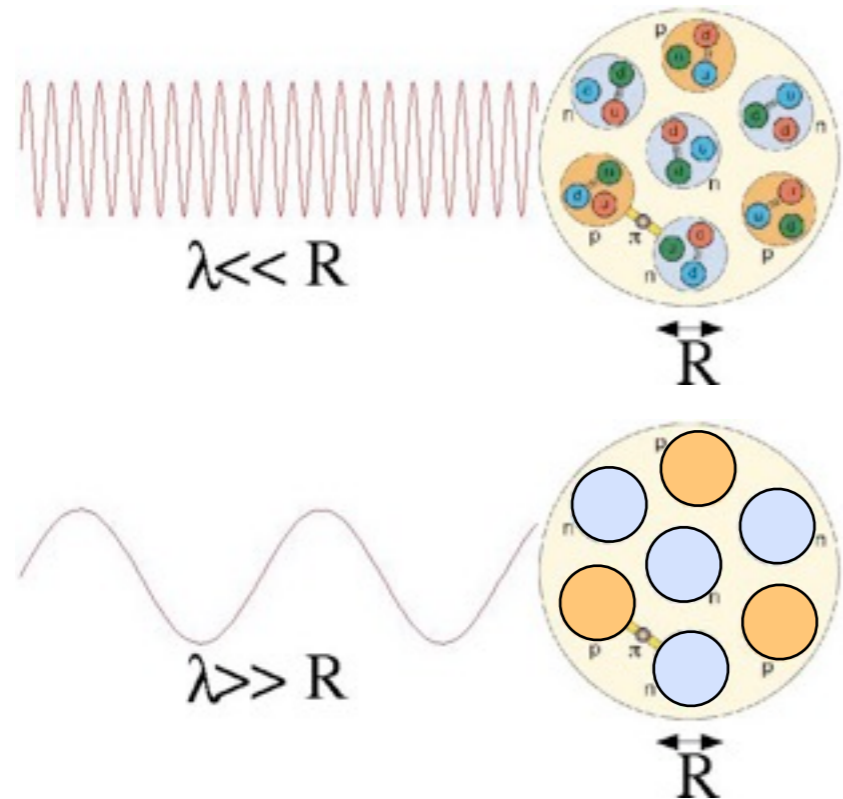


Nuclear effective degrees of freedom

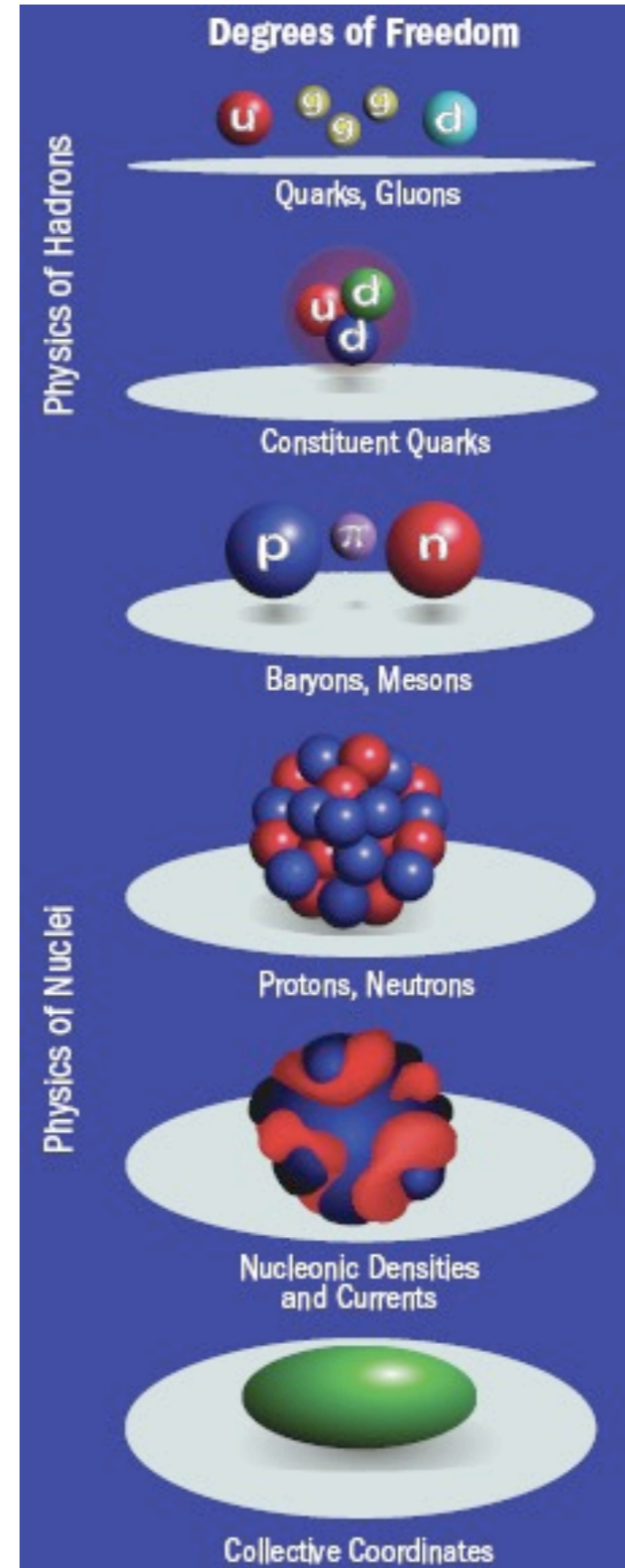


- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved

Nuclear effective degrees of freedom



- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved
- replace fine structure by something simpler (like multipole expansion), low-energy observables unchanged



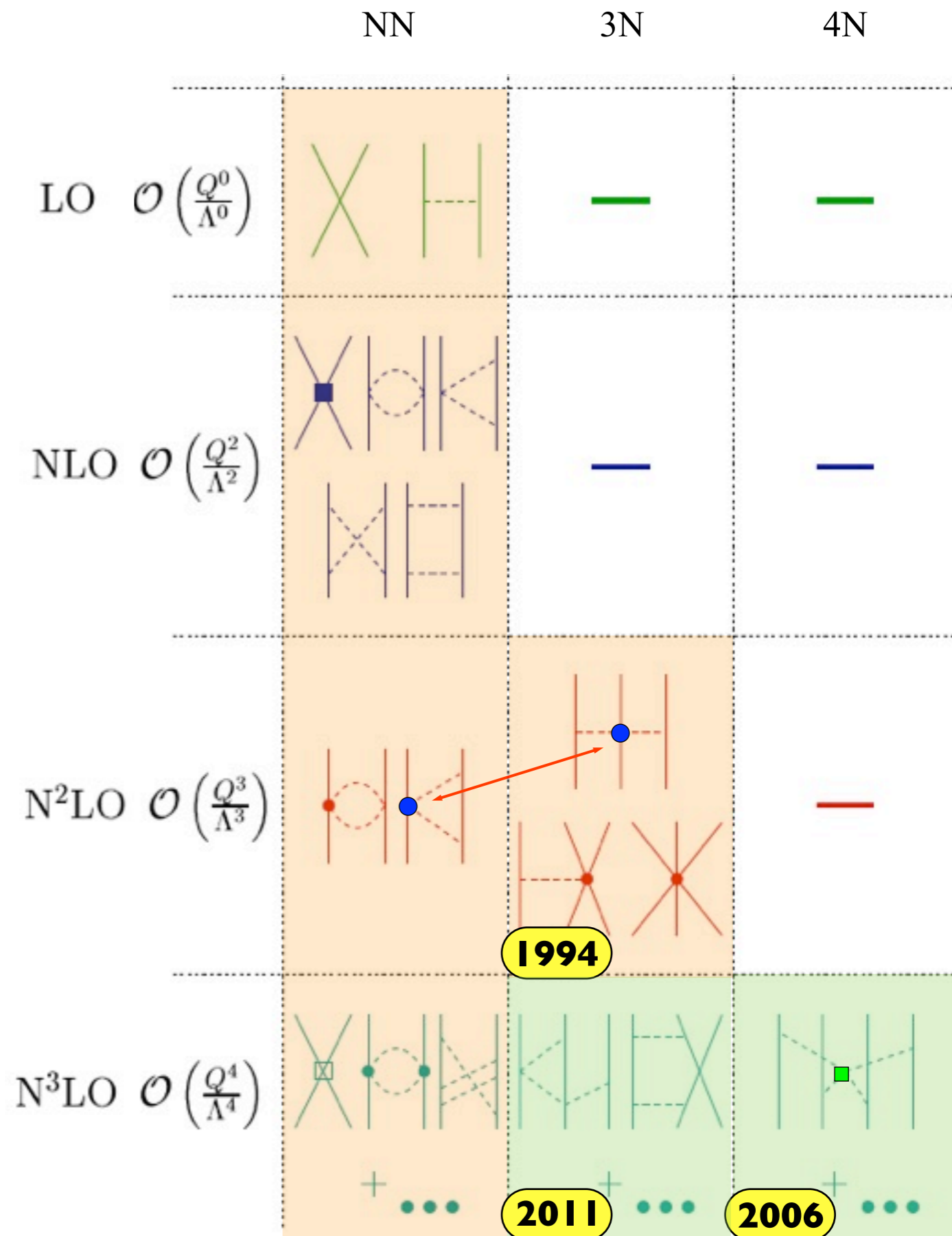
Resolution



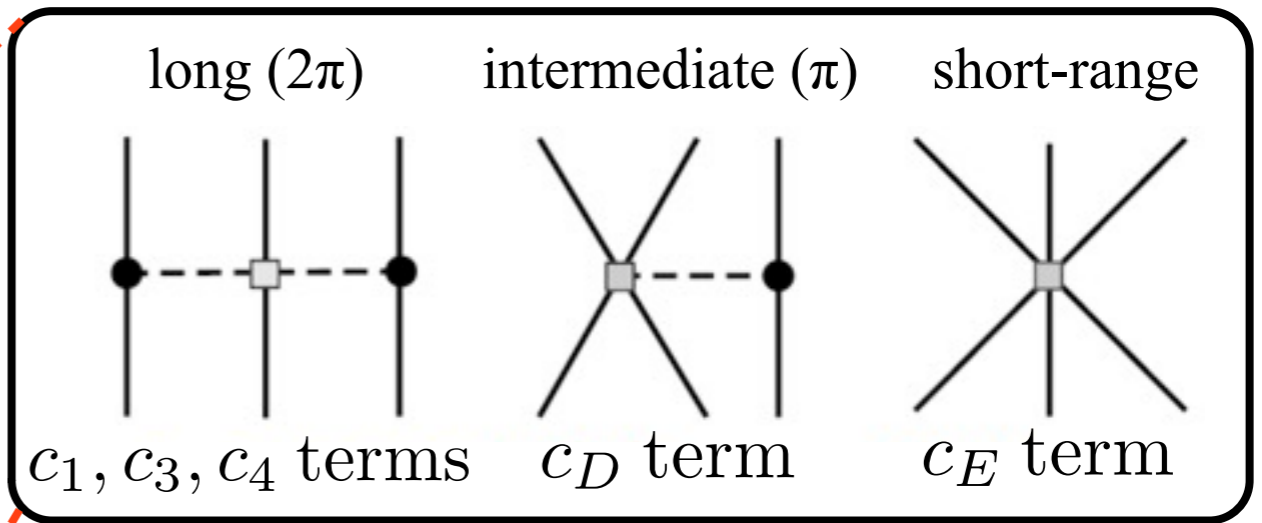
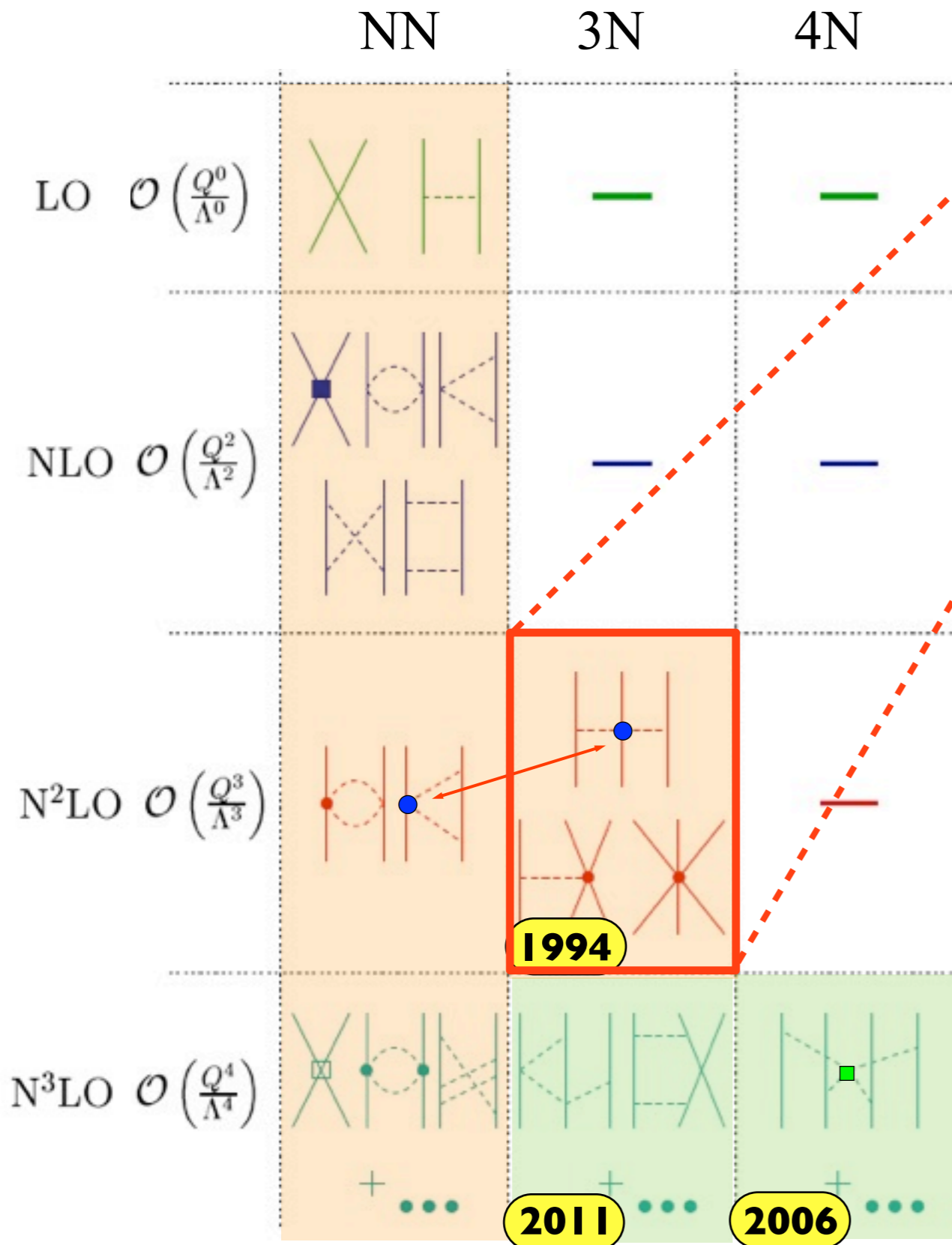
→ effective field theory

Chiral effective field theory for nuclear forces

- choose relevant degrees of freedom: here nucleons and pions
- operators constrained by symmetries of QCD
- short-range physics captured in few short-range couplings
- separation of scales: $Q \ll \Lambda_b$, breakdown scale $\Lambda_b \sim 500$ MeV
- power-counting: expand in powers Q/Λ_b
- systematic: work to desired accuracy, obtain error estimates



Many-body forces in chiral EFT

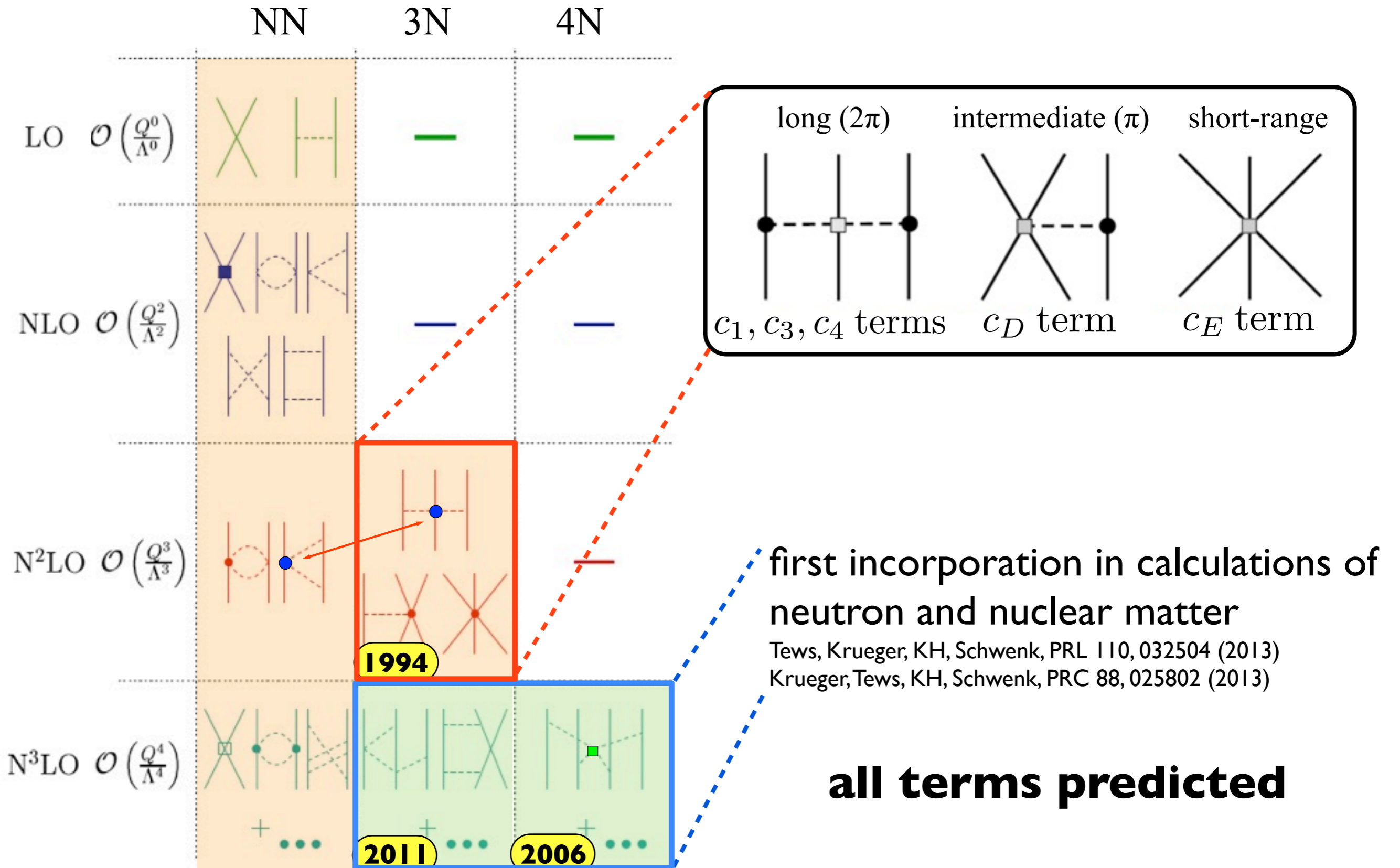


1994

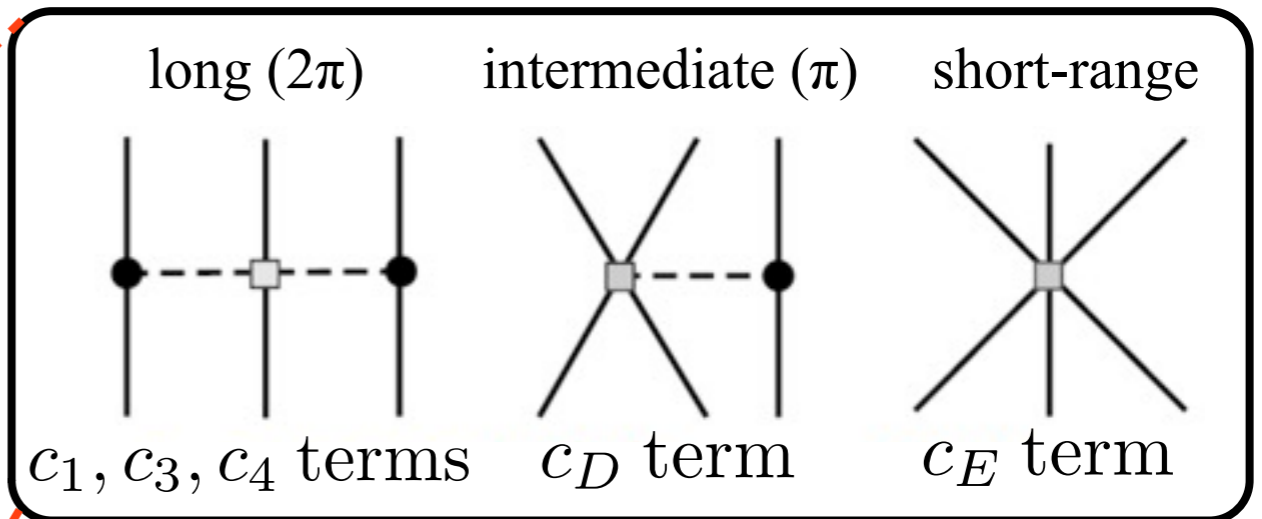
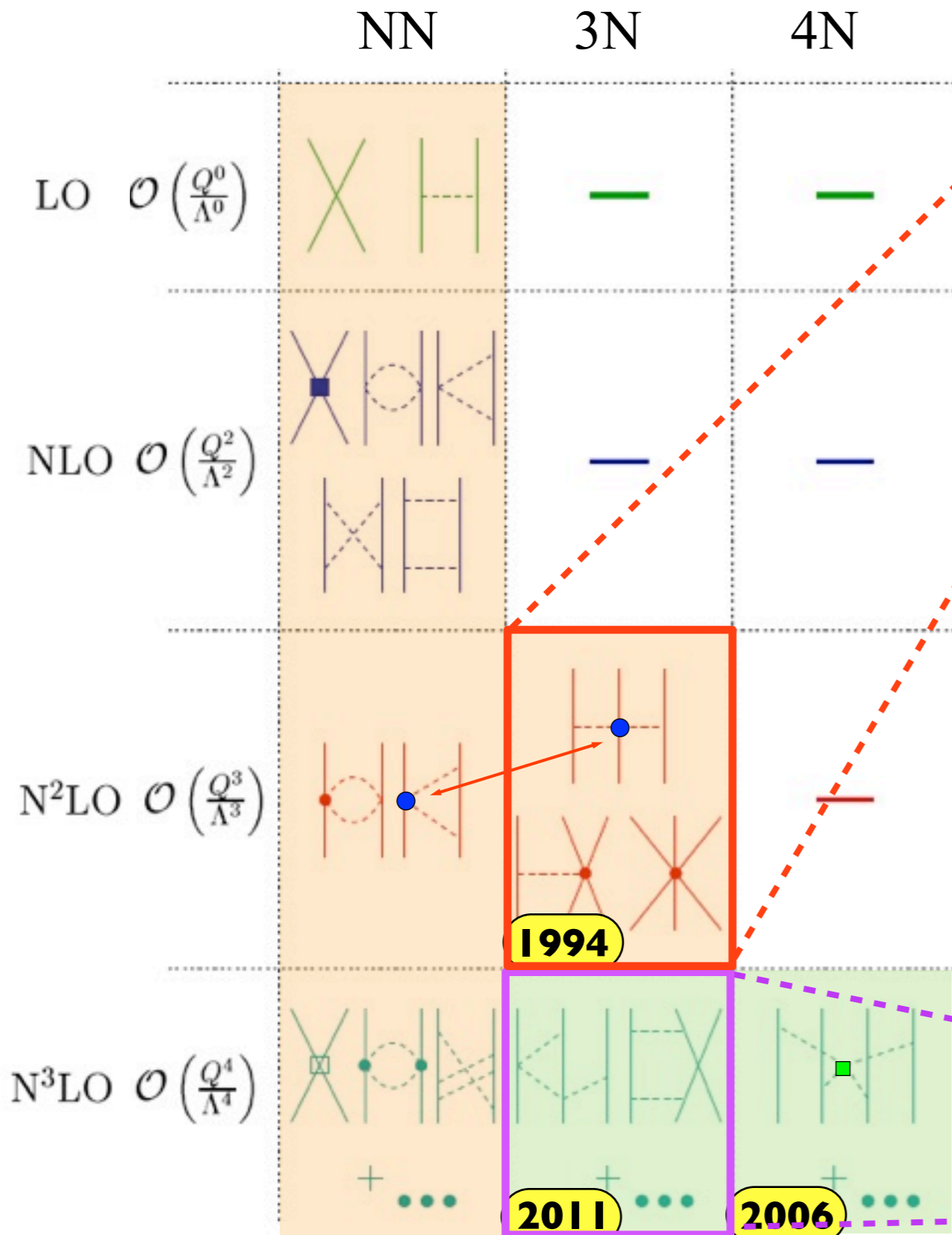
2011

2006

Many-body forces in chiral EFT



Many-body forces in chiral EFT



first incorporation in calculations of neutron and nuclear matter

Tews, Krueger, KH, Schwenk, PRL 110, 032504 (2013)
 Krueger, Tews, KH, Schwenk, PRC 88, 025802 (2013)

first calculation of matrix elements for ab initio studies of matter and nuclei

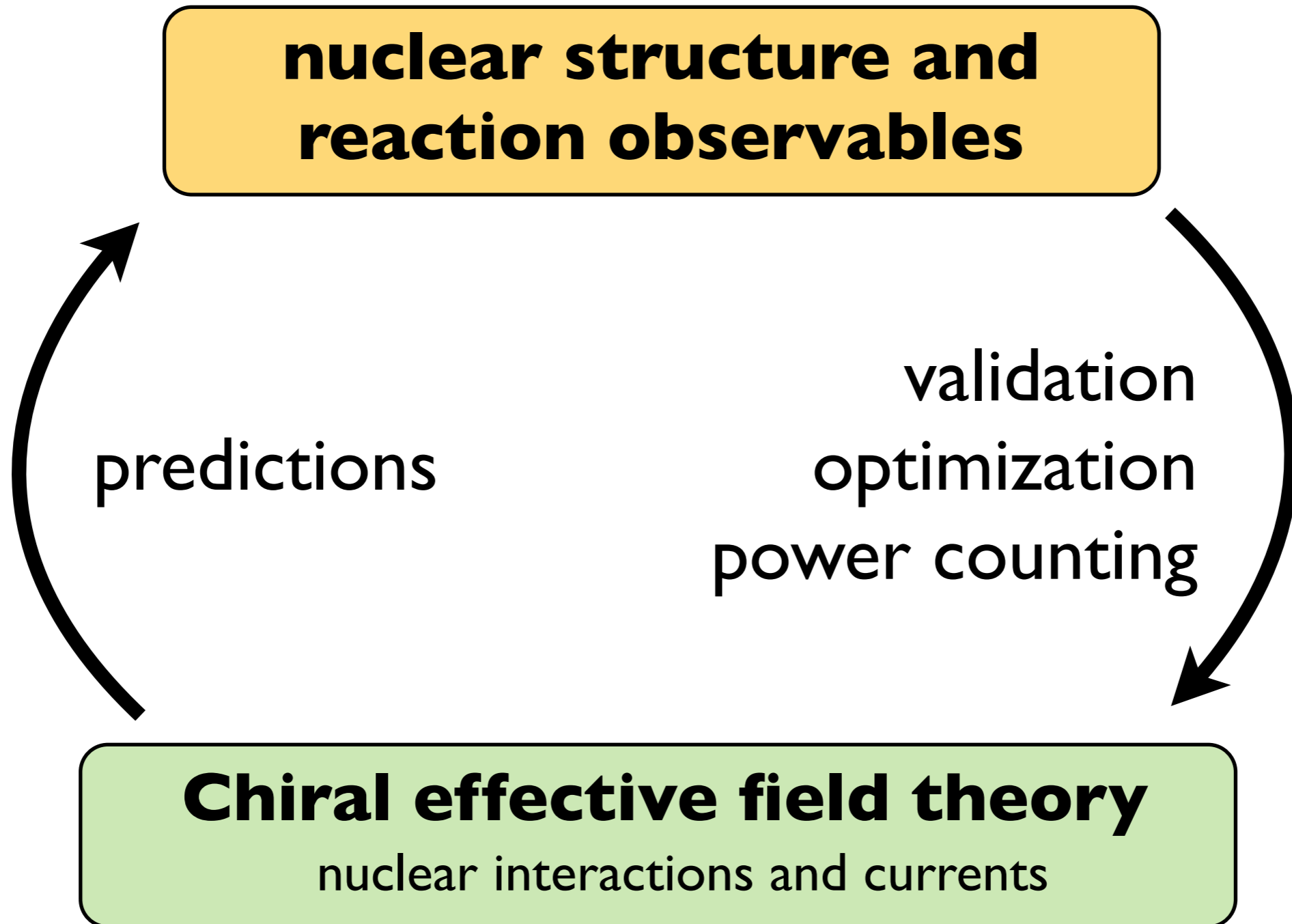
KH, Krebs, Epelbaum, Golak, Skibinski, PRC 91, 044001 (2015)

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Development of nuclear interactions

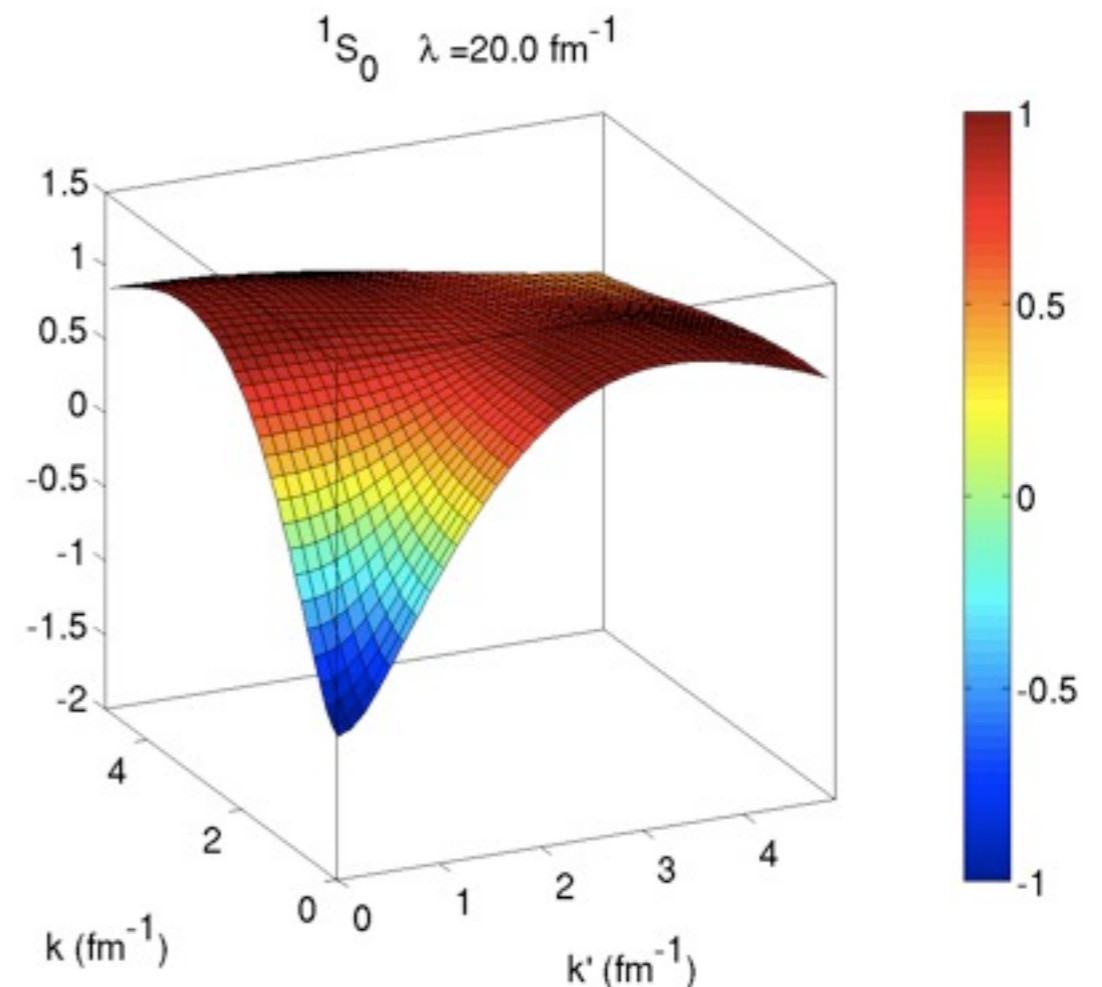
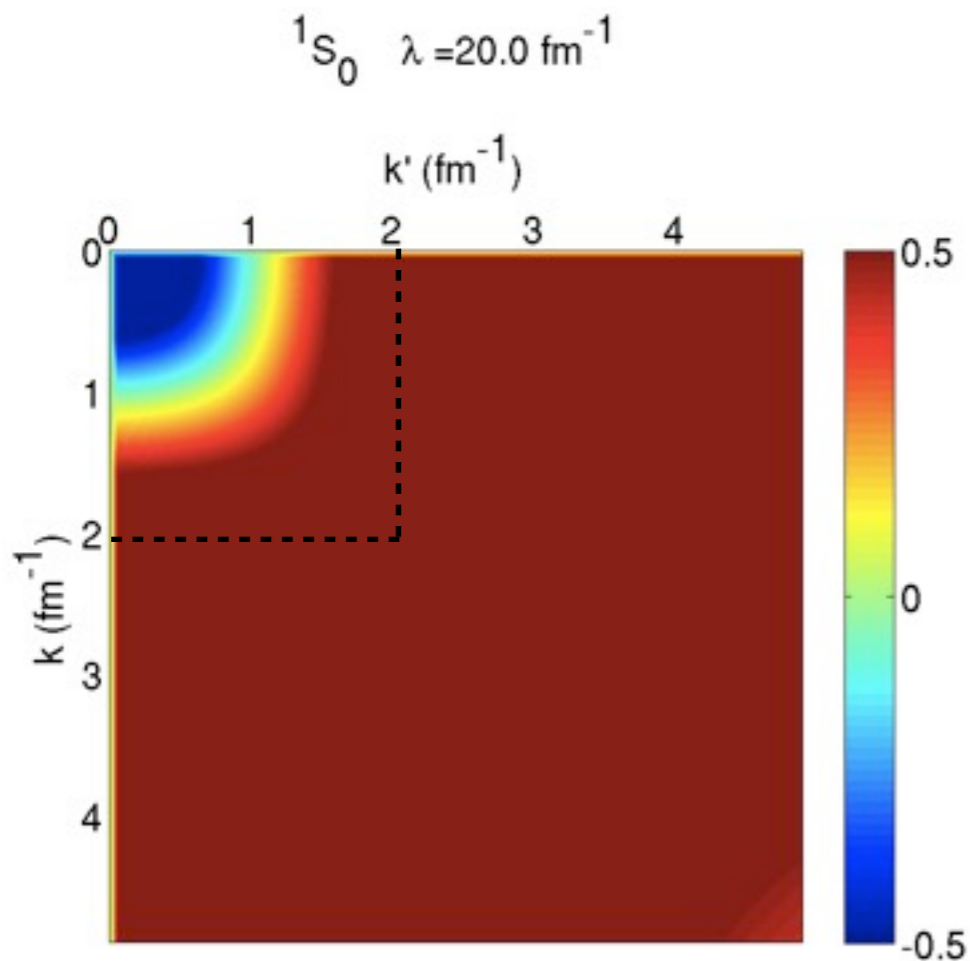


The Similarity Renormalization Group

- generate unitary transformation which **decouples** low- and high momenta

$$H_\lambda = U_\lambda H U_\lambda^\dagger \quad \text{with the resolution parameter } \lambda$$

- basic idea: change resolution successively in small steps: $\frac{dH_\lambda}{d\lambda} = [\eta_\lambda, H_\lambda]$
- generator η_λ can be chosen and tailored to different applications
- observables are preserved due to unitarity of transformation

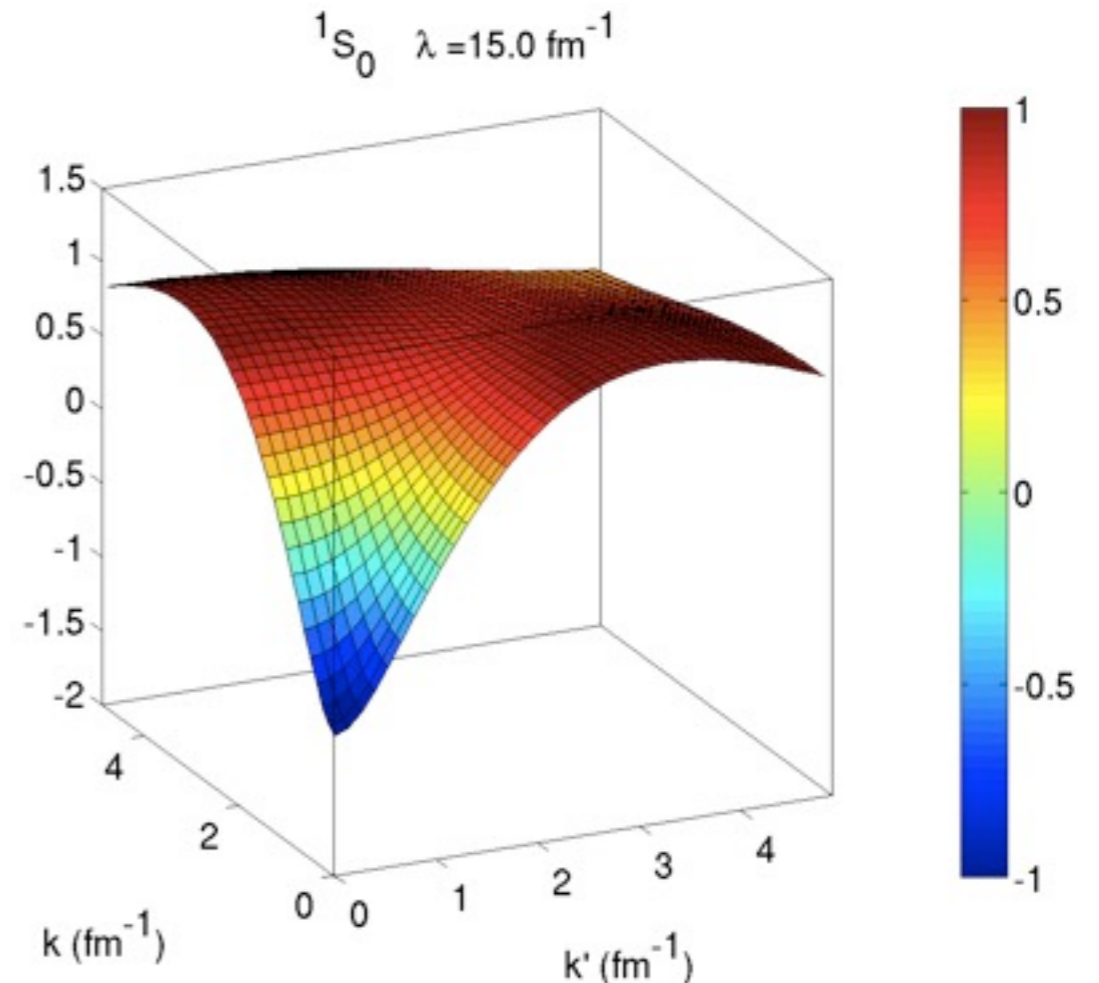
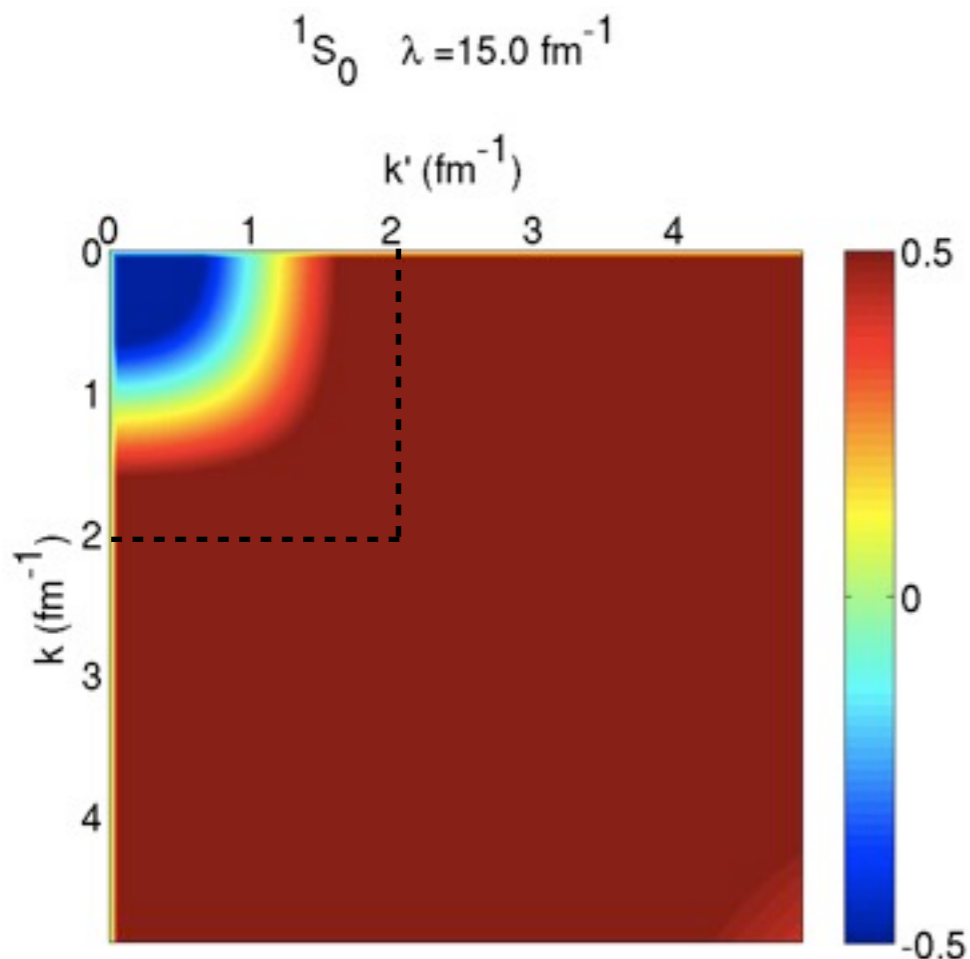


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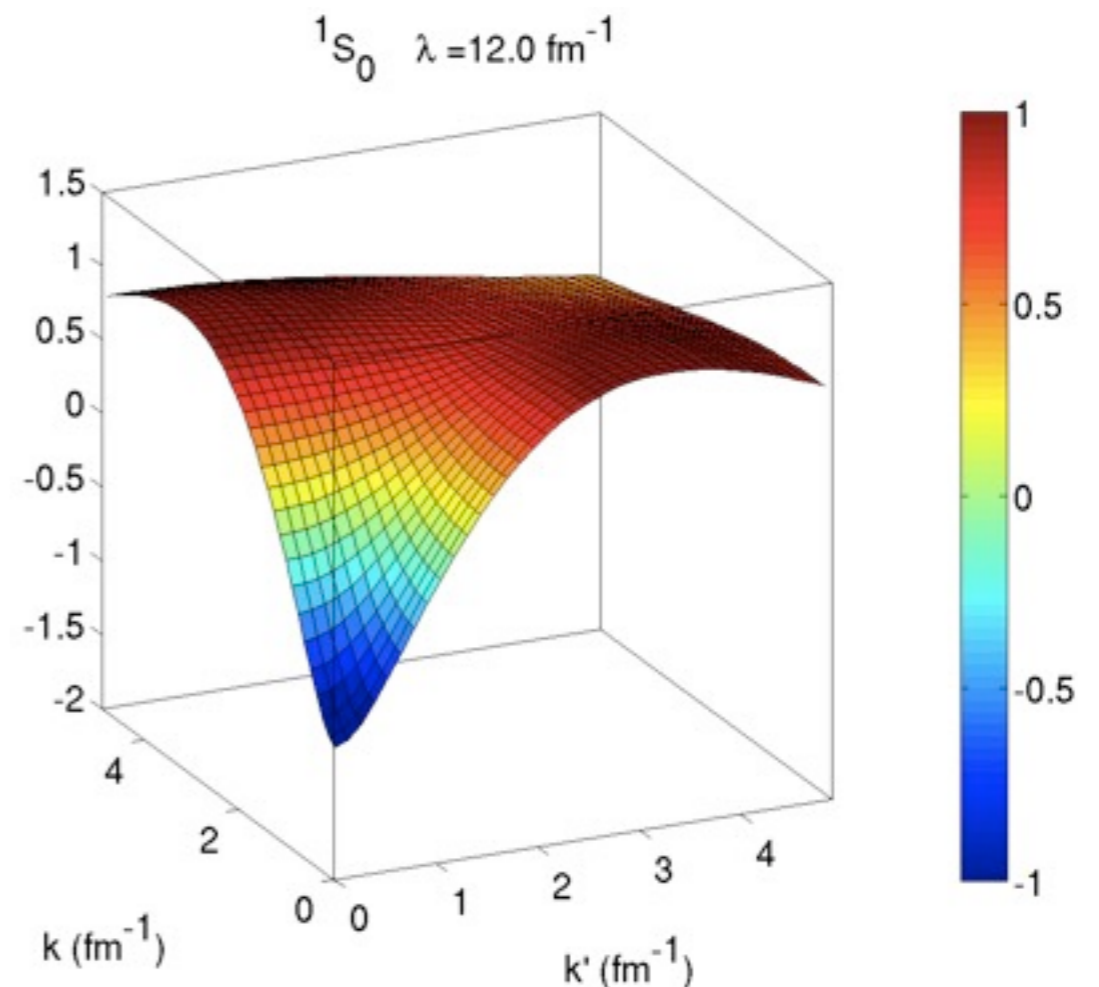
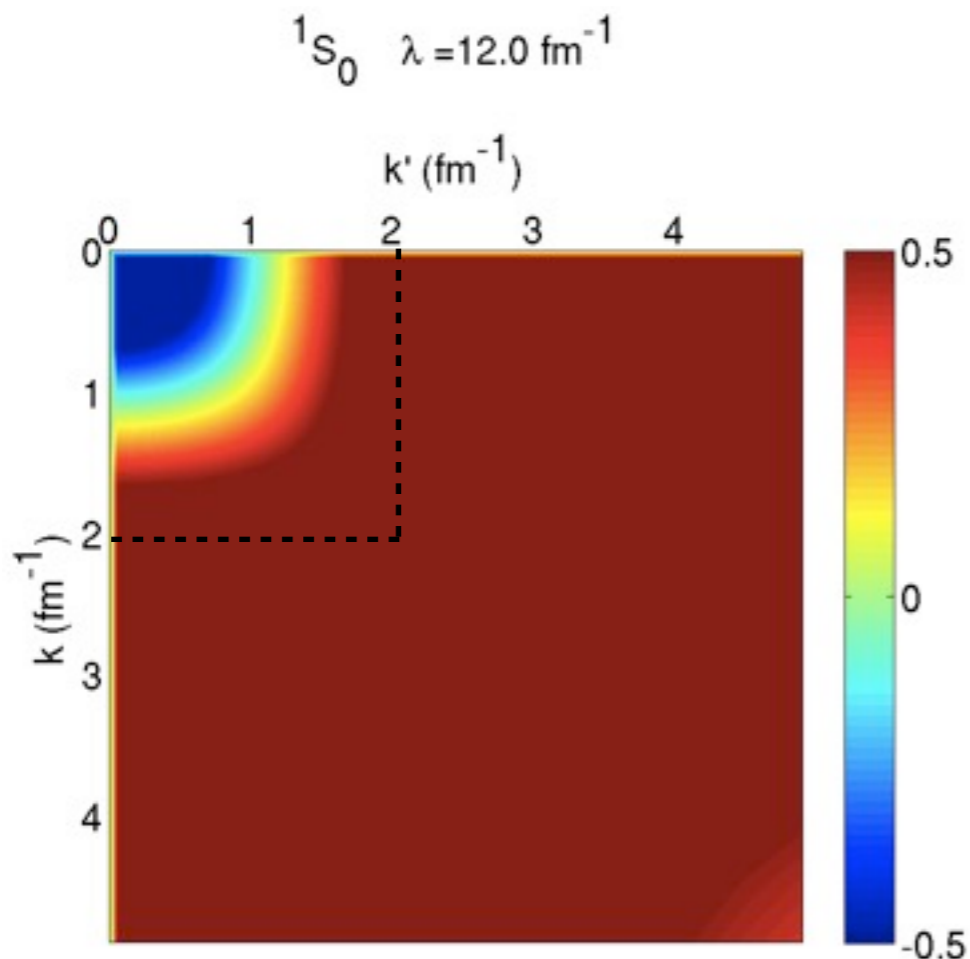


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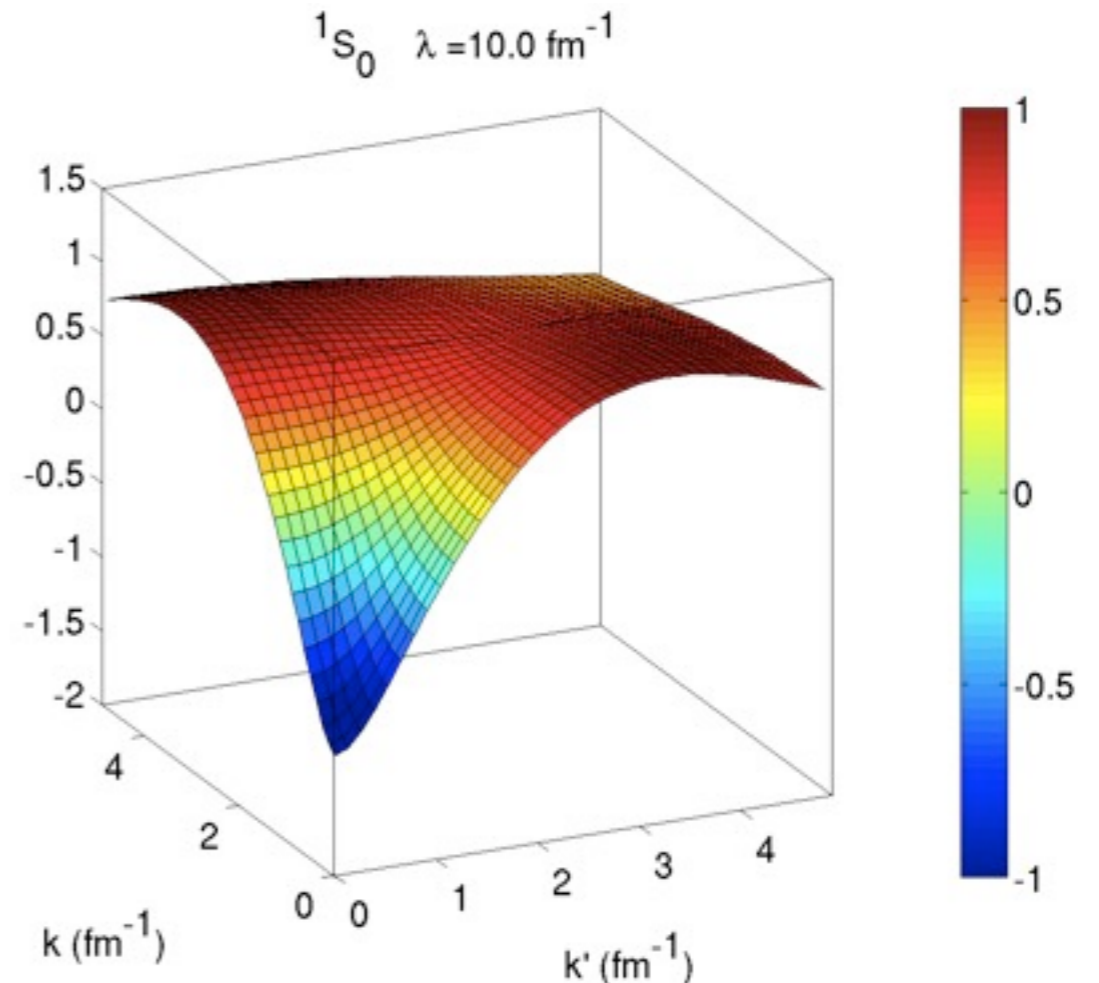
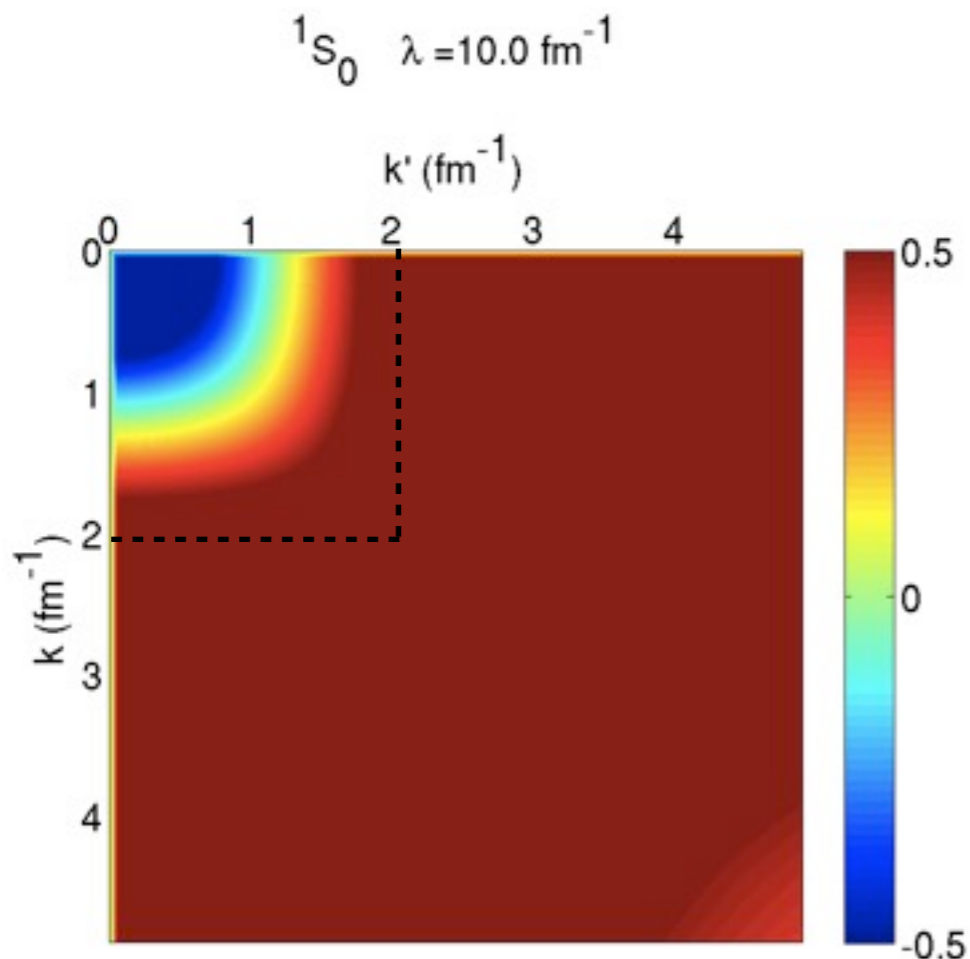


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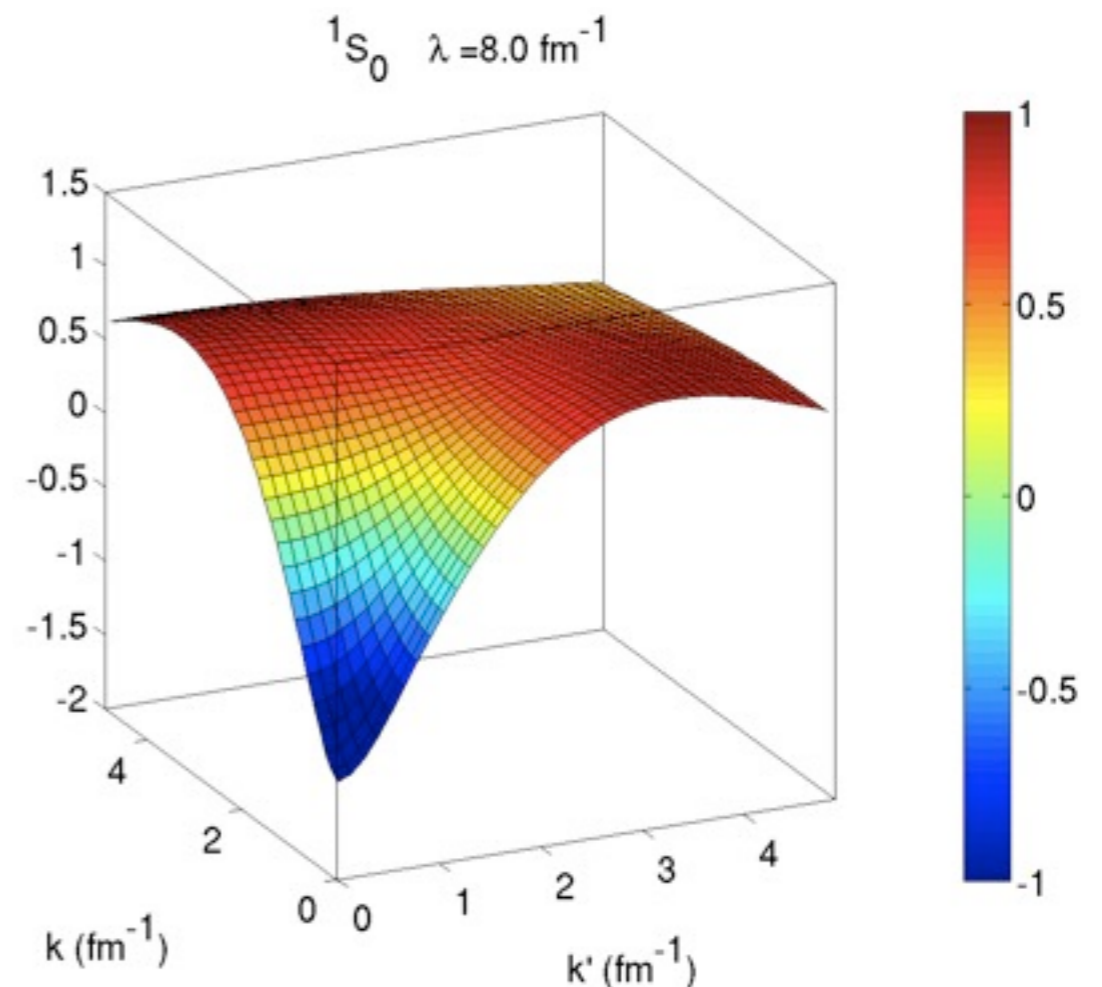
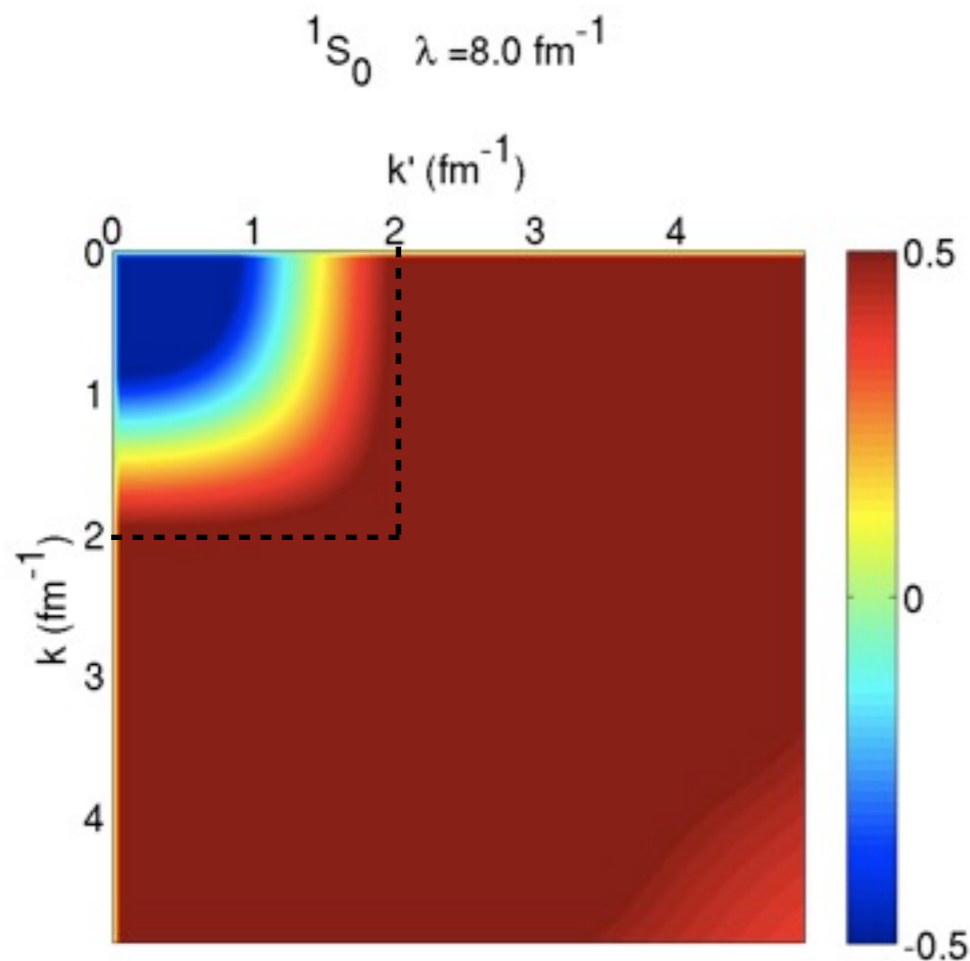


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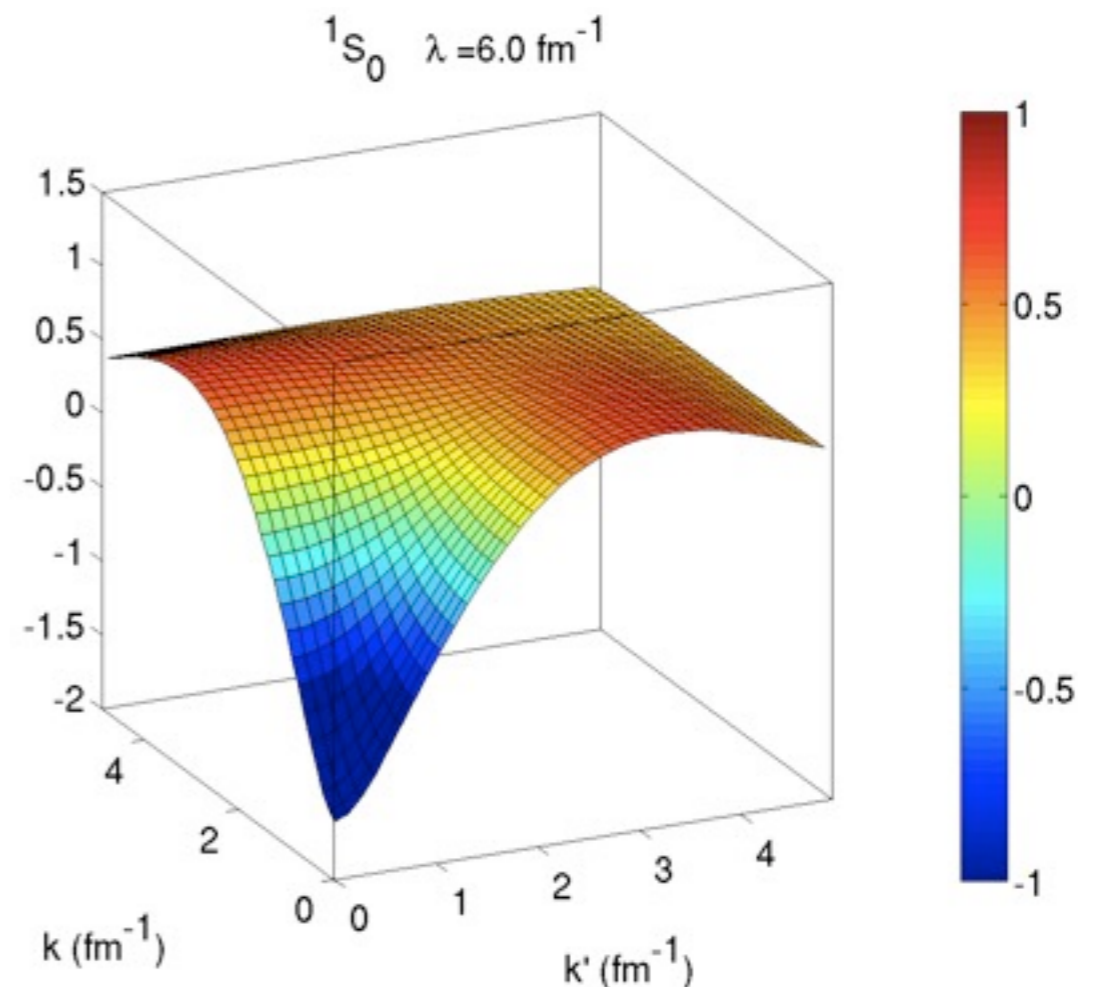
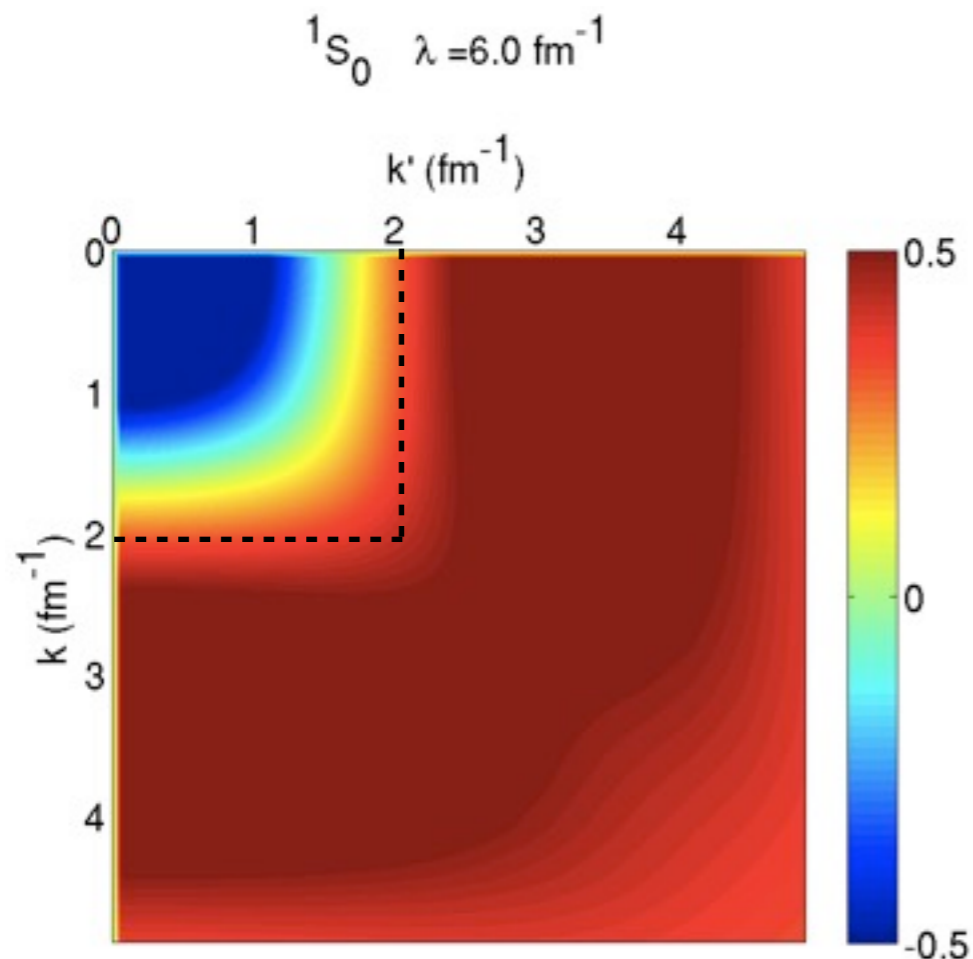


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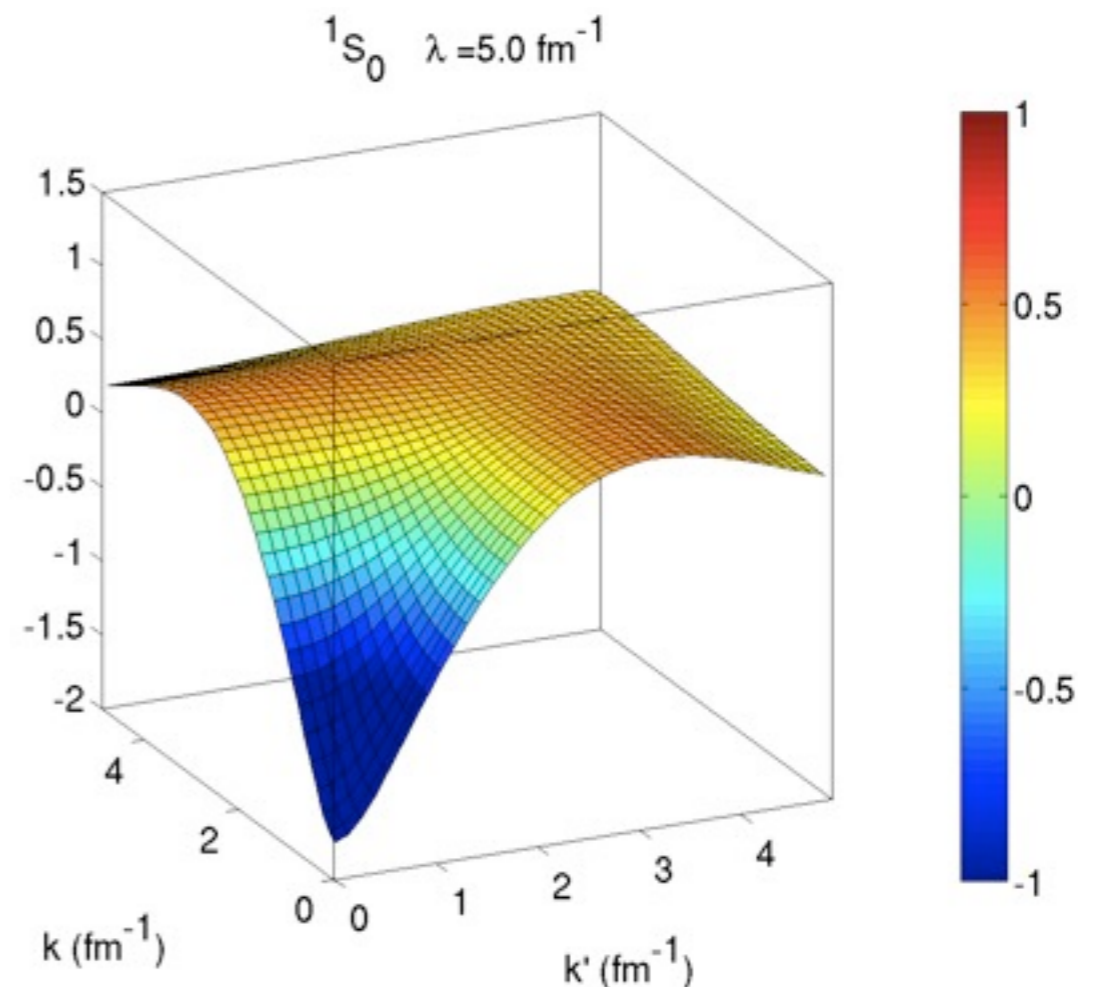
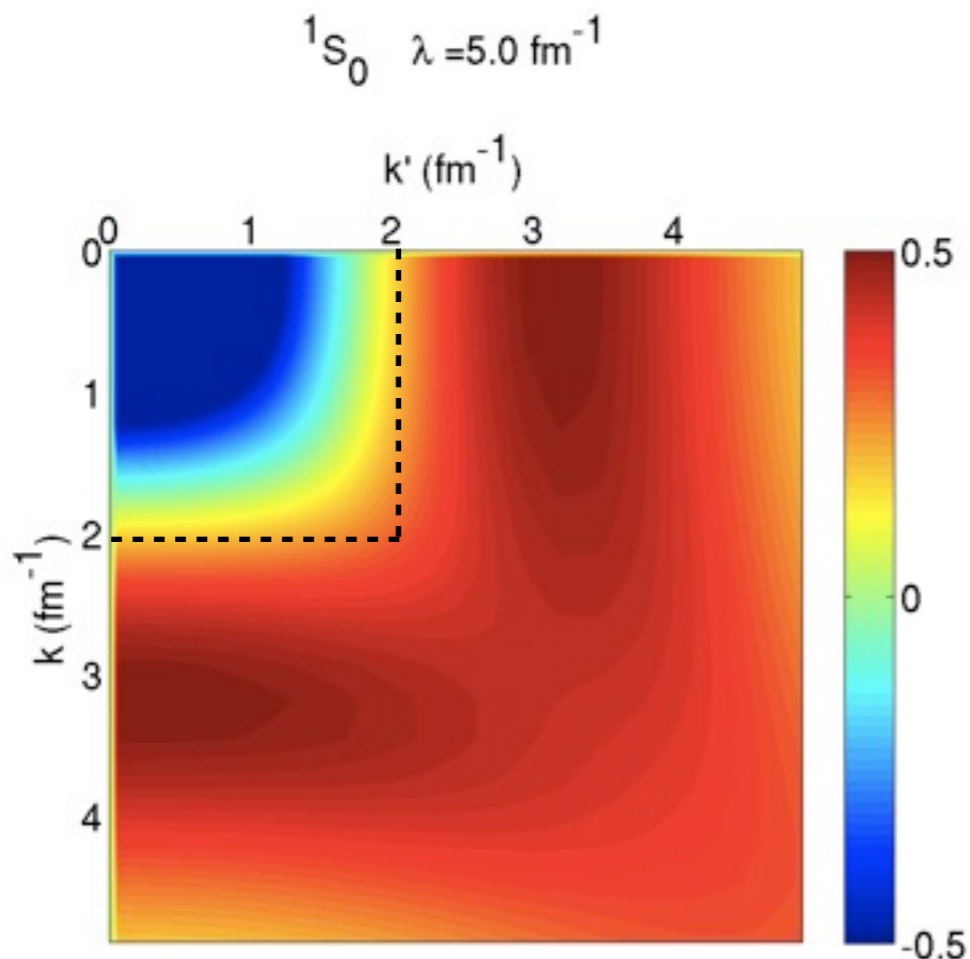


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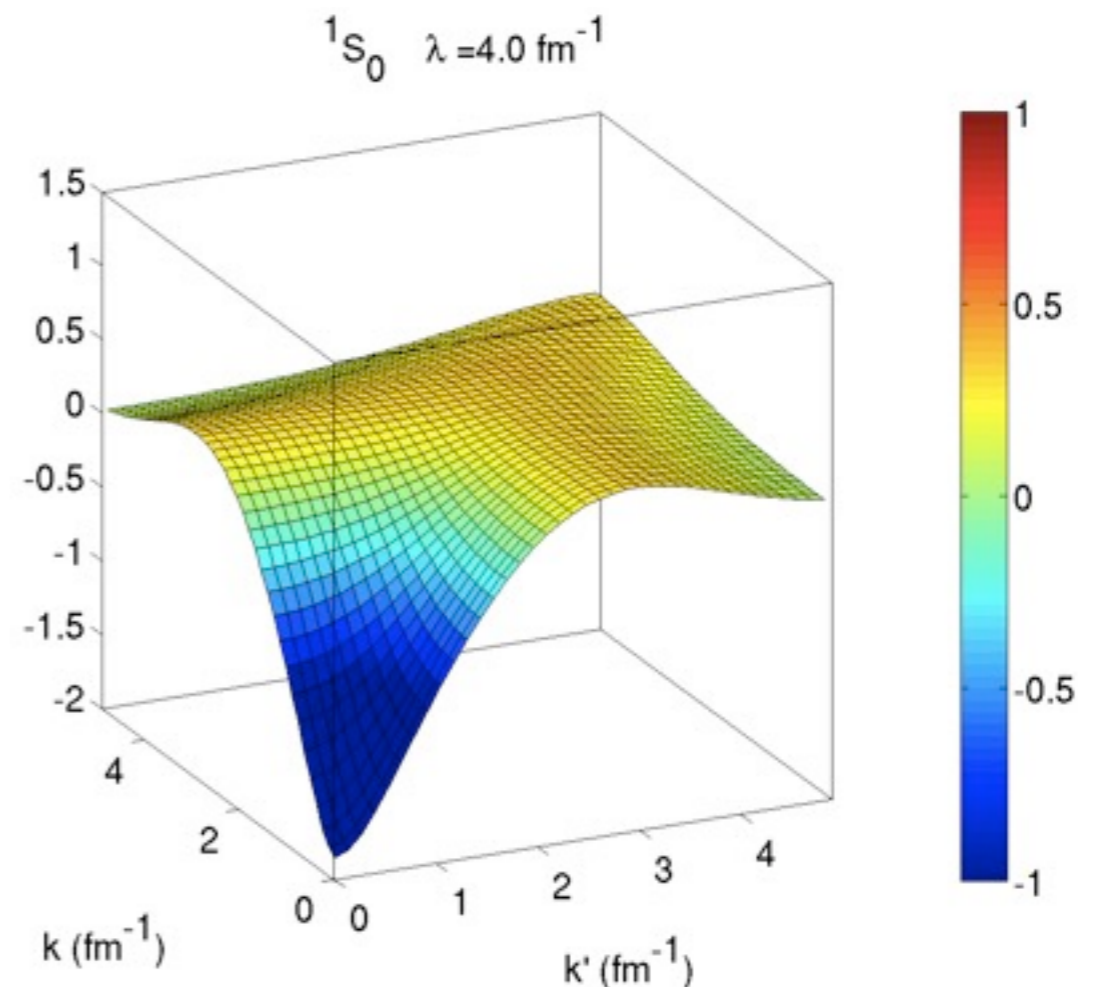
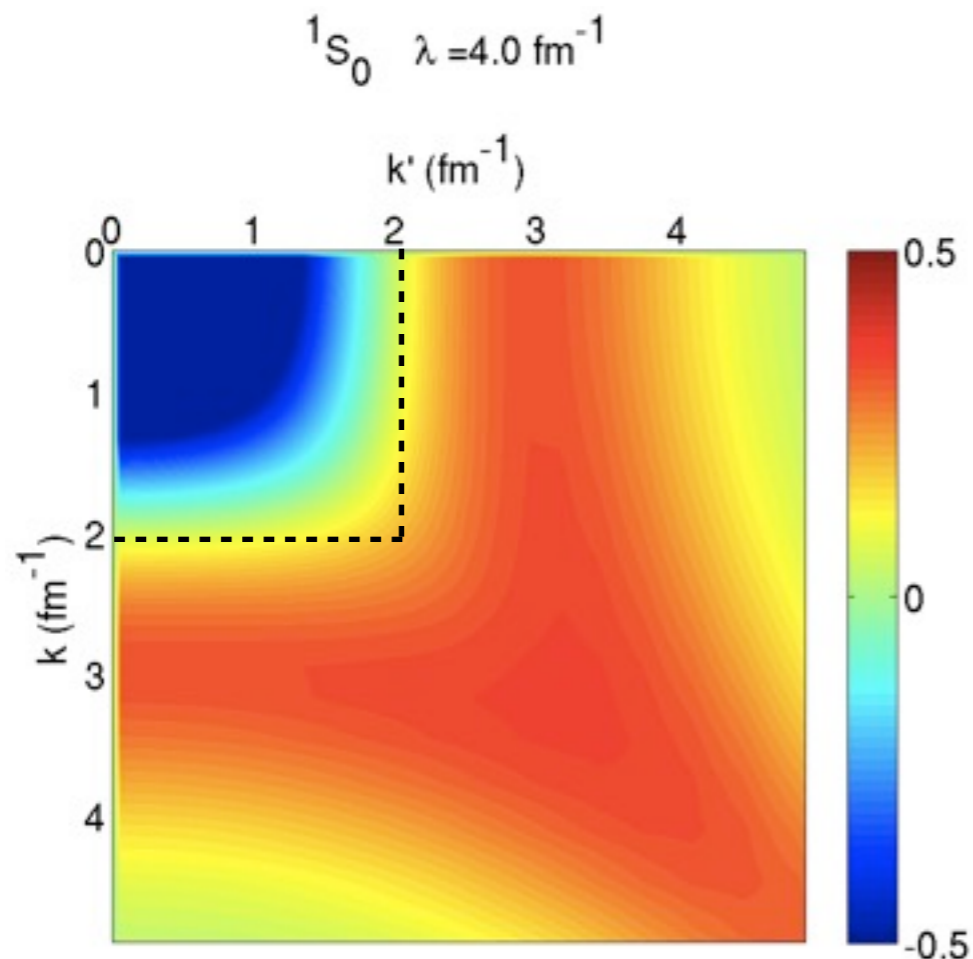


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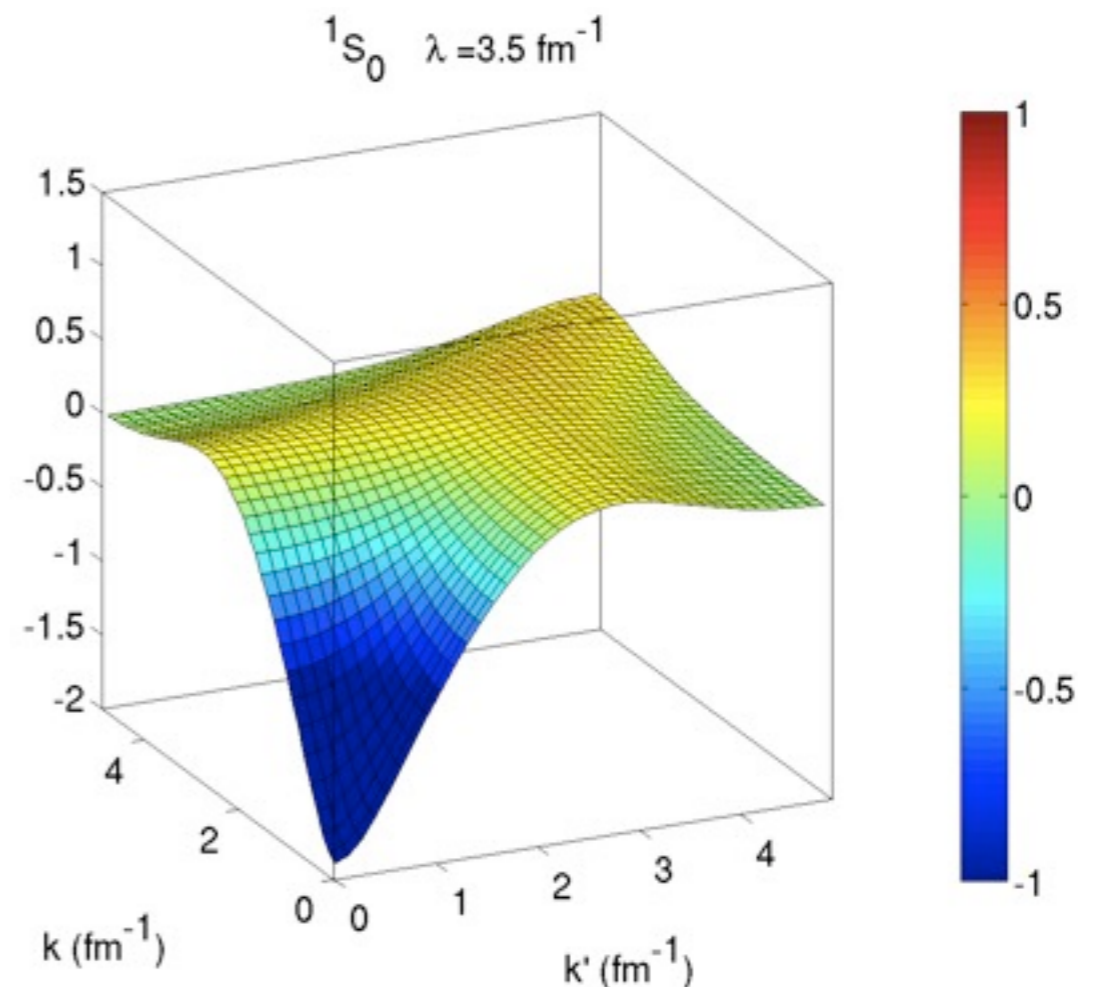
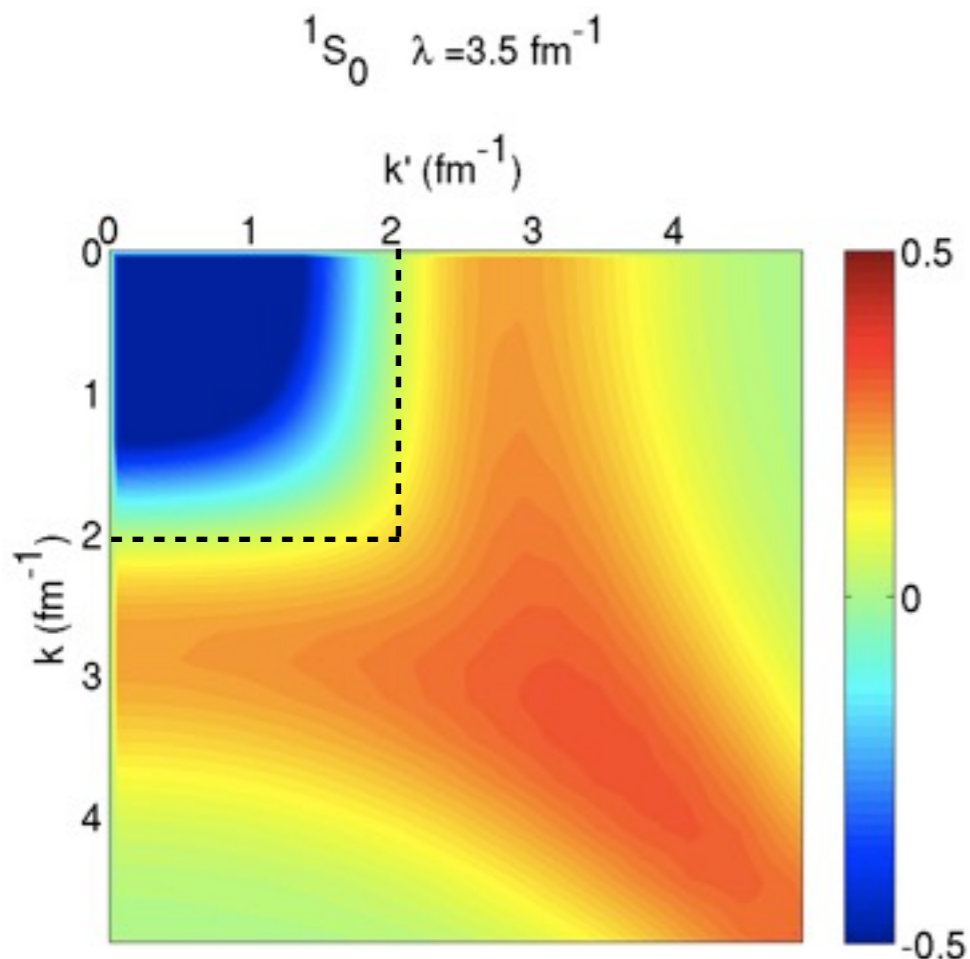


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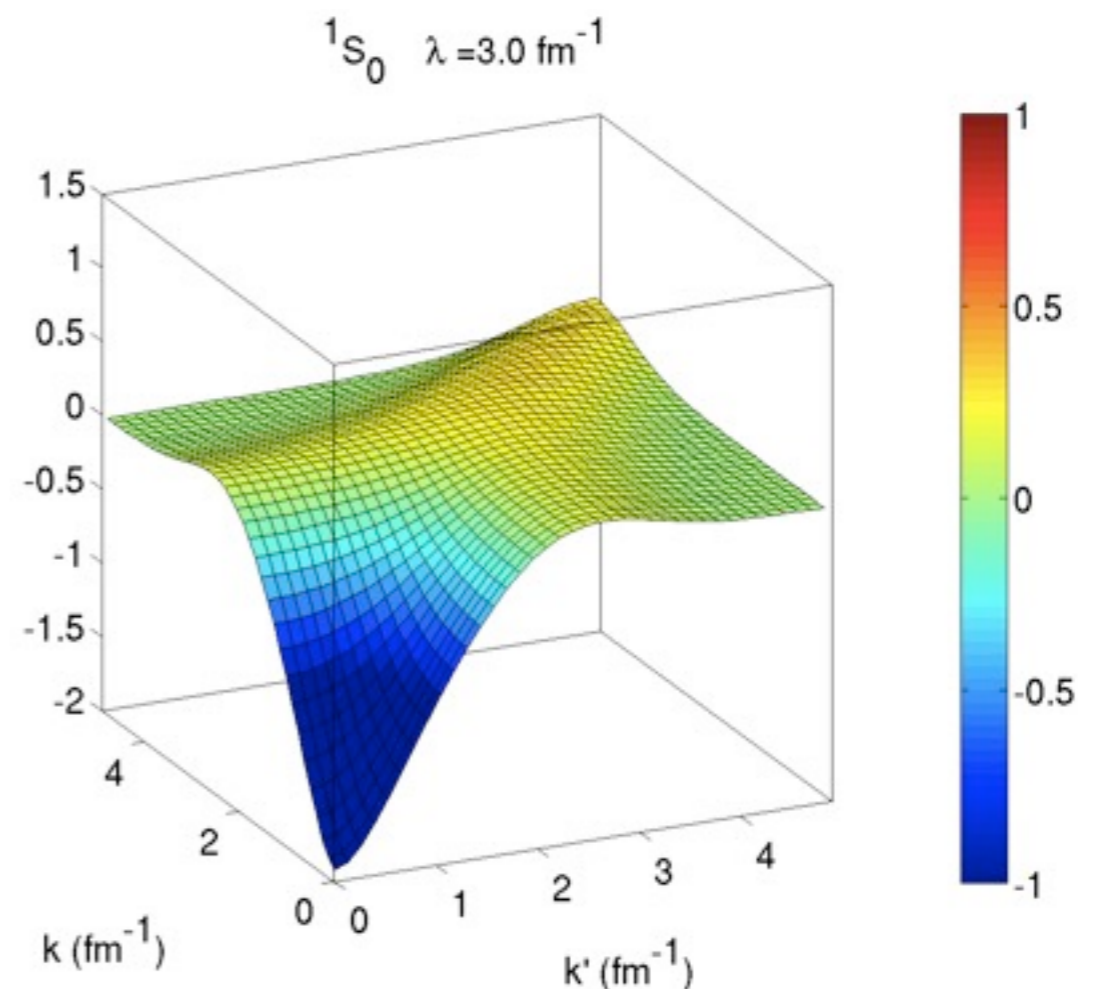
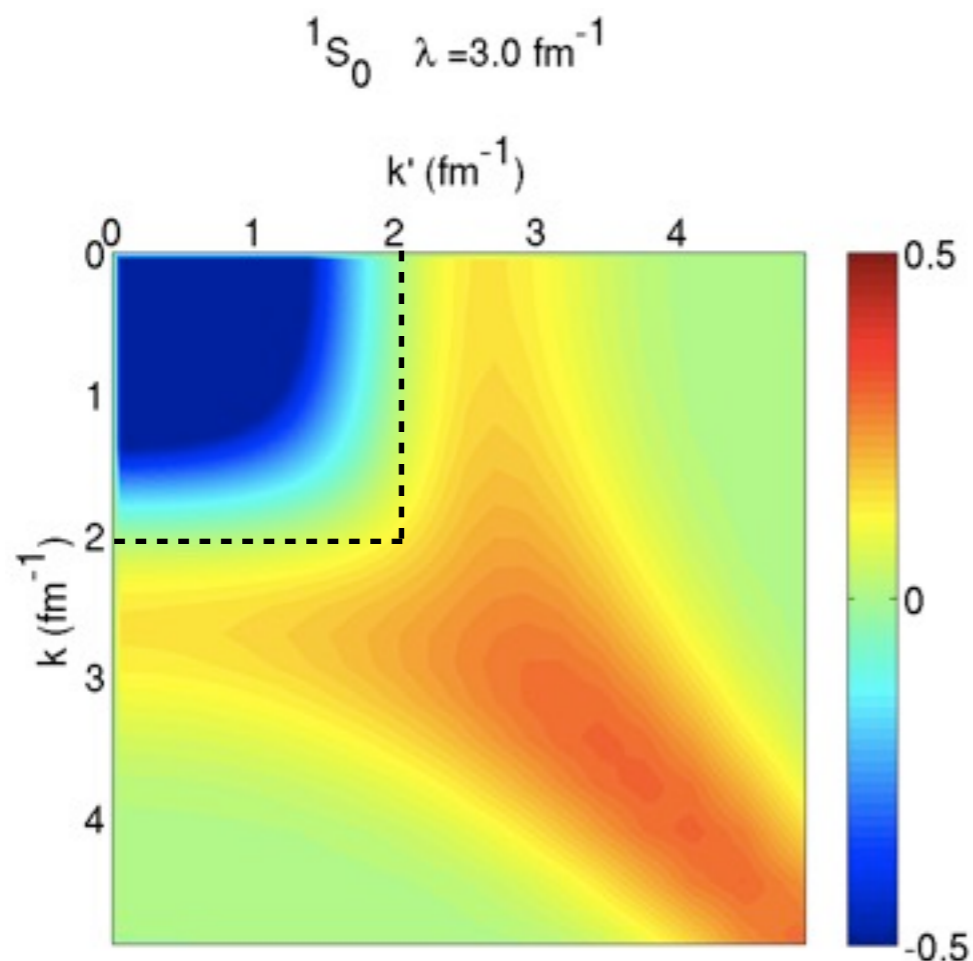


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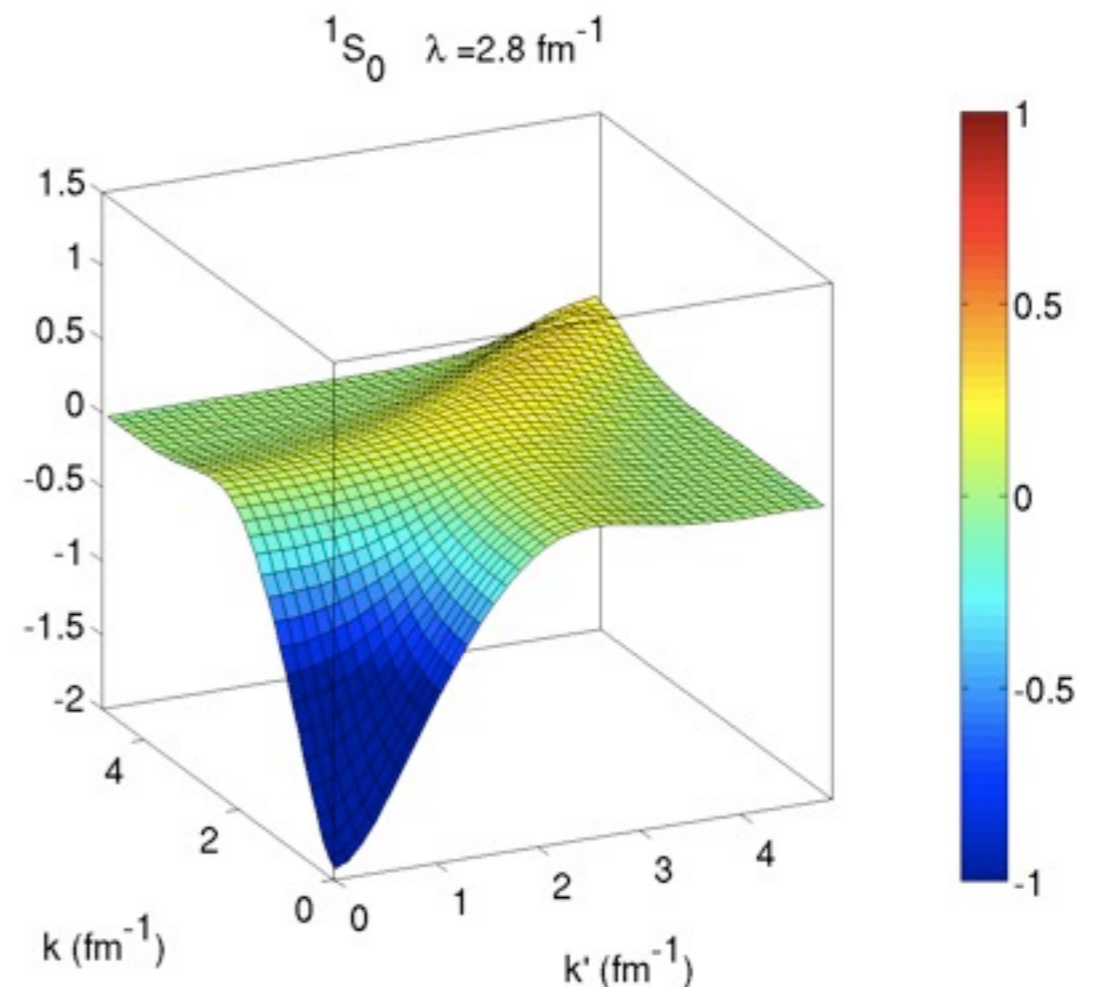
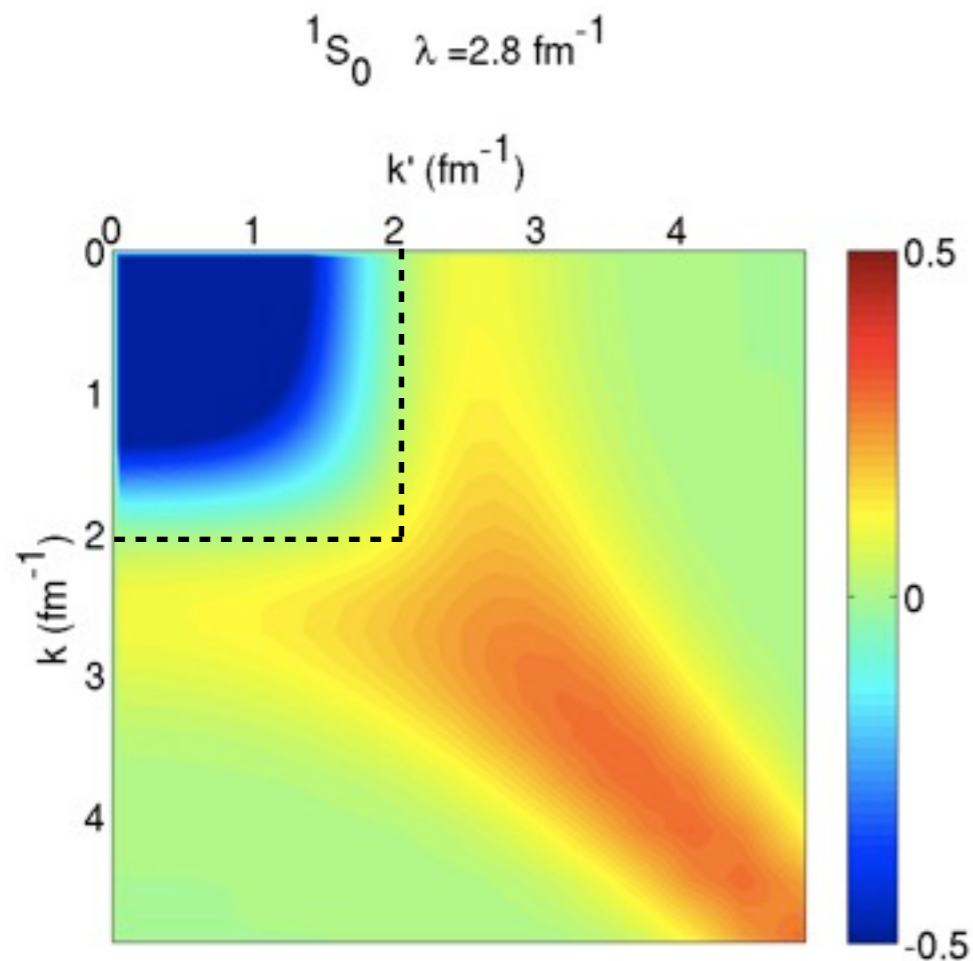


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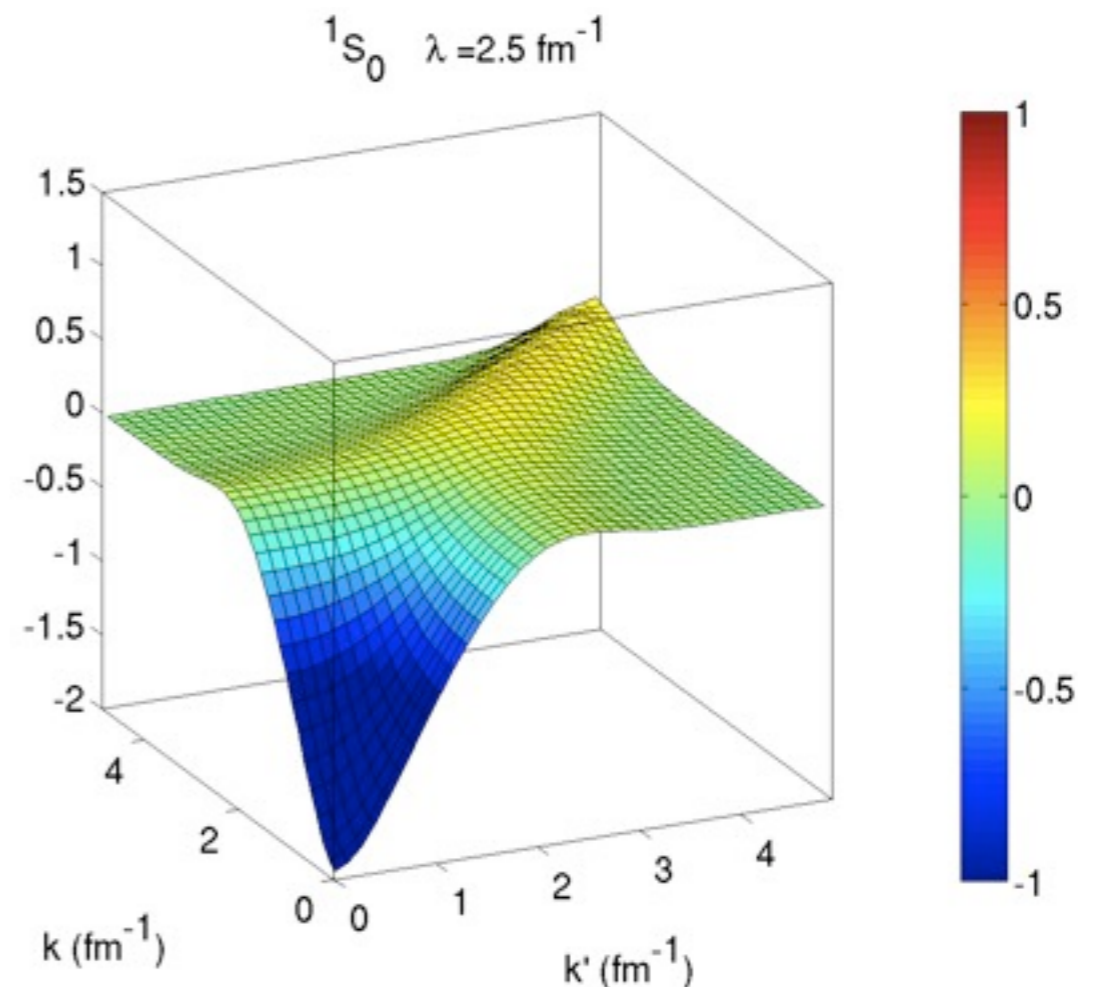
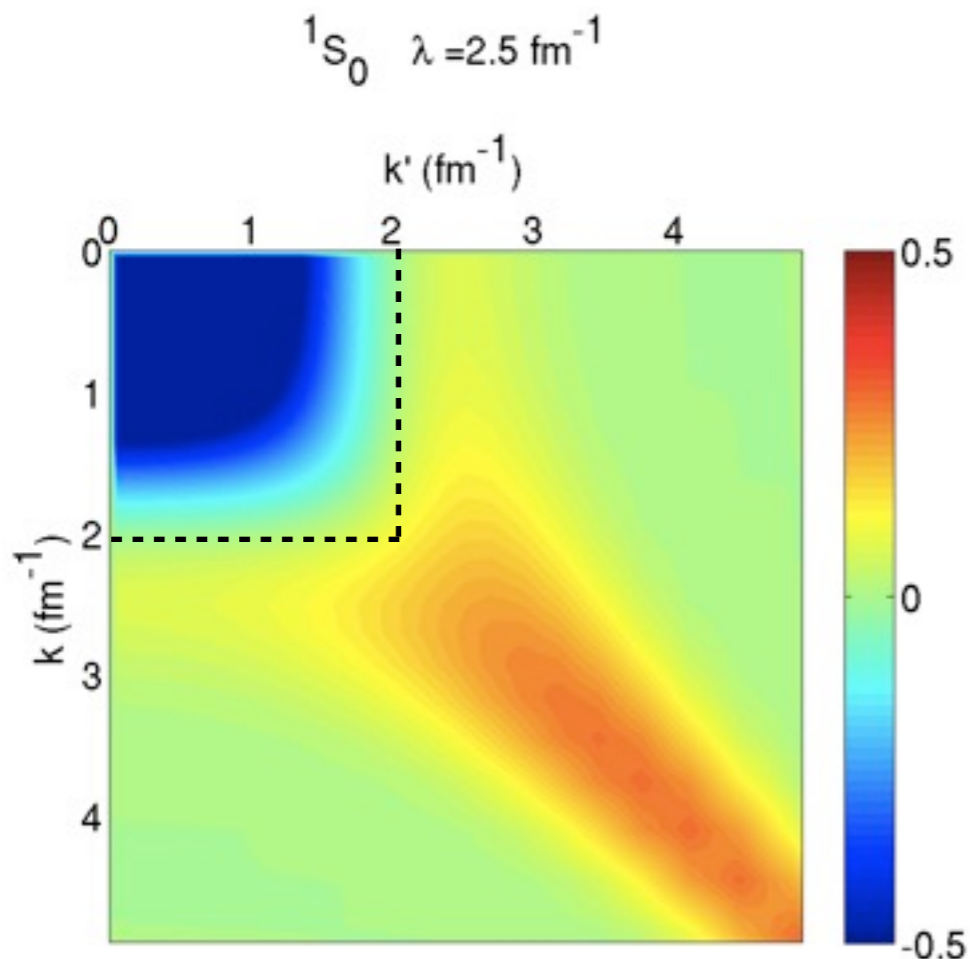


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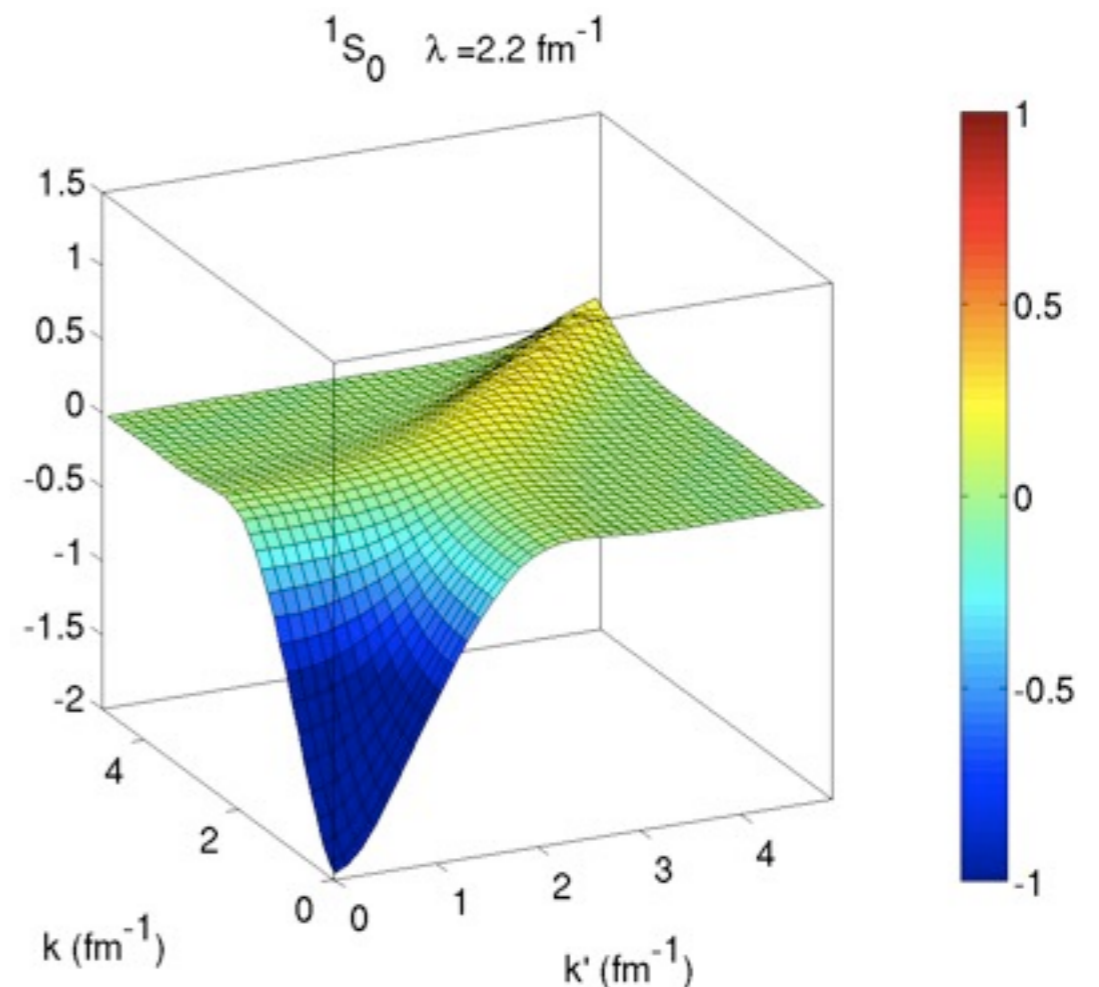
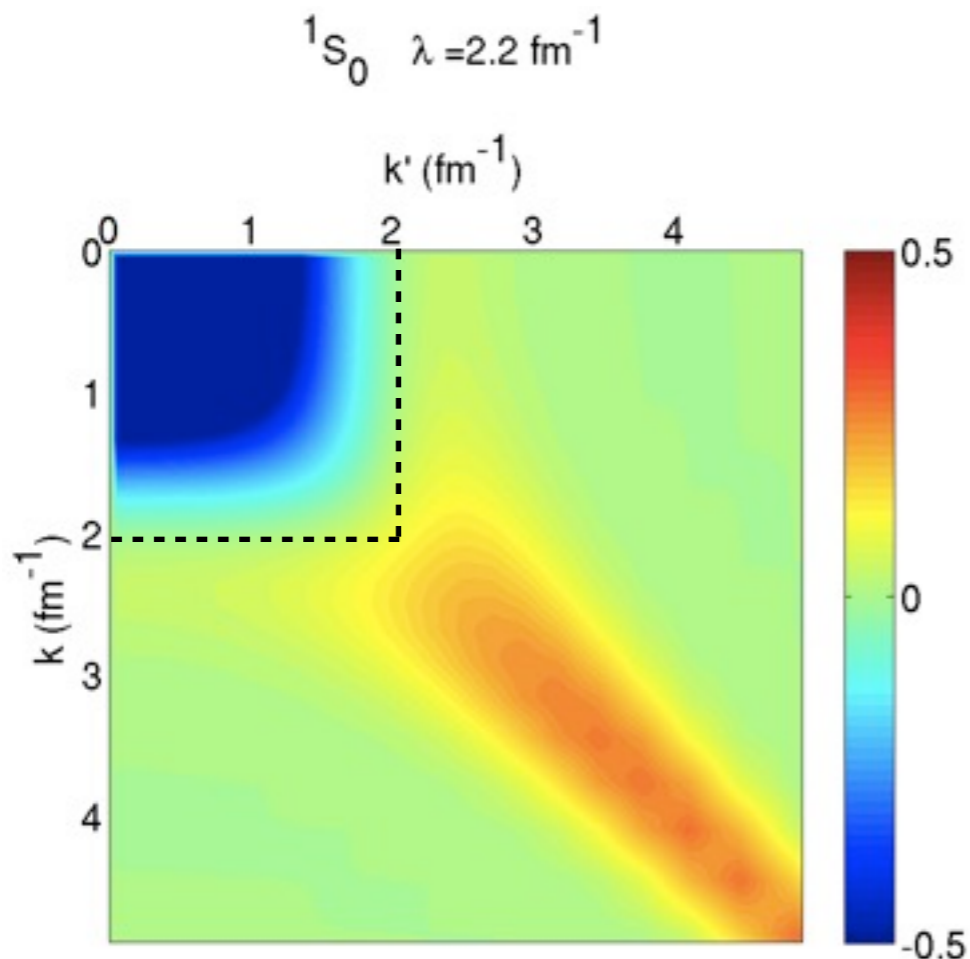


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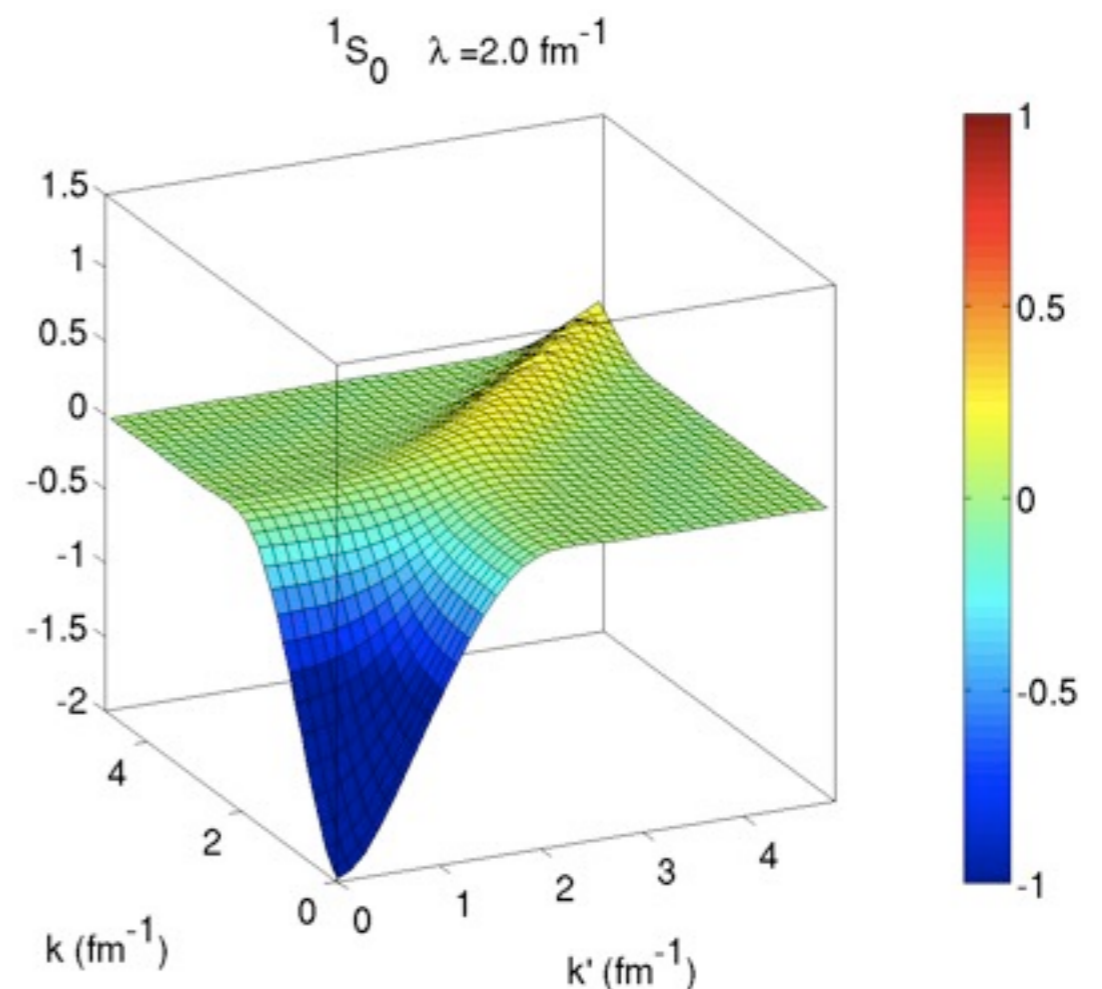
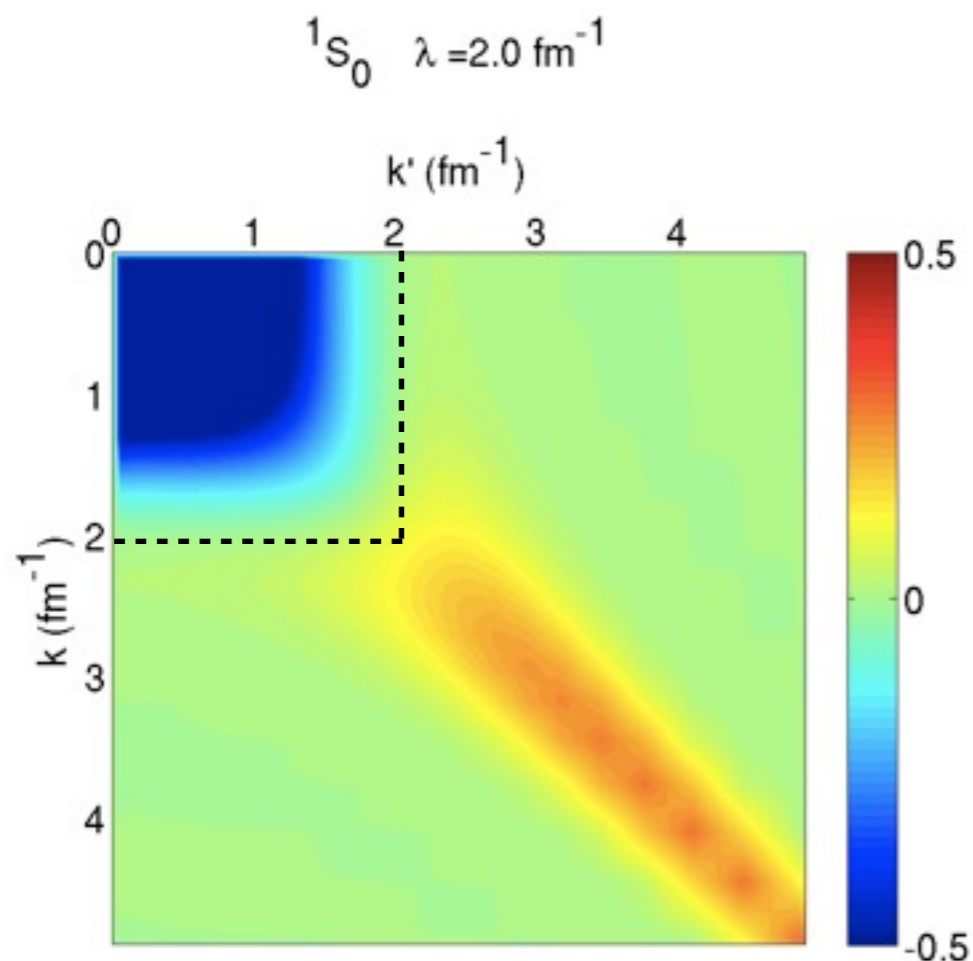


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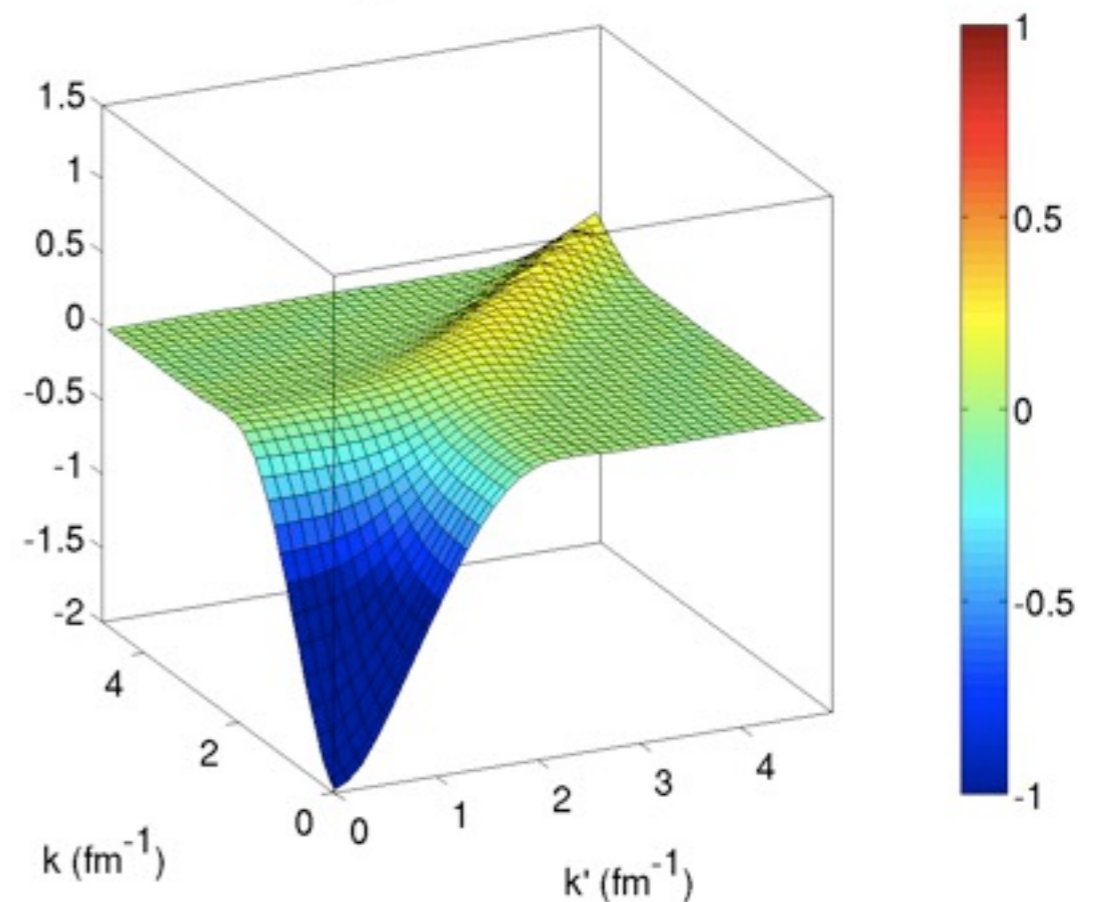
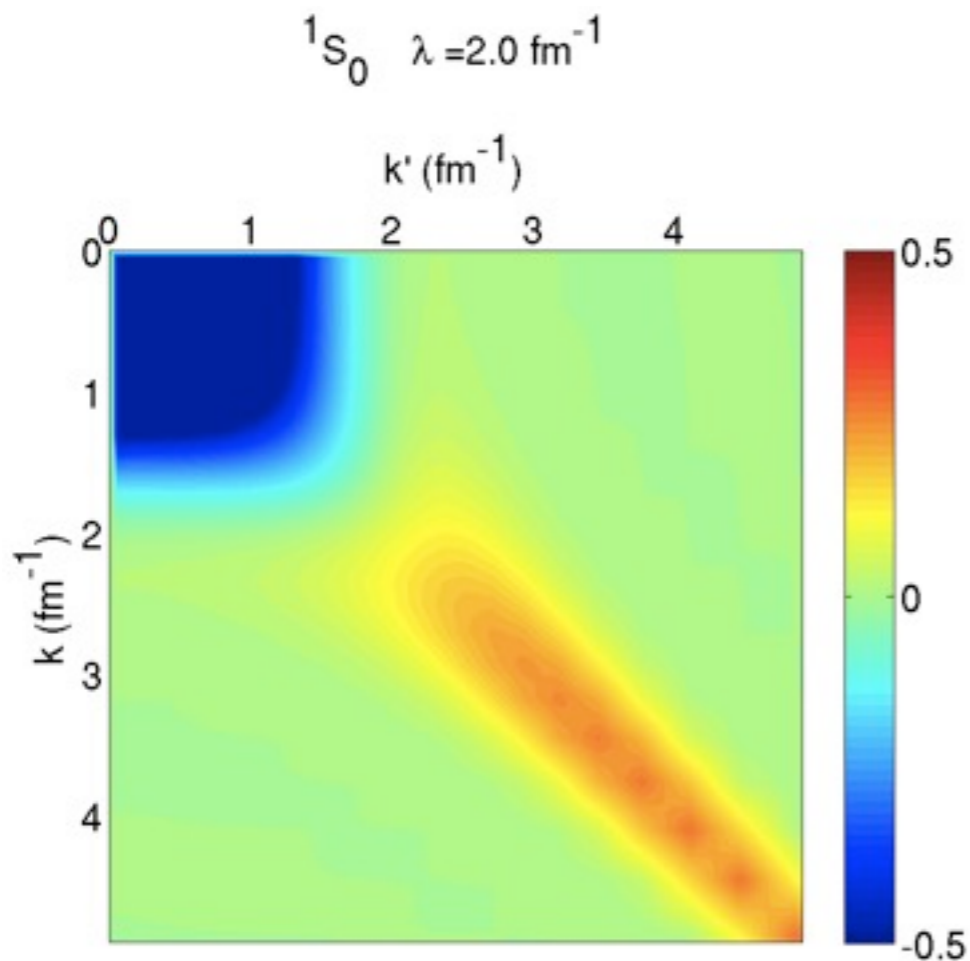
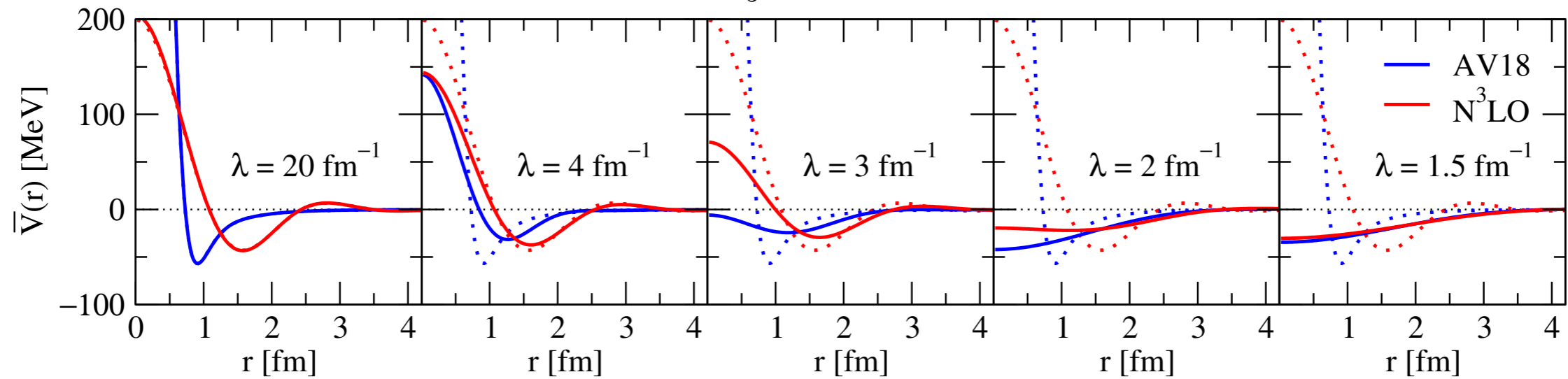
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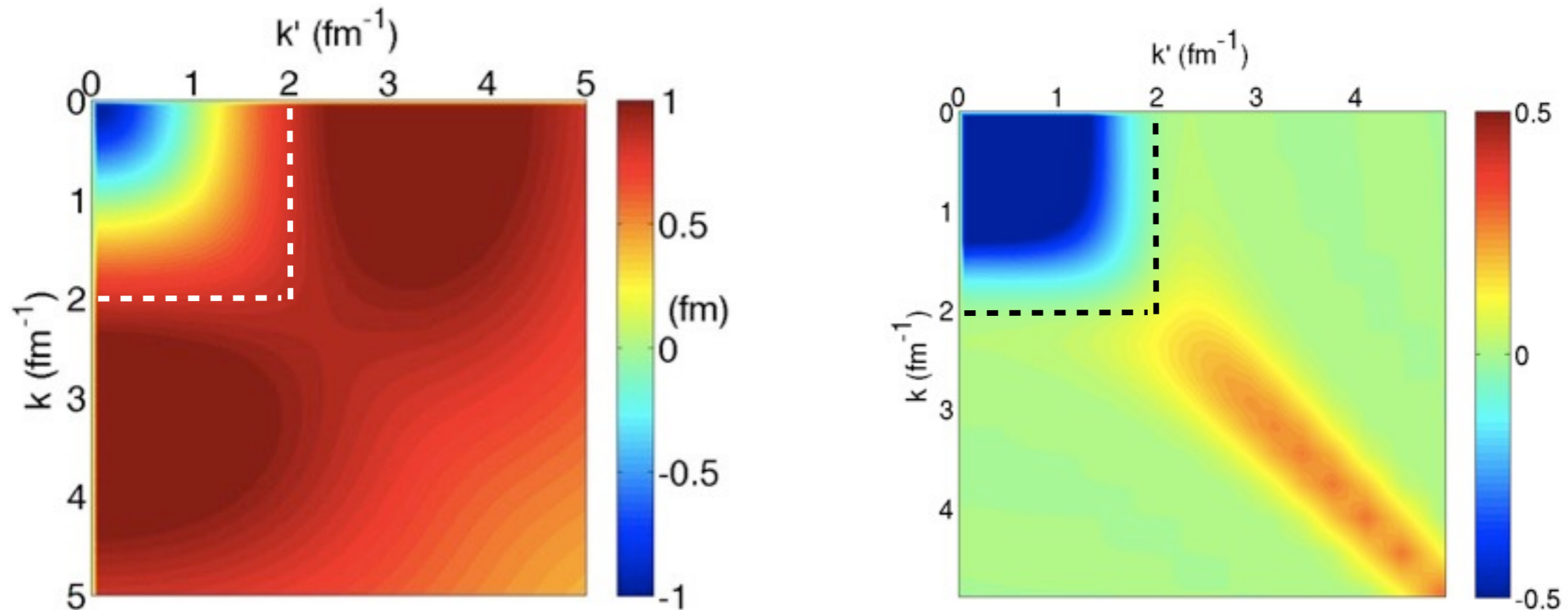


Systematic decoupling of high-momentum physics: The Similarity Renormalization Group

$$\bar{V}_\lambda(r) = \int dr' r'^2 V_\lambda(r, r')$$



Systematic decoupling of high-momentum physics: The Similarity Renormalization Group

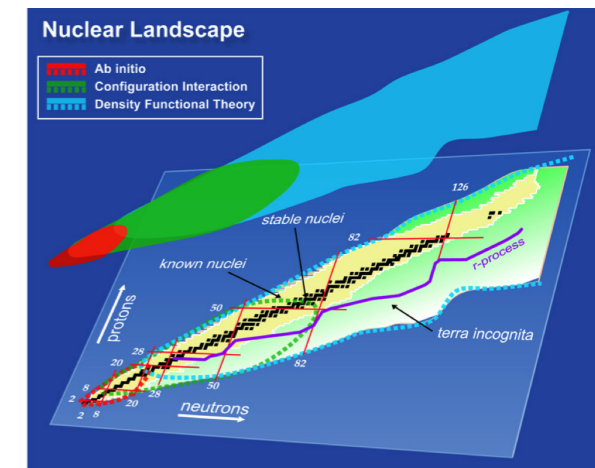
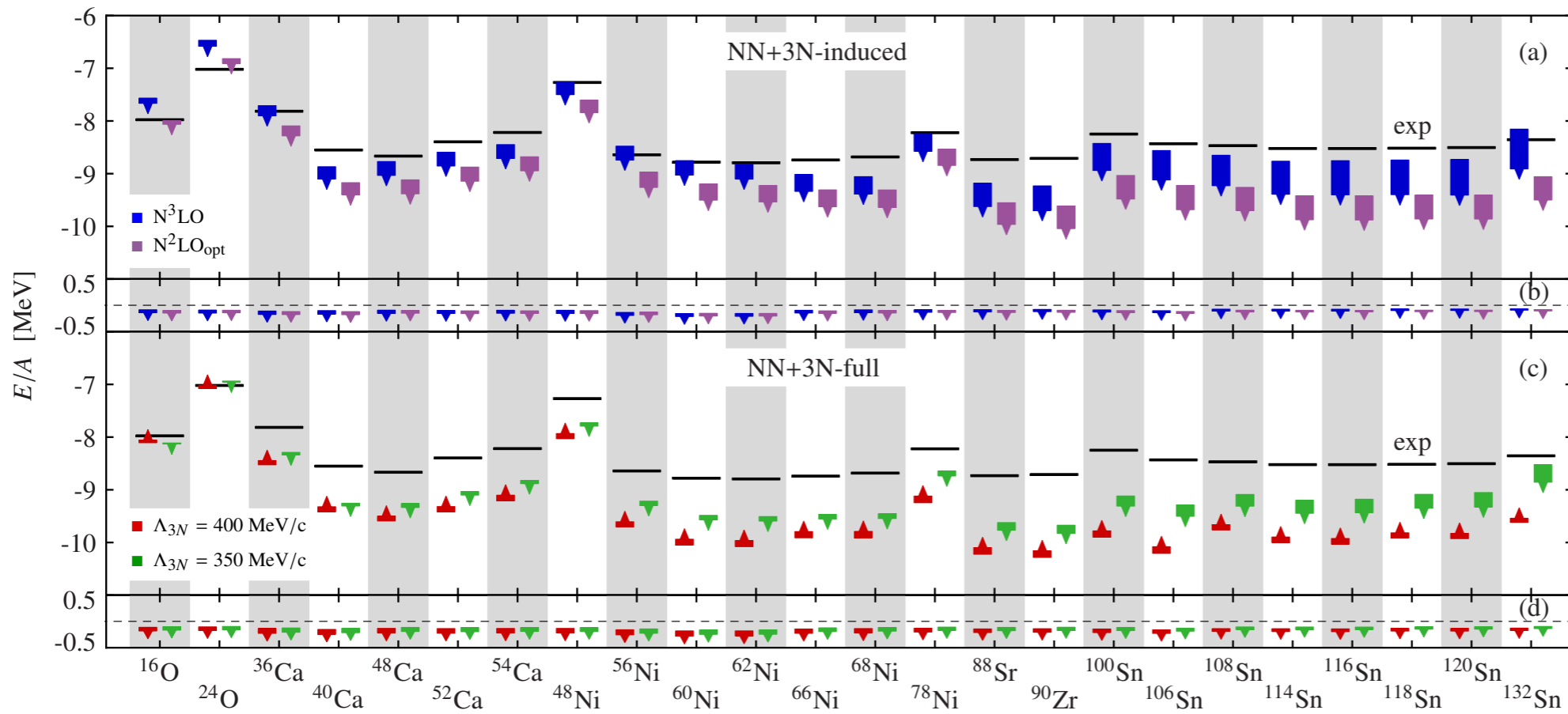


- elimination of coupling between low- and high momentum components,
→ simplified many-body calculations, smaller required model spaces
- observables unaffected by resolution change (for exact calculations)
- residual resolution dependences can be used as tool to test calculations

Not the full story:

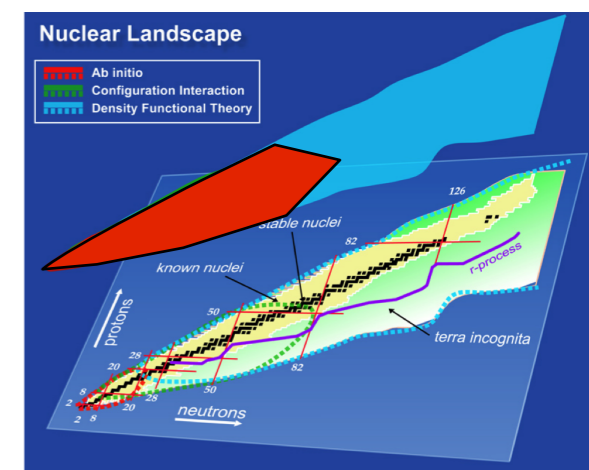
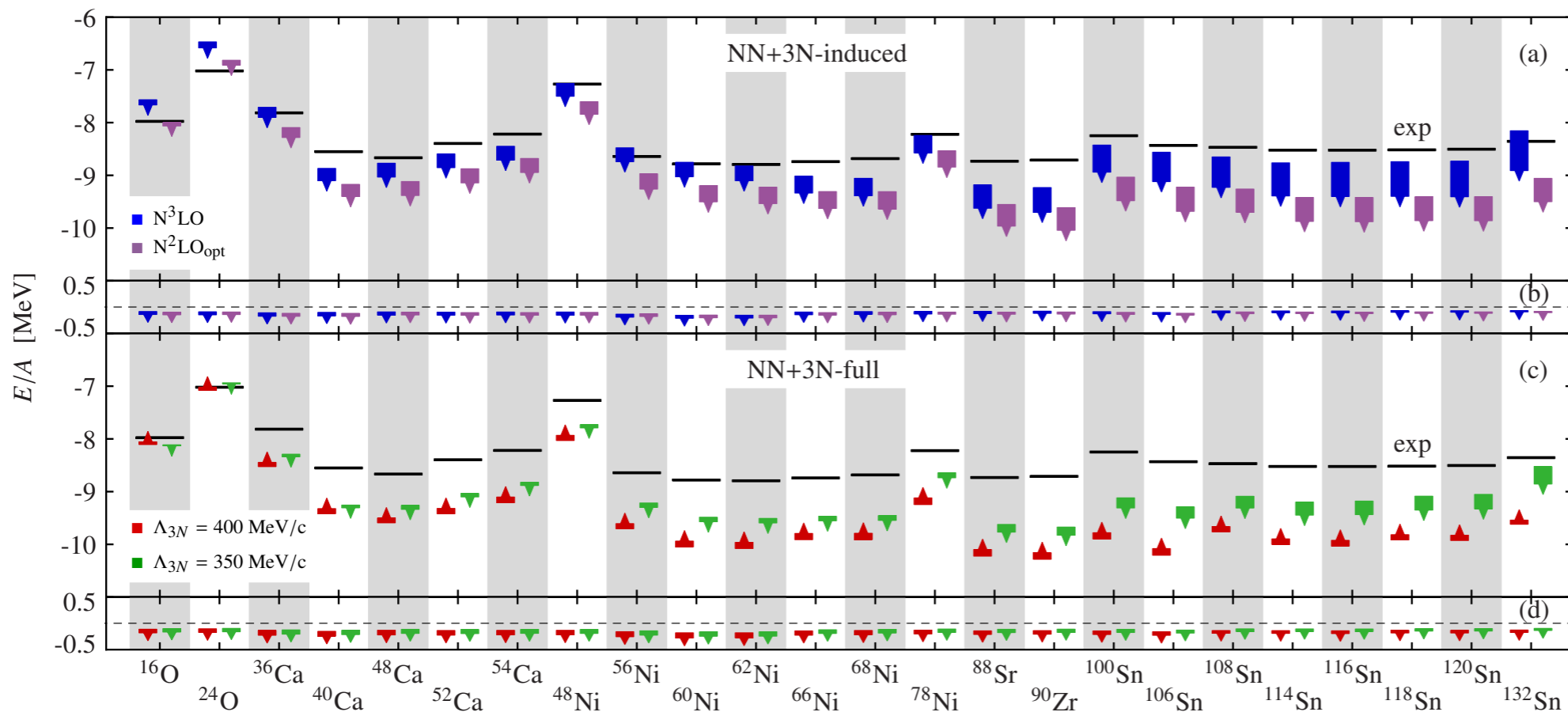
RG transformation also changes **three-body** (and higher-body) interactions.

Recent advances in ab-initio many-body theory

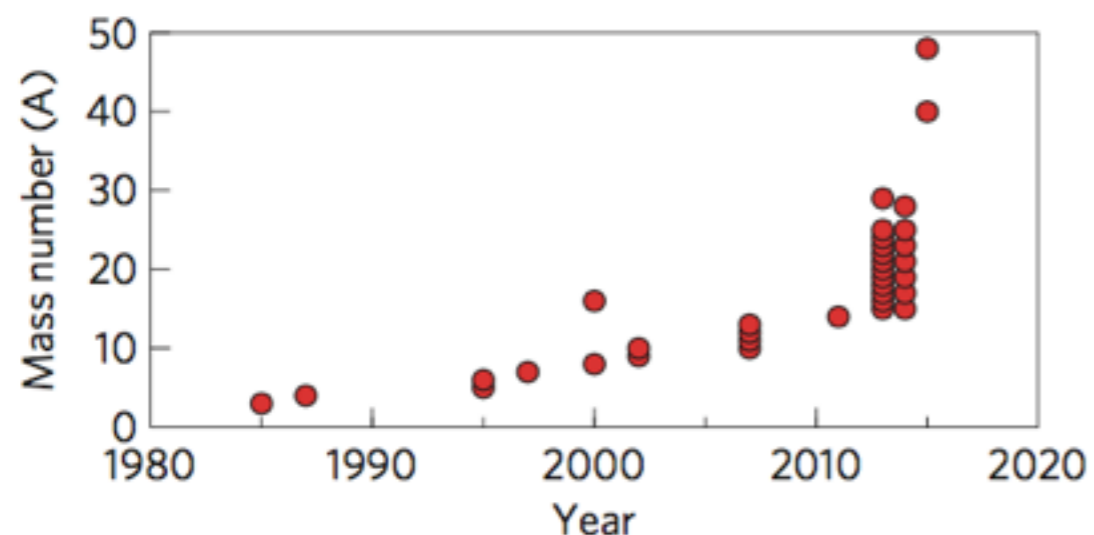


Binder et al., Phys. Lett B 736, 119 (2014)

Recent advances in ab-initio many-body theory



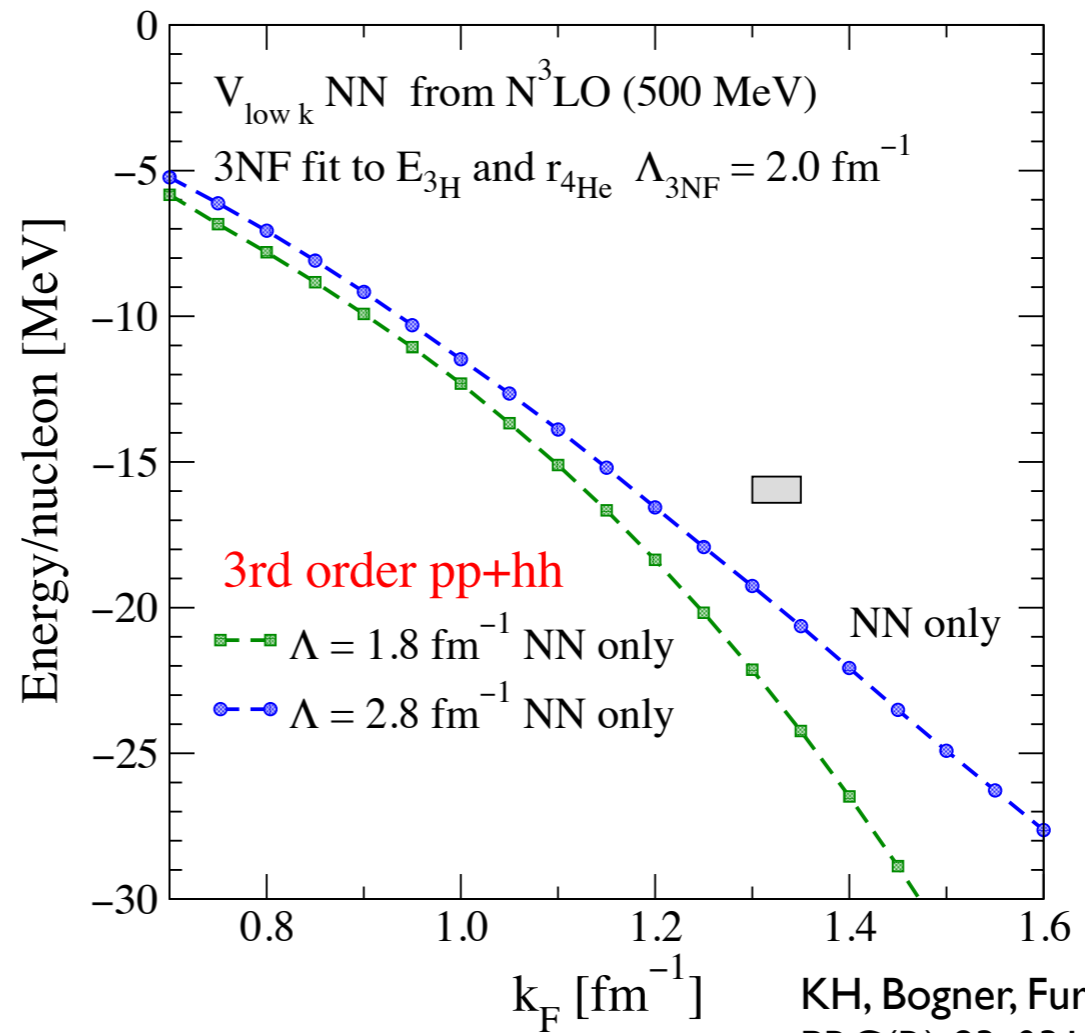
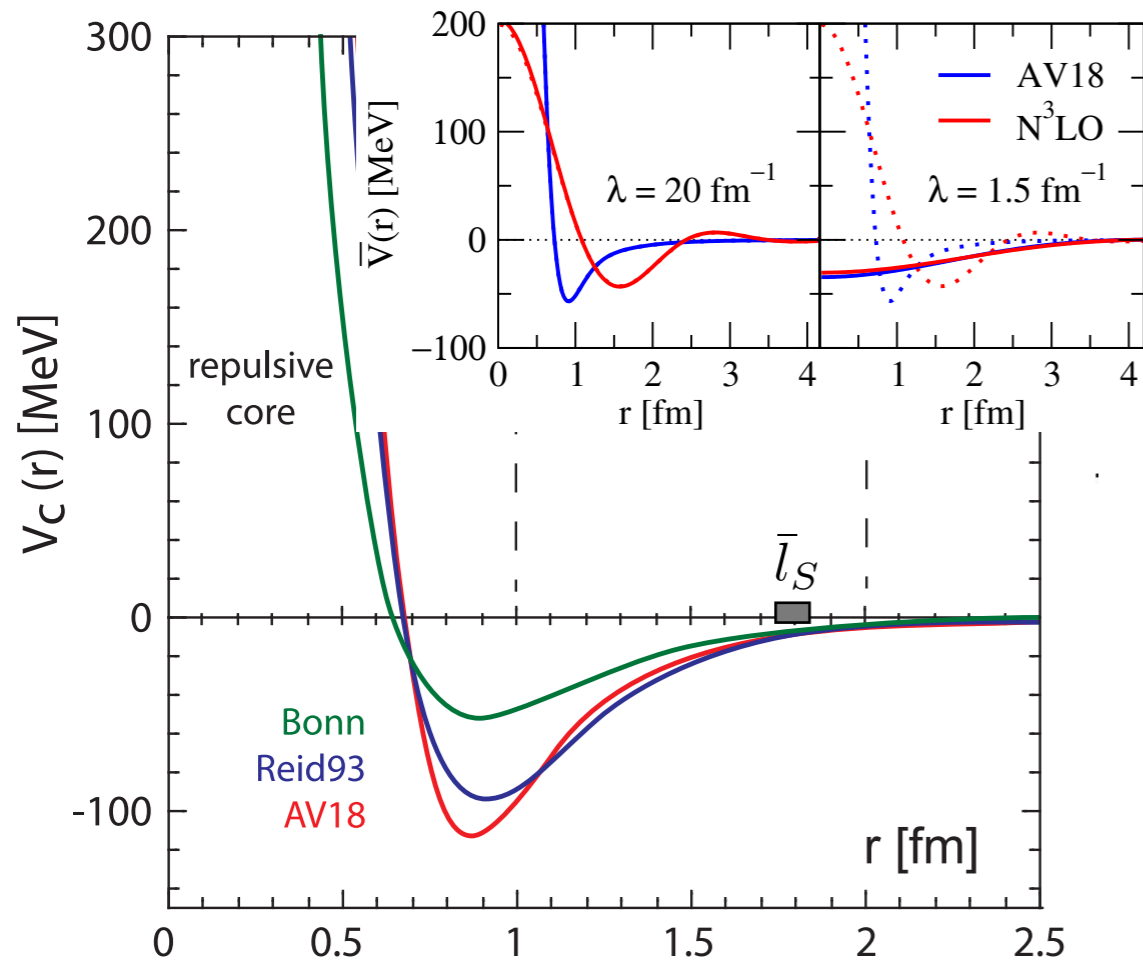
Binder et al., Phys. Lett B 736, 119 (2014)



Hagen et al., Nature Physics 12, 186 (2016)

- **spectacular increase** in range of applicability of *ab initio* many body frameworks
- **significant overbinding** in heavy nuclei for presently used nuclear interactions

Fitting the 3NF LECs at low resolution scales



	2N basis	3N basis	4N basis
LO $\phi(\vec{p})$	X H	-	-
NLO $\phi(\vec{p})$	X H H	-	-
NLO $\phi(\vec{p})$	H H	H H	-
NLO $\phi(\vec{p})$	X H H	X H H	H H

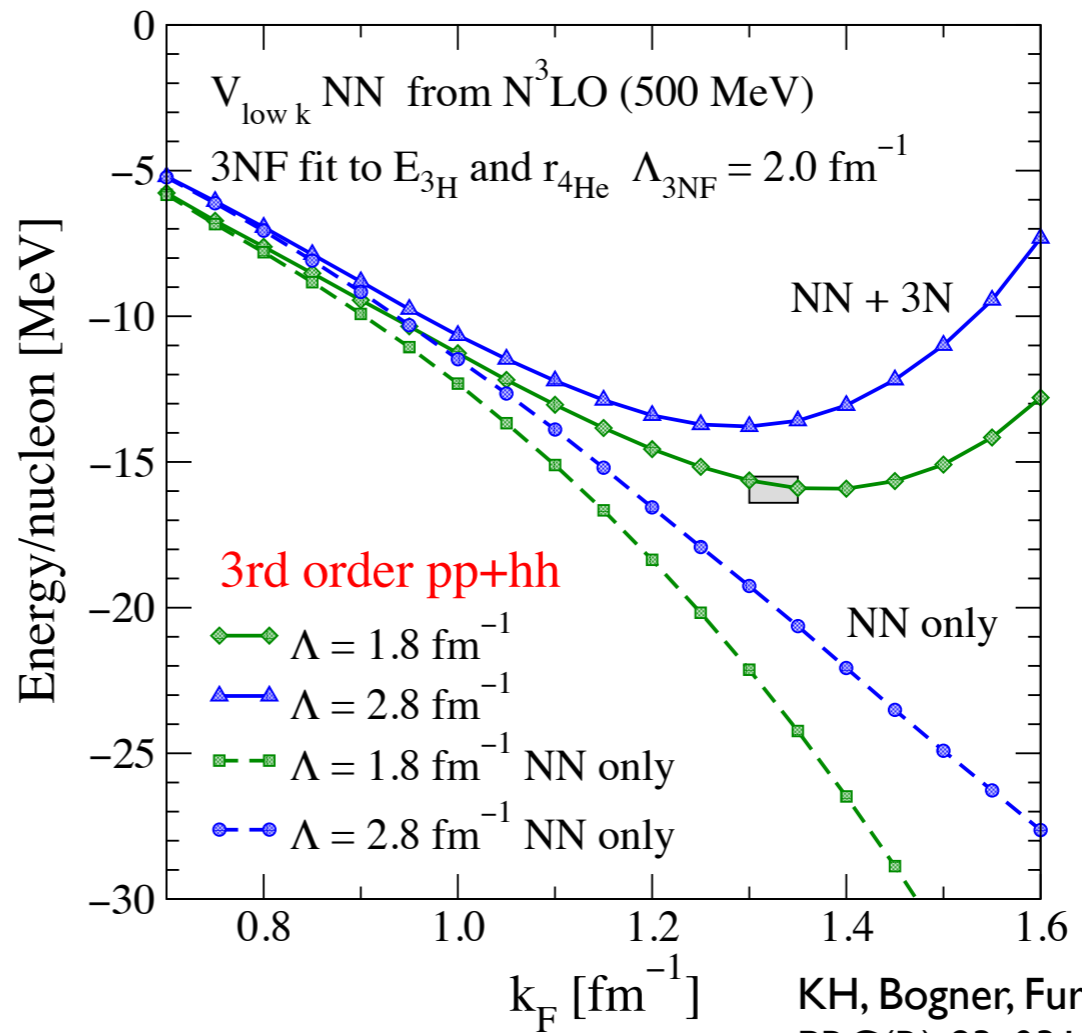
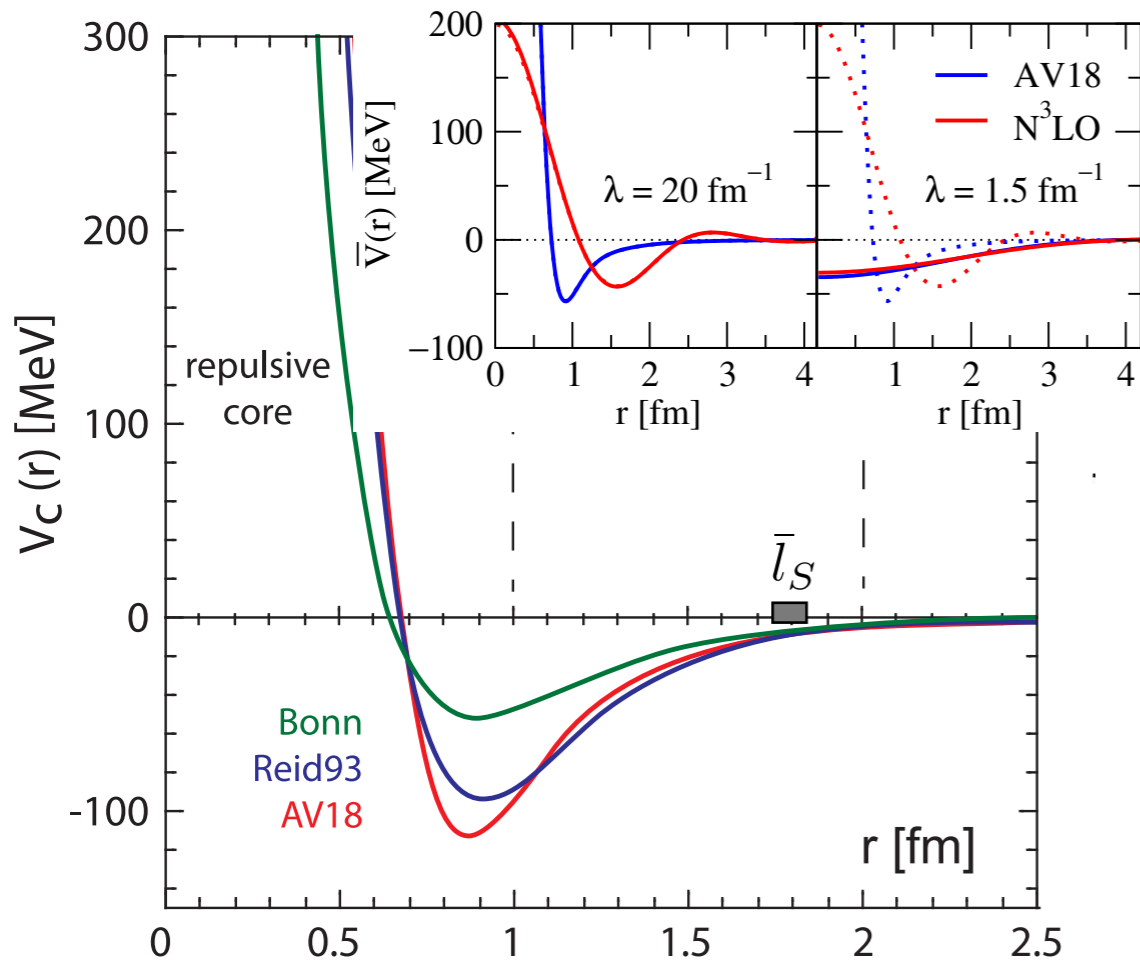
KH, Bogner, Furnstahl, Nogga, PRC(R) 83, 031301 (2011)



“Very soft potentials must be excluded because they do not give saturation; they give too much binding and too high density. In particular, a substantial tensor force is required.”

Hans Bethe (1971)

Fitting the 3NF LECs at low resolution scales



	0h basis	0h basis	0h basis
LO $\phi(\mathbb{F})$	X H	-	-
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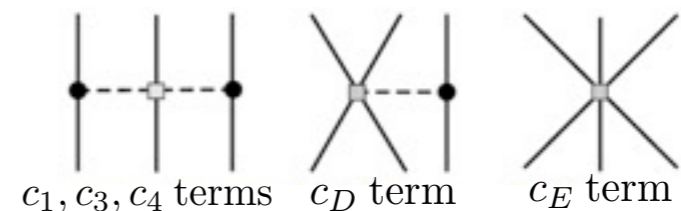


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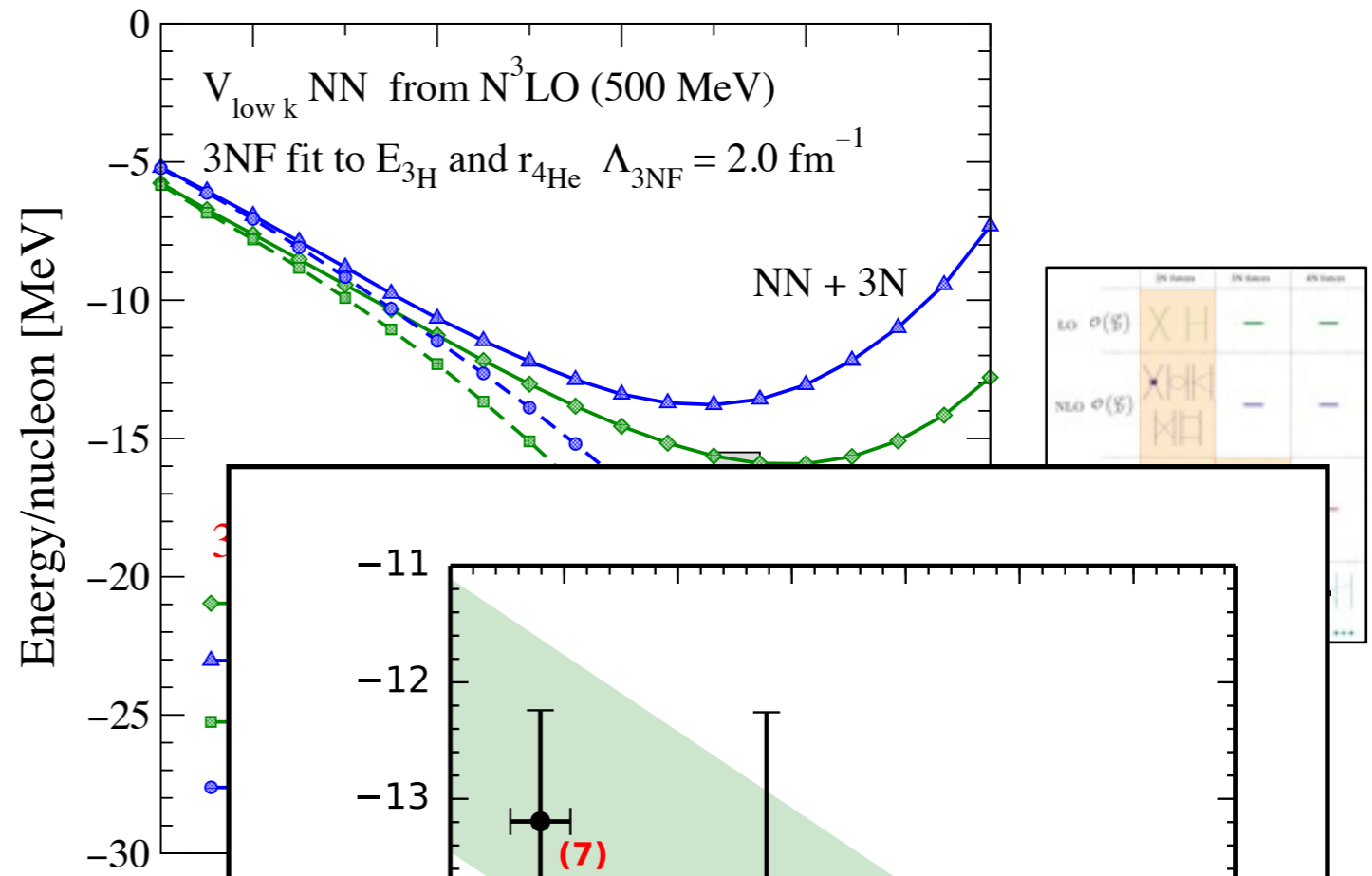
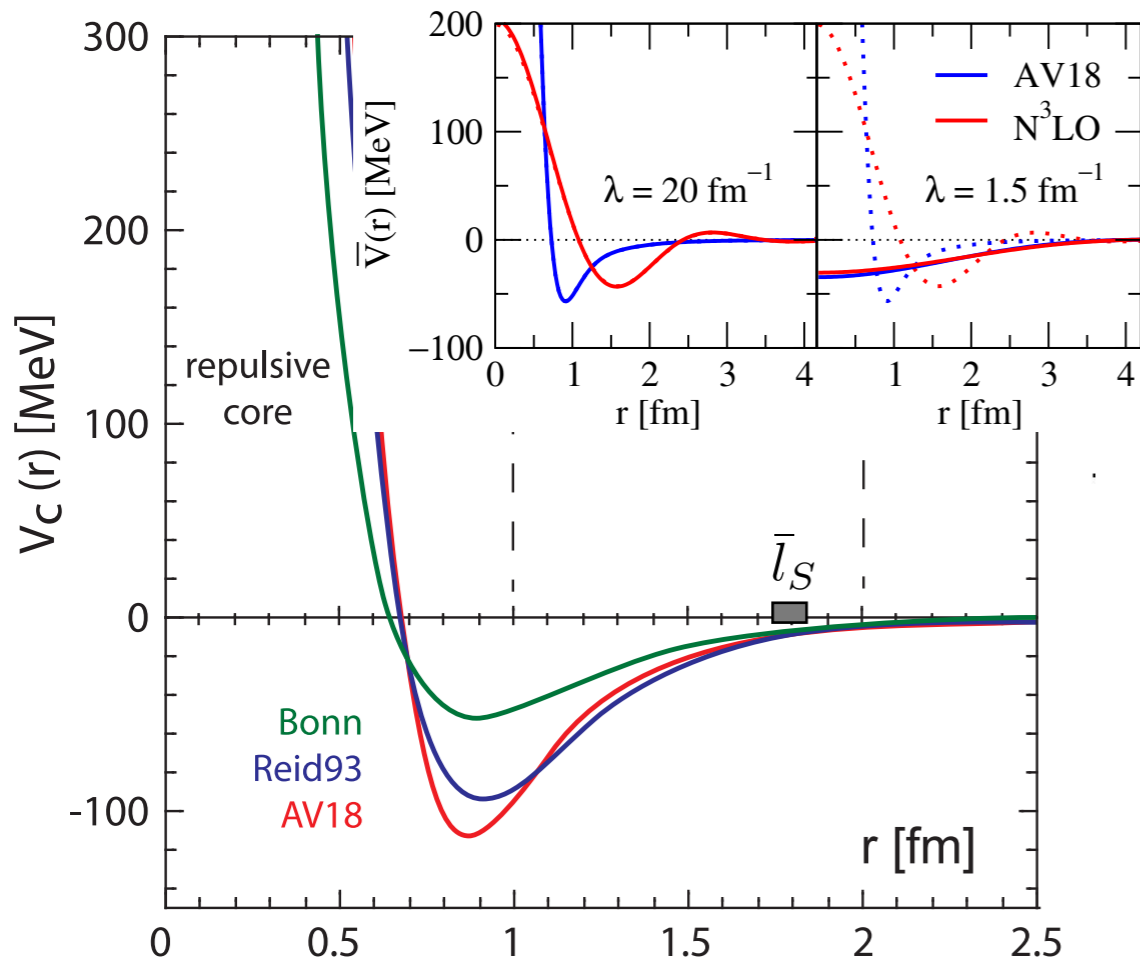
Hans Bethe (1971)

intermediate (c_D) and short-range (c_E) 3NF couplings fitted to few-body systems at different resolution scales:

$$E_{3H} = -8.482 \text{ MeV} \quad r_{4He} = 1.464 \text{ fm}$$

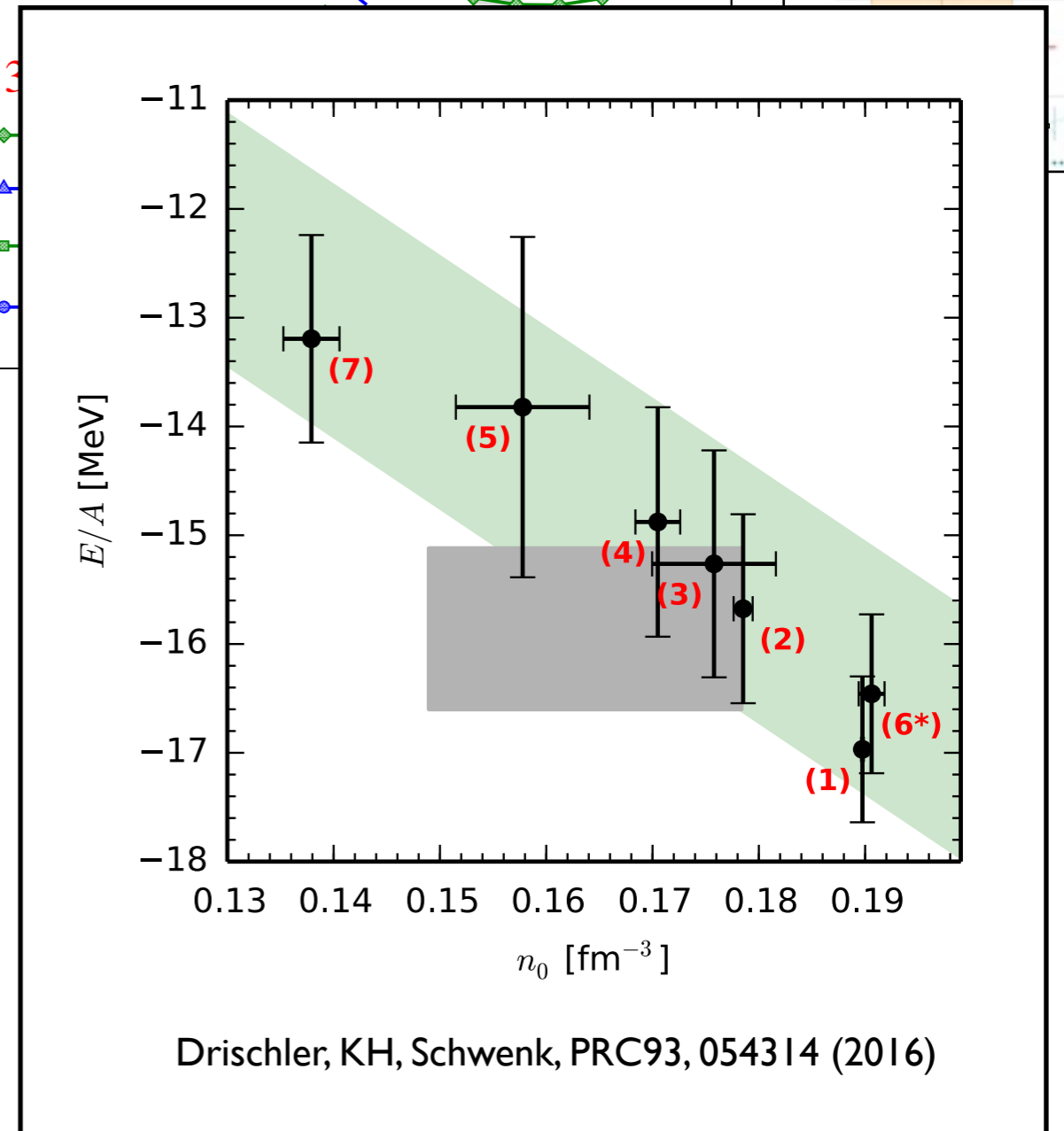


Fitting the 3NF LECs at low resolution scales

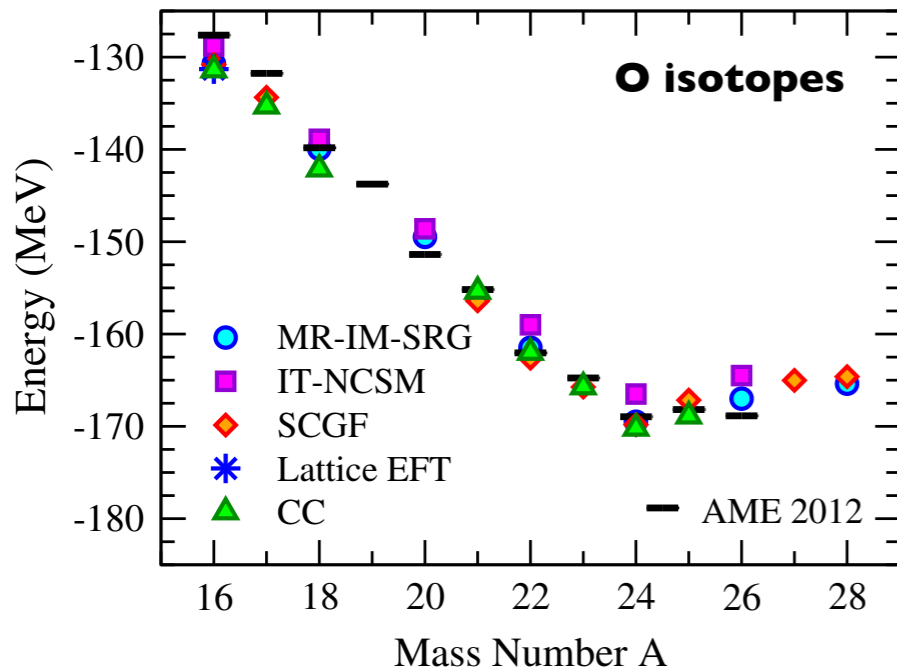
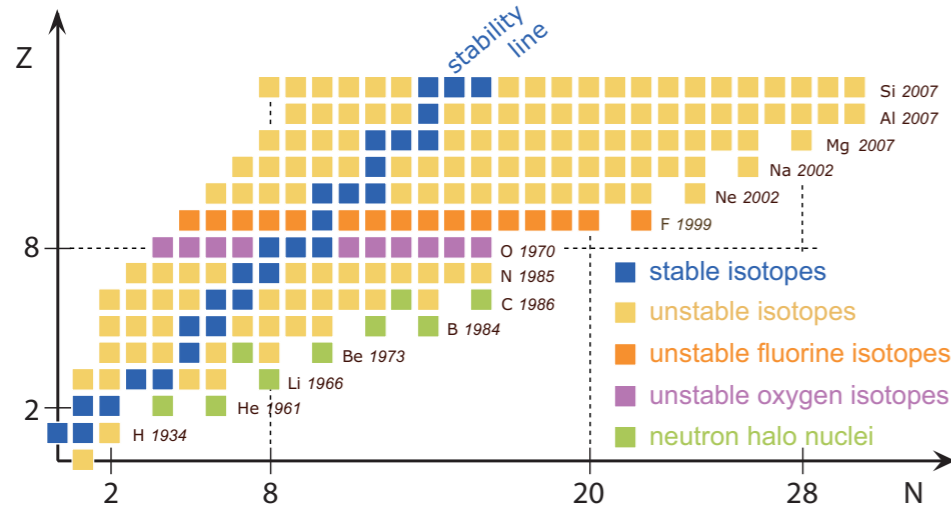


“Very soft potentials must be excluded because they do not give saturation; they give too much binding and too high density. In particular, a substantial tensor force is required.”

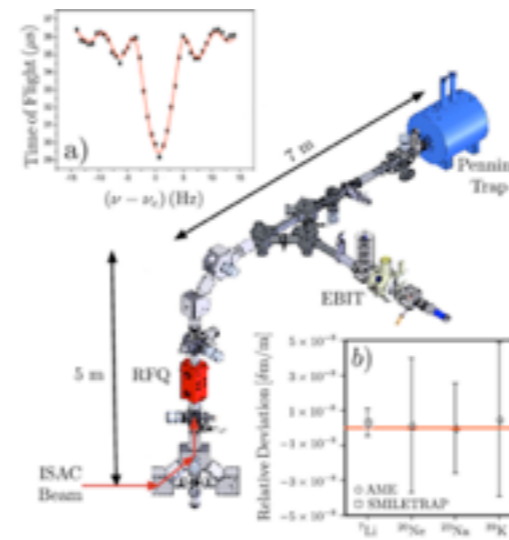
Hans Bethe (1971)



Studies of neutron-rich nuclei

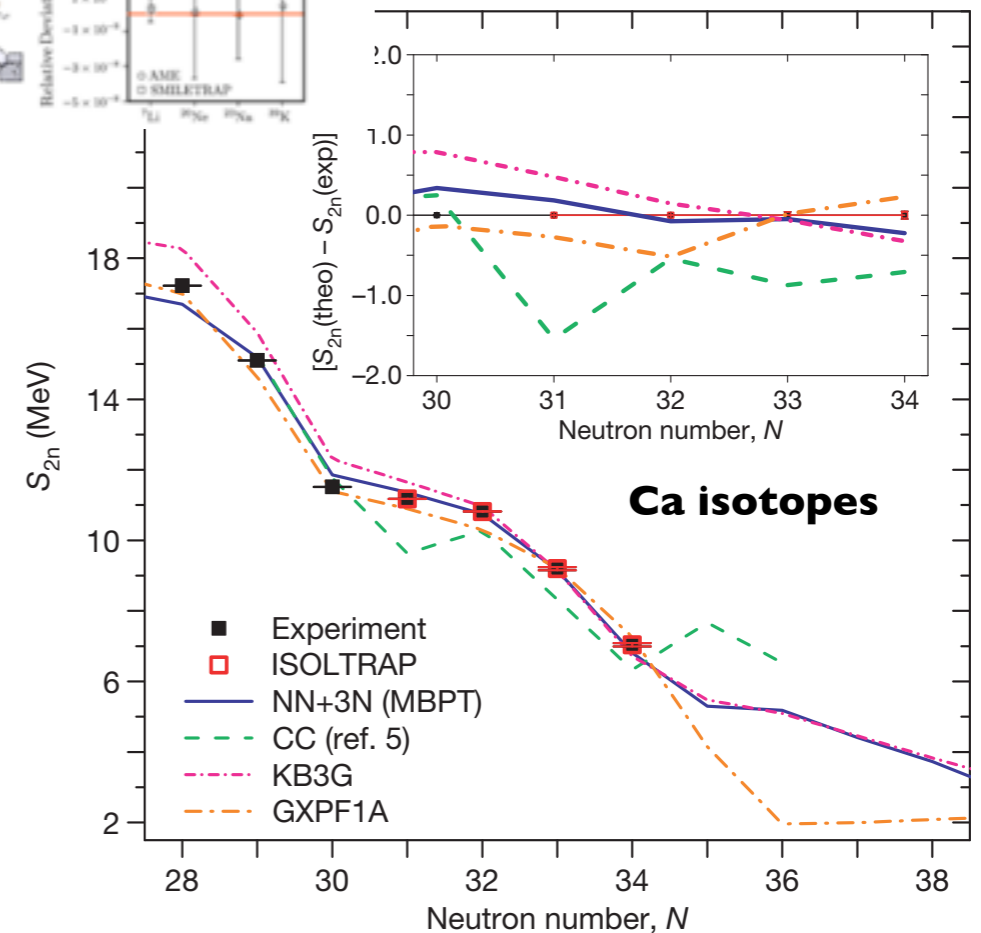


KH et al., Ann. Rev. Nucl. Part. Sci. 165, 457 (2015)



Gallant et al.
PRL 109, 032506 (2012)

Wienholtz et al.
Nature 498, 346 (2013)

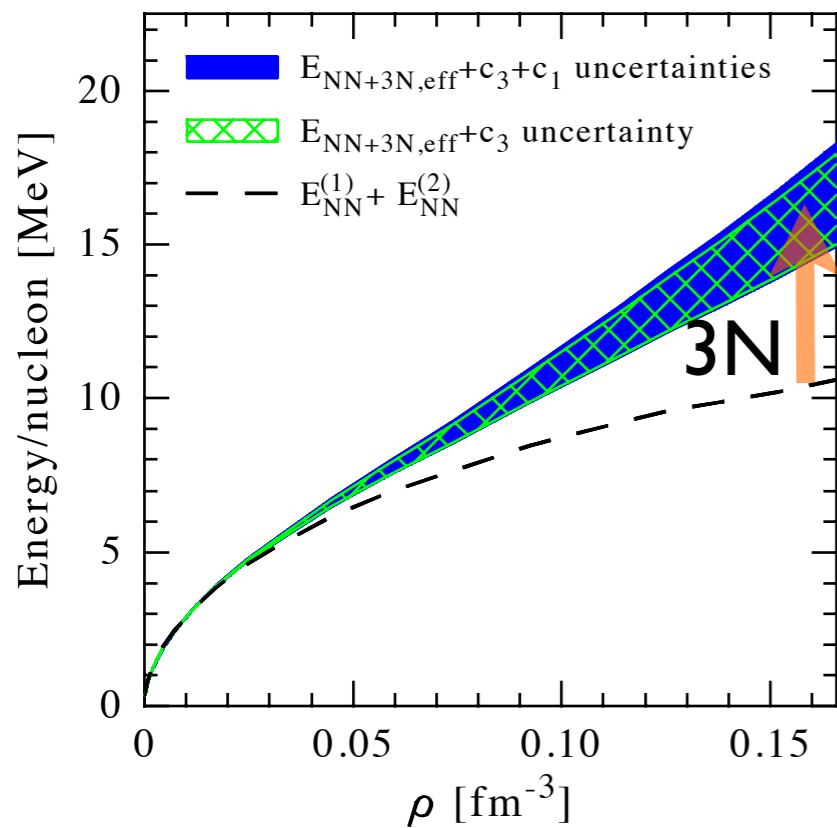
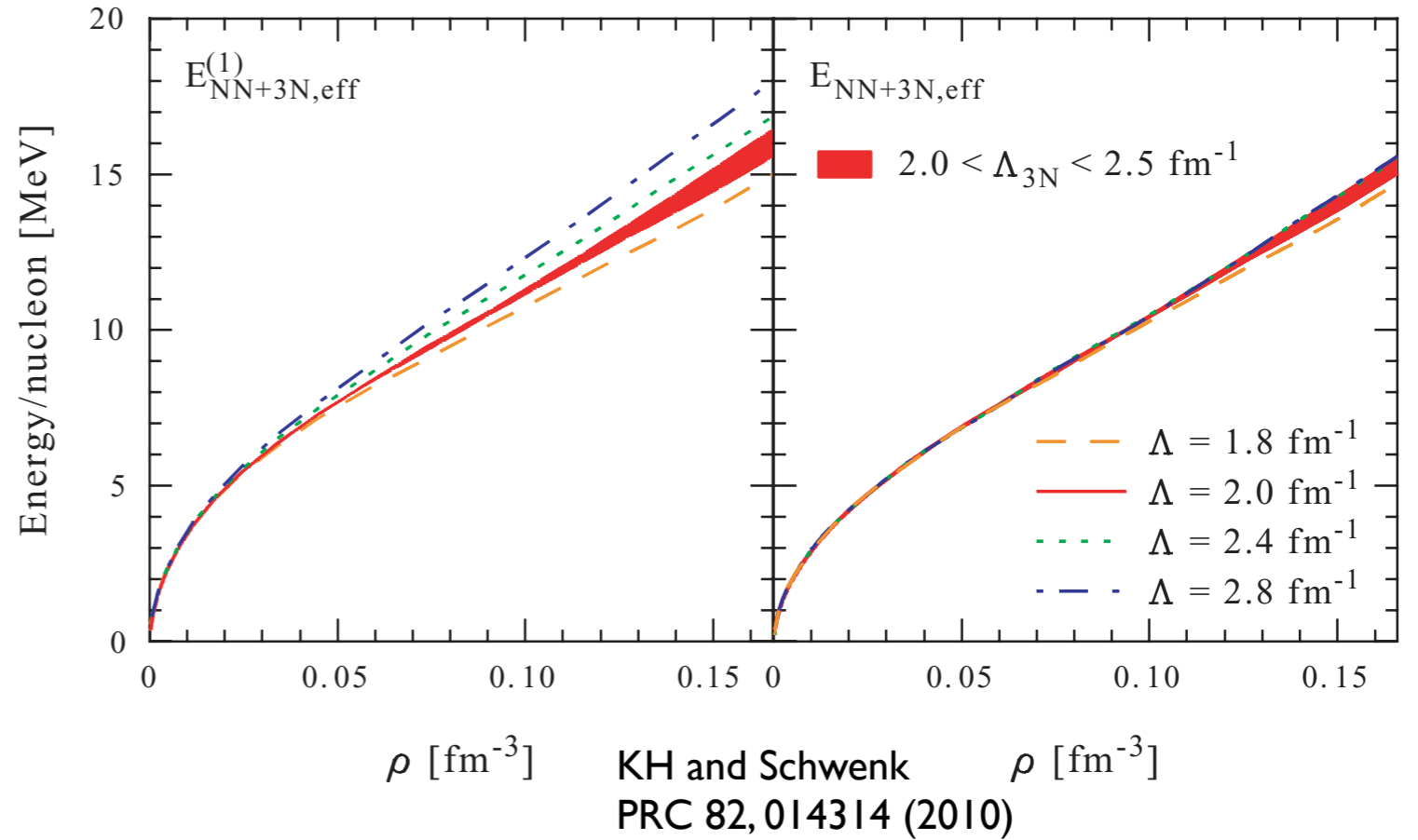
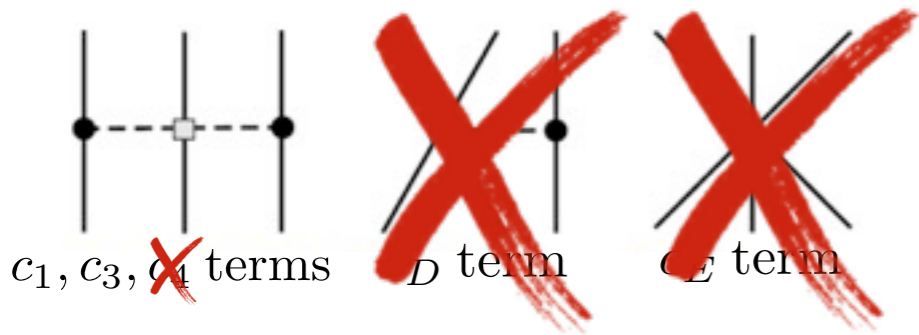


- remarkable agreement between different many-body frameworks
- excellent agreement between theory and experiment for masses of oxygen and calcium isotopes based on specific chiral interactions
- need to quantify **theoretical uncertainties**

Results for the neutron matter equation of state

neutron matter is a **unique system** for chiral EFT:

only long-range 3NF contribute in leading order



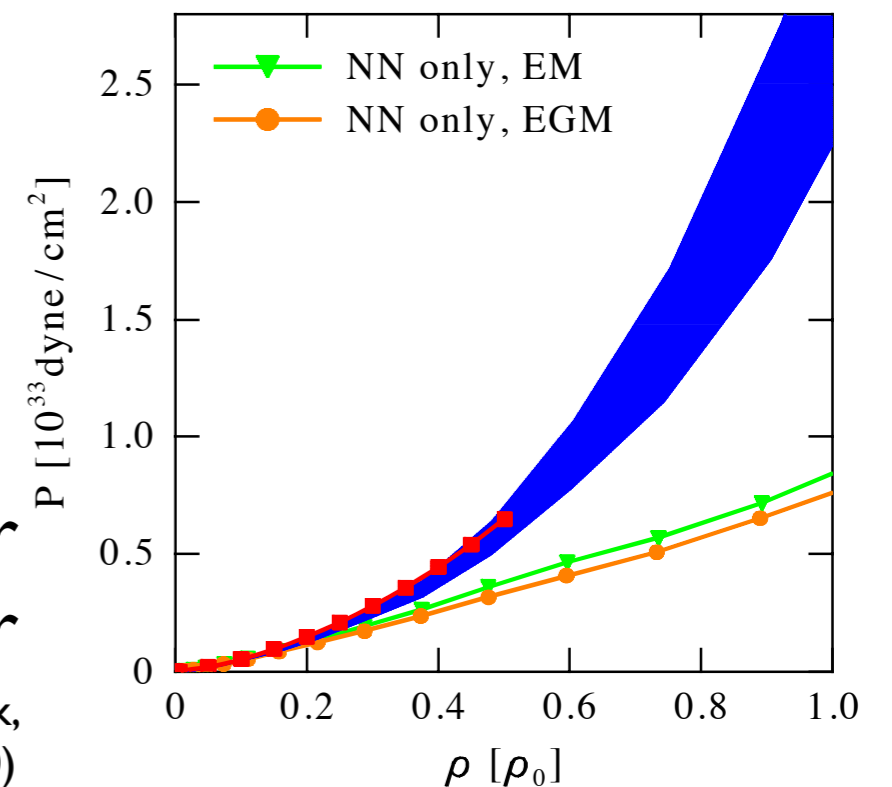
pure neutron matter

KH and Schwenk PRC 82, 014314 (2010)

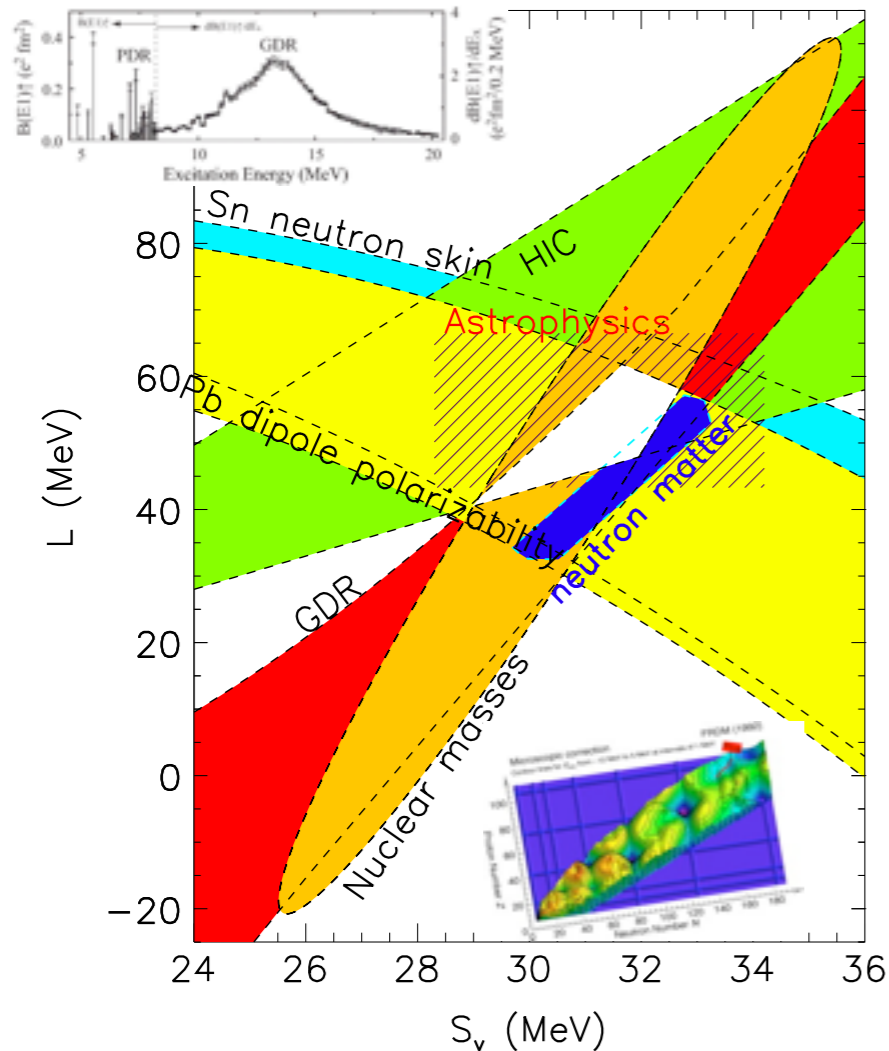
	2N forces	2N forces	2N forces
LO $\mathcal{O}(\frac{1}{\Lambda^0})$	X H	-	-
NLO $\mathcal{O}(\frac{1}{\Lambda^2})$	X H H	-	-
N ² LO $\mathcal{O}(\frac{1}{\Lambda^4})$	H •	•	-
N ³ LO $\mathcal{O}(\frac{1}{\Lambda^6})$	X H H H X H H H	X H H H X H H H	•

neutron star matter

KH, Lattimer, Pethick, Schwenk,
 PRL 105, 161102 (2010)



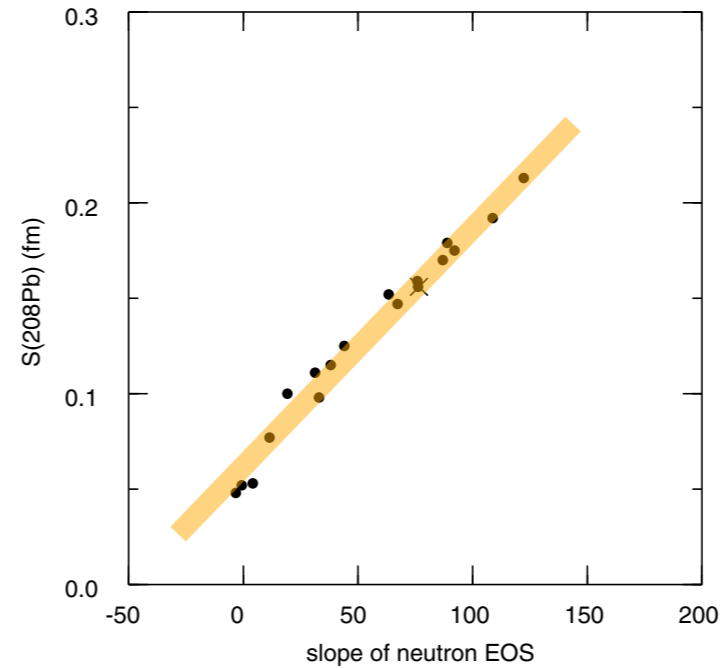
Symmetry energy and neutron skin constraints



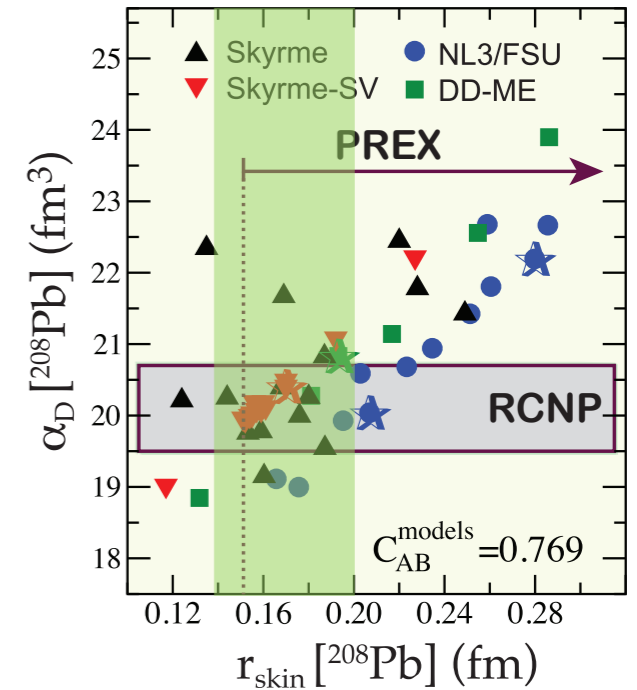
KH, Lattimer, Pethick, Schwenk, ApJ 773,11 (2013)

$$S_v = \left. \frac{\partial^2 E/N}{\partial^2 x} \right|_{\rho=\rho_0, x=1/2}$$

$$L = \frac{3}{8} \left. \frac{\partial^3 E/N}{\partial \rho \partial^2 x} \right|_{\rho=\rho_0, x=1/2}$$



Brown, PRL 85, 5296 (2000)



Piekarewicz, PRC 85, 041302 (2012)

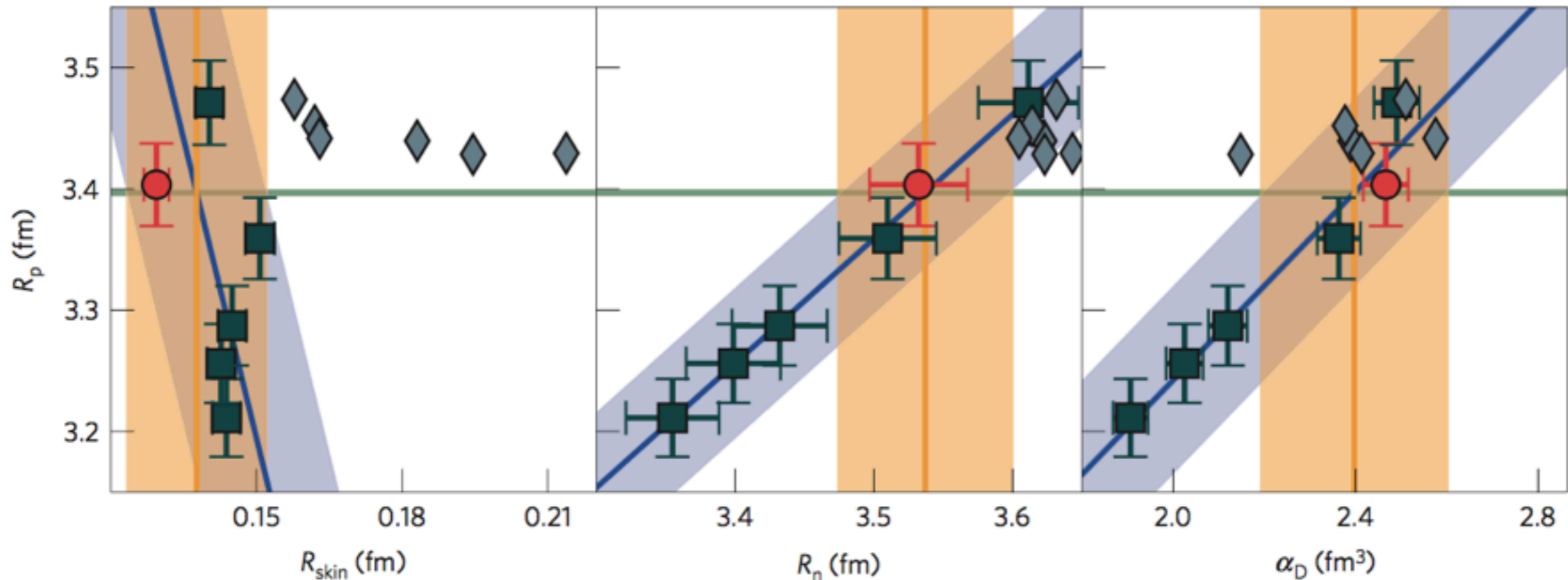
neutron skin constraint from
neutron matter results:

$$r_{\text{skin}} [^{208}\text{Pb}] = 0.14 - 0.2 \text{ fm}$$

KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

- neutron matter give tightest constraints
- in agreement with all other constraints

Predictions for the neutron skin of ^{48}Ca

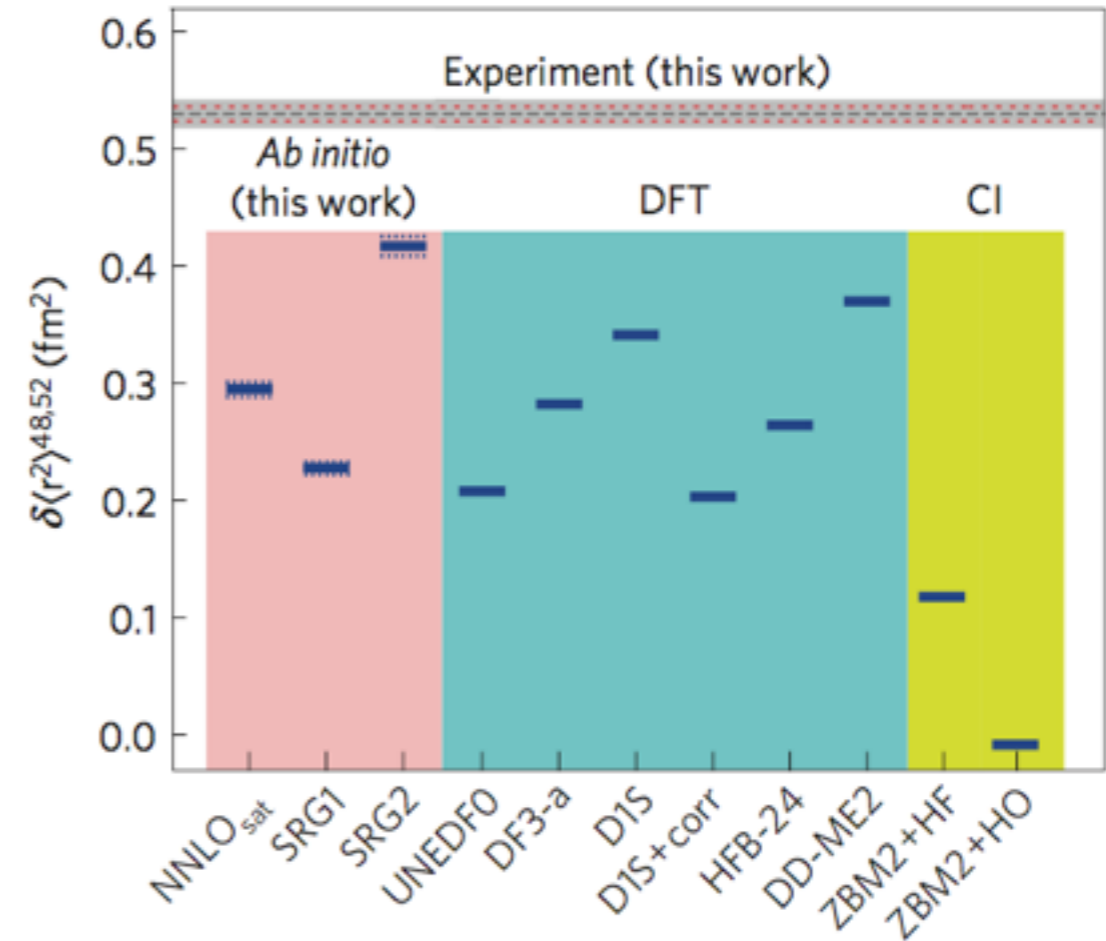
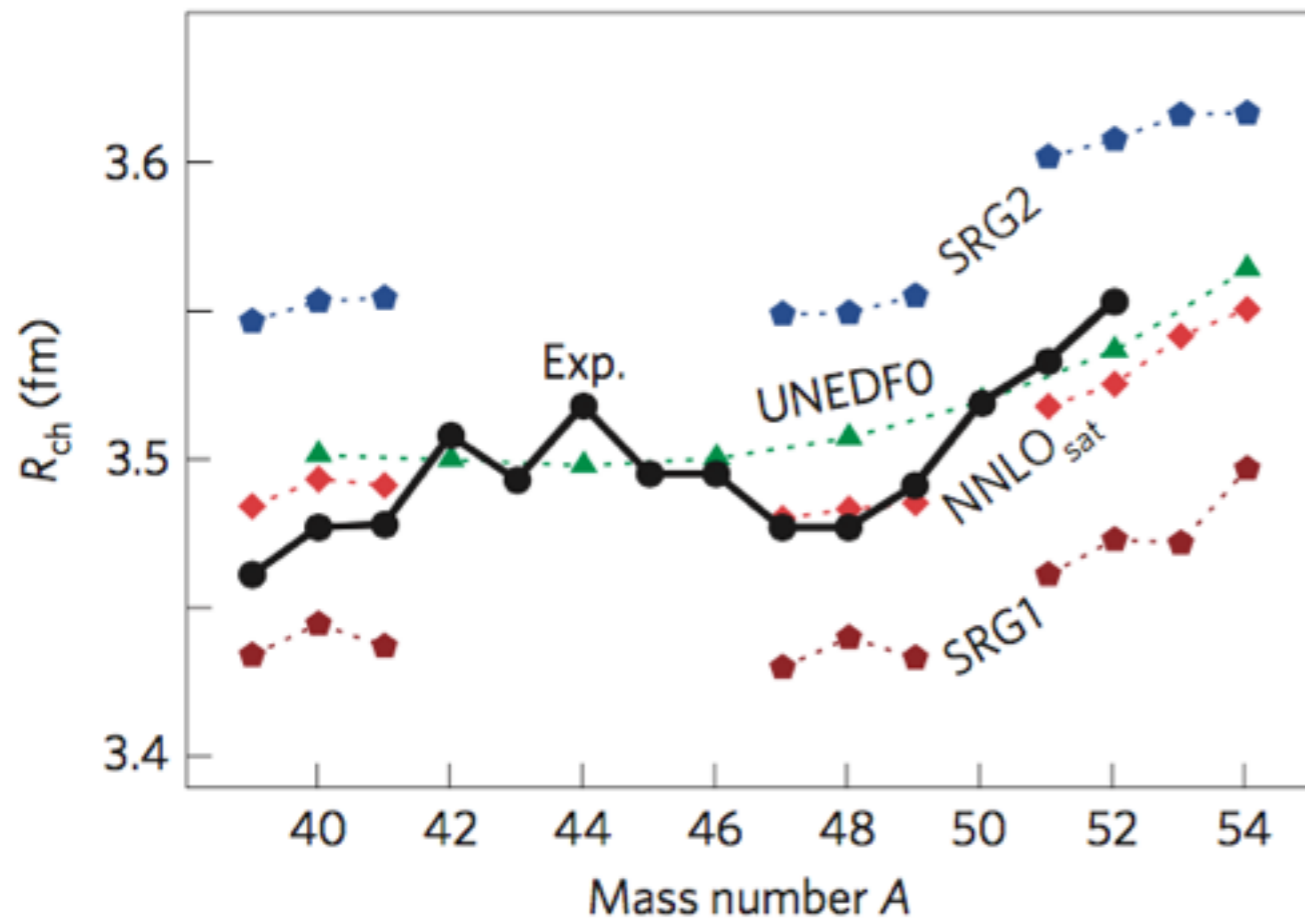


Hagen et al., Nature Physics 12, 186 (2016)

- microscopic coupled cluster results based on a set of different nuclear NN+3N interactions (see also Phys. Rev. C91, 051301 (2015))
- correlations between different observables and the precisely measured R_p
- prediction of significantly **smaller neutron skin** compared to EDF results:

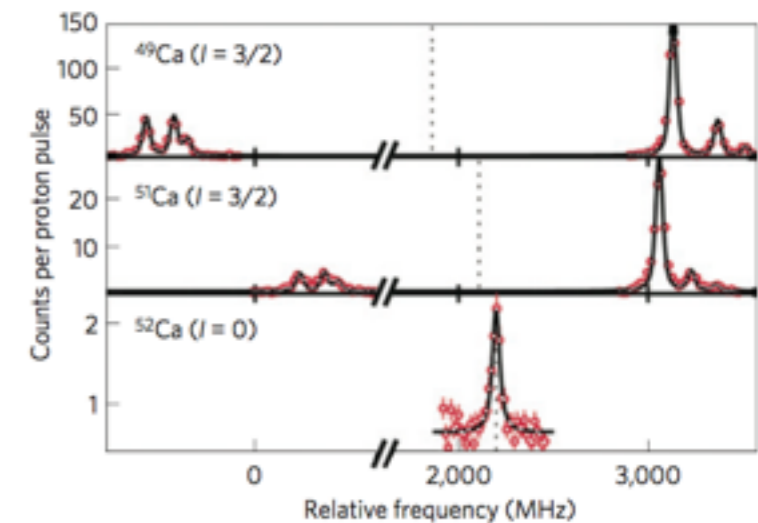
$$0.12 \lesssim R_{\text{skin}} \lesssim 0.15 \text{ fm}$$

Charge radii of calcium isotopes



Garcia Ruiz et al., Nature Physics (advanced online, 2016)

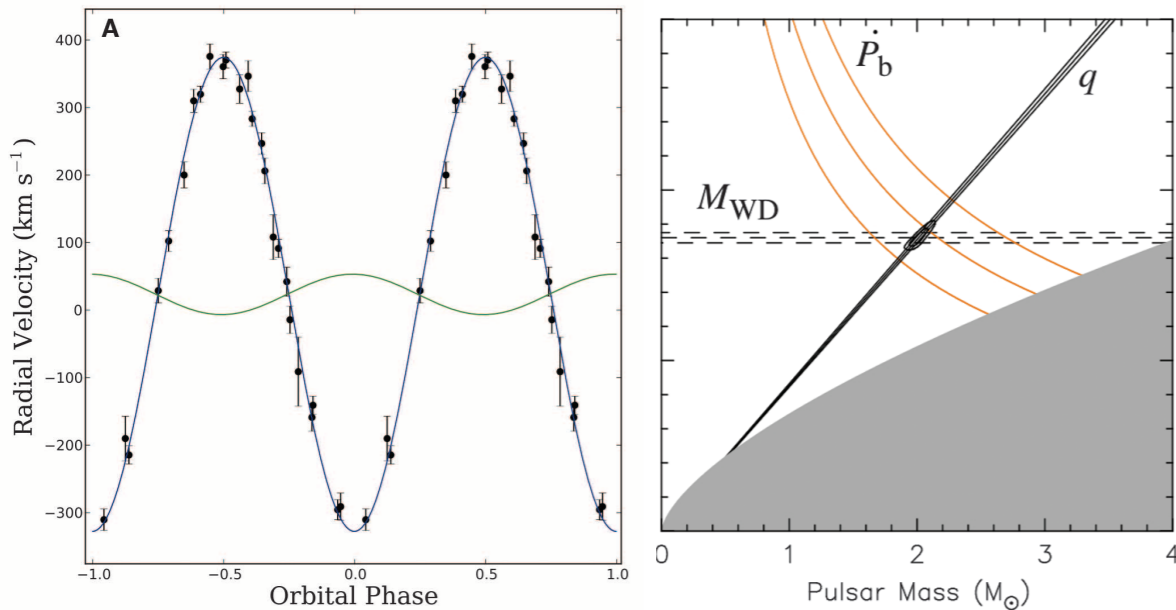
- novel precise measurements of Ca isotope shifts
- **unexpectedly large radii** of neutron-rich isotopes
- reasonable theoretical reproduction of radius trends in coupled cluster calculations based on chiral EFT interactions
- radius increase quantitatively underestimated in all theoretical studies



Constraints on the nuclear equation of state (EOS)

Science

A Massive Pulsar in a Compact Relativistic Binary

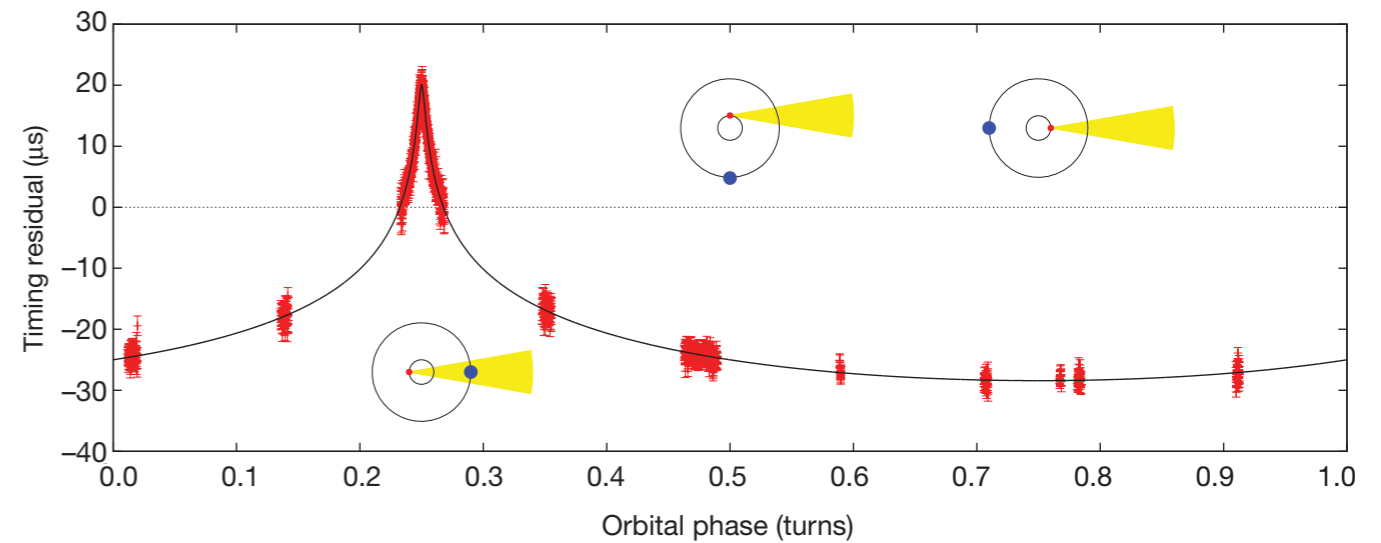


Antoniadis et al., Science 340, 448 (2013)

nature

A two-solar-mass neutron star measured using Shapiro delay

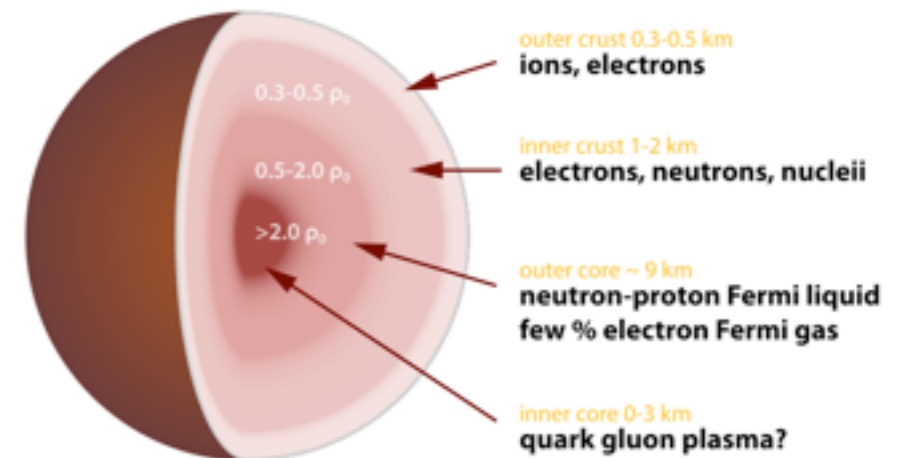
P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}



Demorest et al., Nature 467, 1081 (2010)

New constraints from recent observations:

$$M_{\max} = 1.65M_{\odot} \rightarrow 1.97 \pm 0.04 M_{\odot} \\ \rightarrow 2.01 \pm 0.04 M_{\odot}$$



Calculation of neutron star properties require EOS up to high densities.

Strategy:

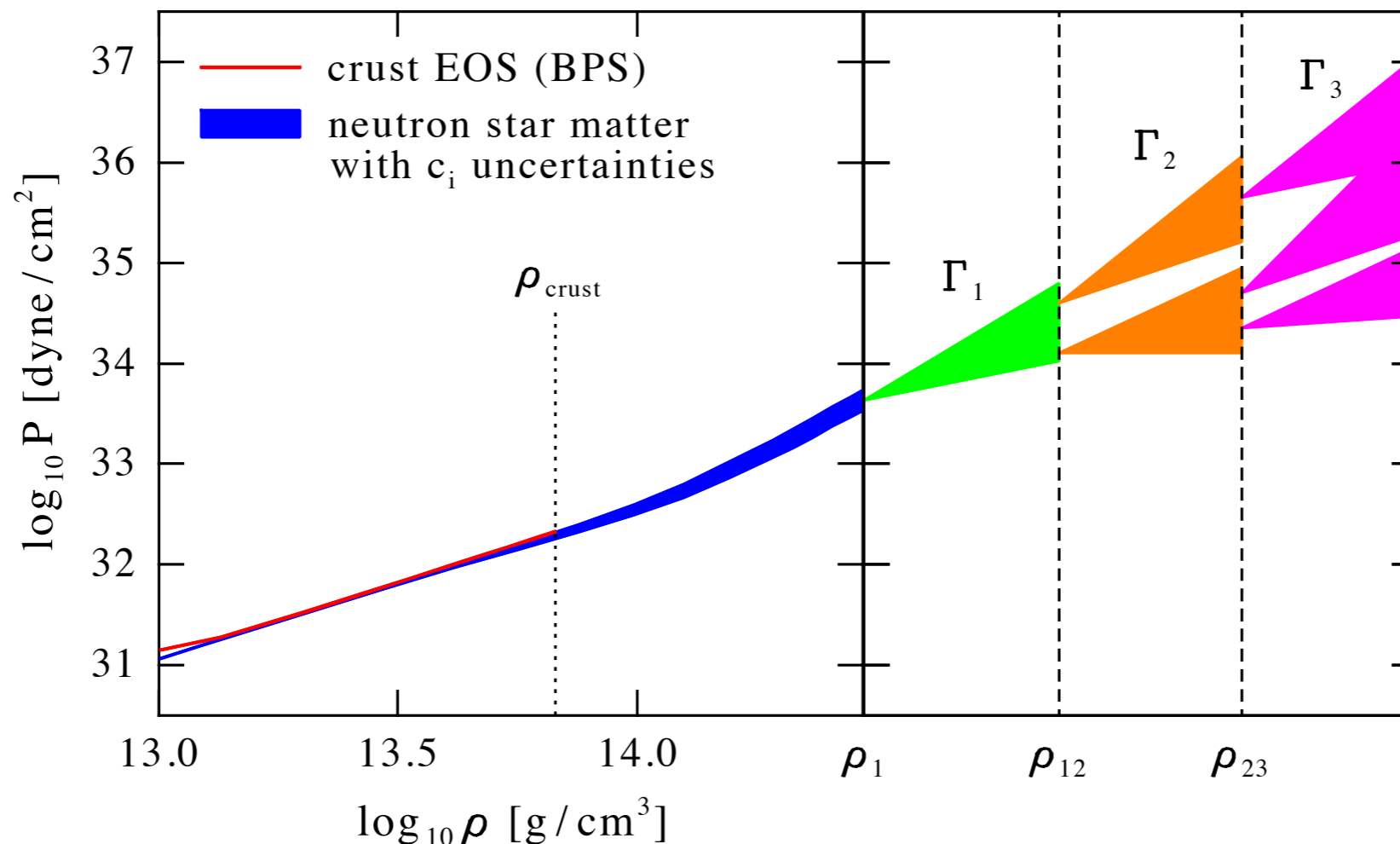
Use observations to constrain the high-density part of the nuclear EOS.

Neutron star radius constraints

incorporation of beta-equilibrium: neutron matter \longrightarrow neutron star matter

parametrize piecewise high-density extensions of EOS:

- use polytropic ansatz $p \sim \rho^\Gamma$
- range of parameters $\Gamma_1, \rho_{12}, \Gamma_2, \rho_{23}, \Gamma_3$ limited by physics



Constraints on the nuclear equation of state

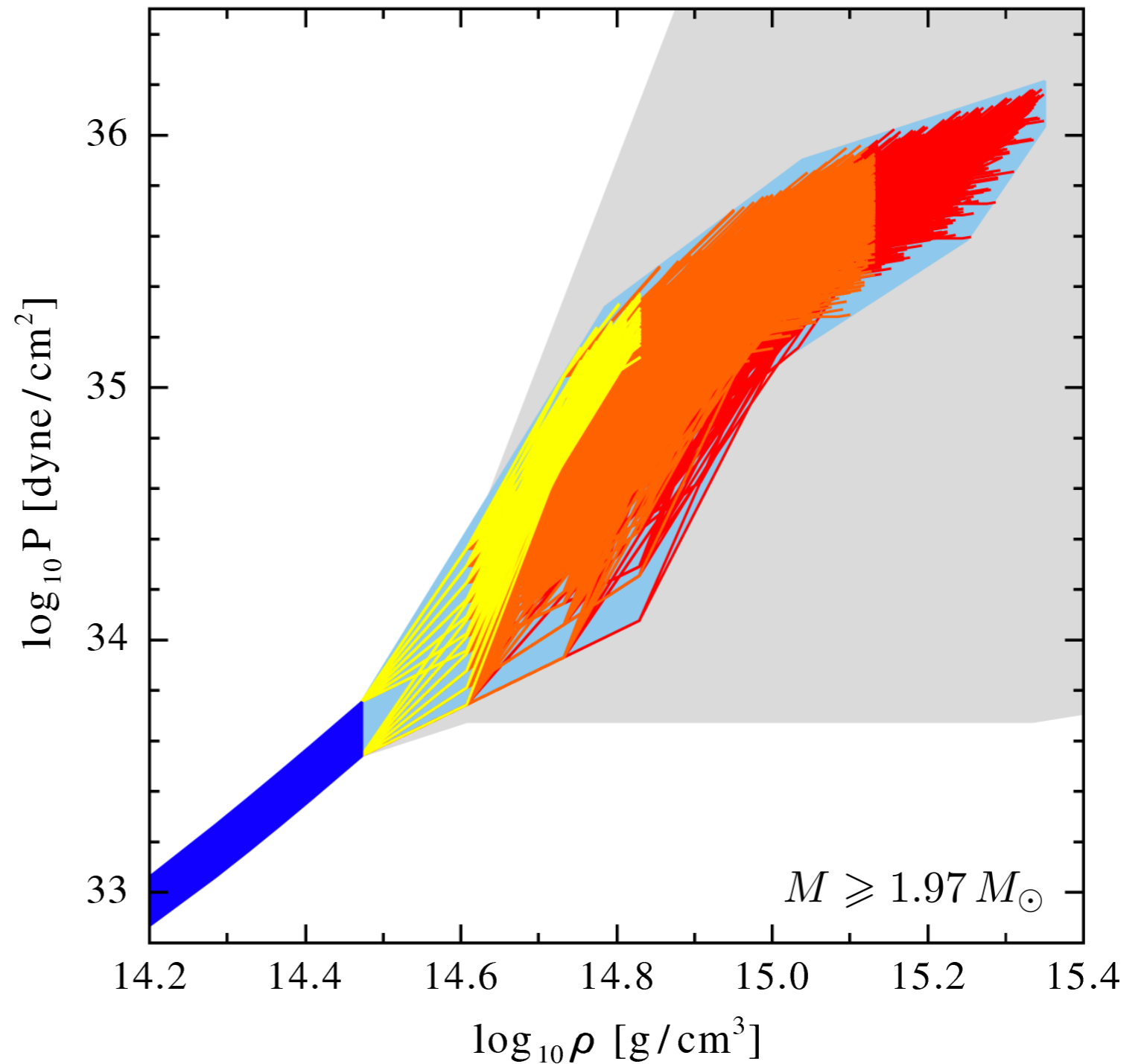
use the constraints:

recent NS observations

$$M_{\text{max}} > 1.97 M_{\odot}$$

causality

$$v_s(\rho) = \sqrt{dP/d\varepsilon} < c$$



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

constraints lead to significant reduction of EOS uncertainty band

Constraints on the nuclear equation of state

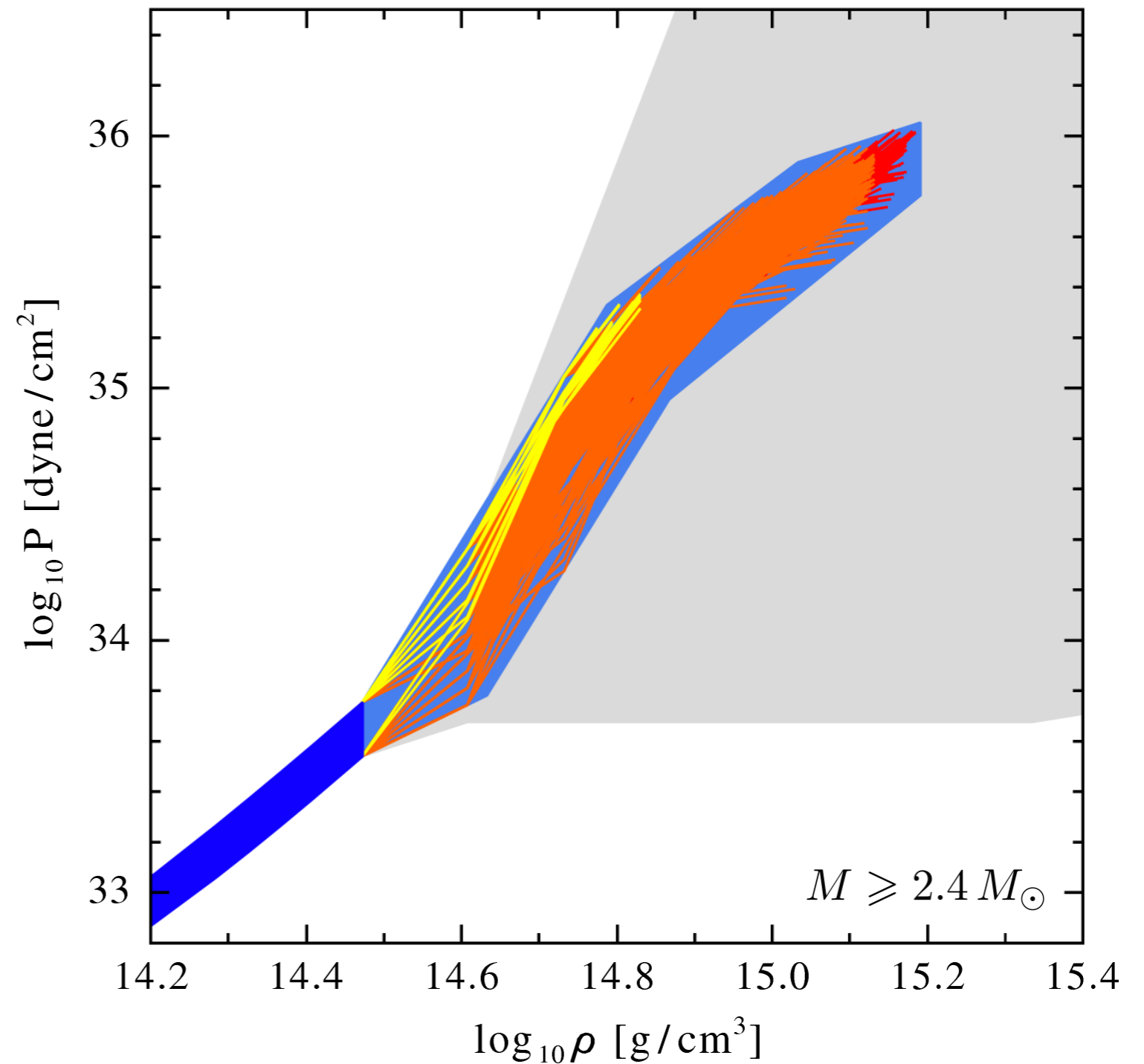
use the constraints:

fictitious NS mass

$$M_{\max} > 2.4 M_{\odot}$$

causality

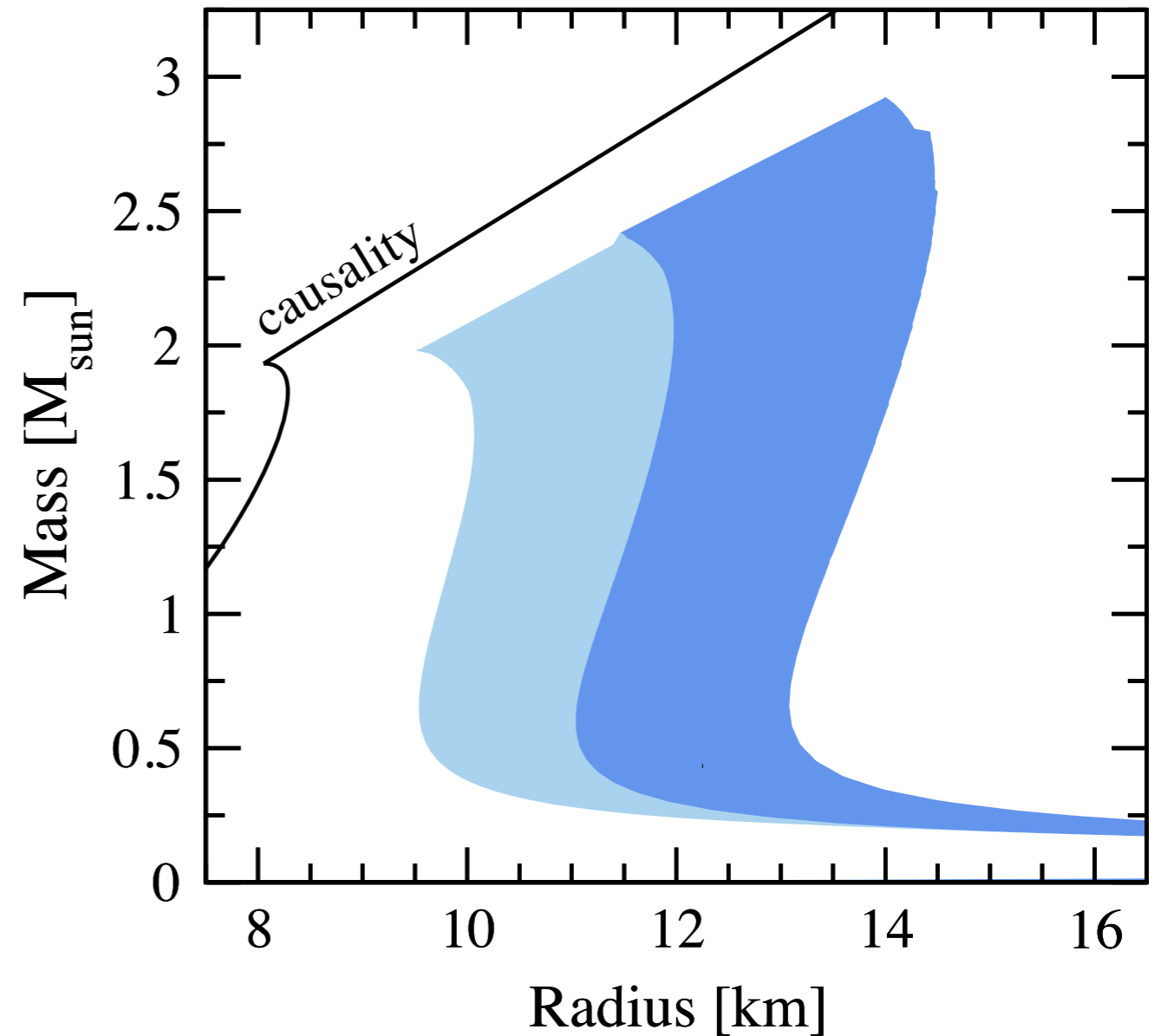
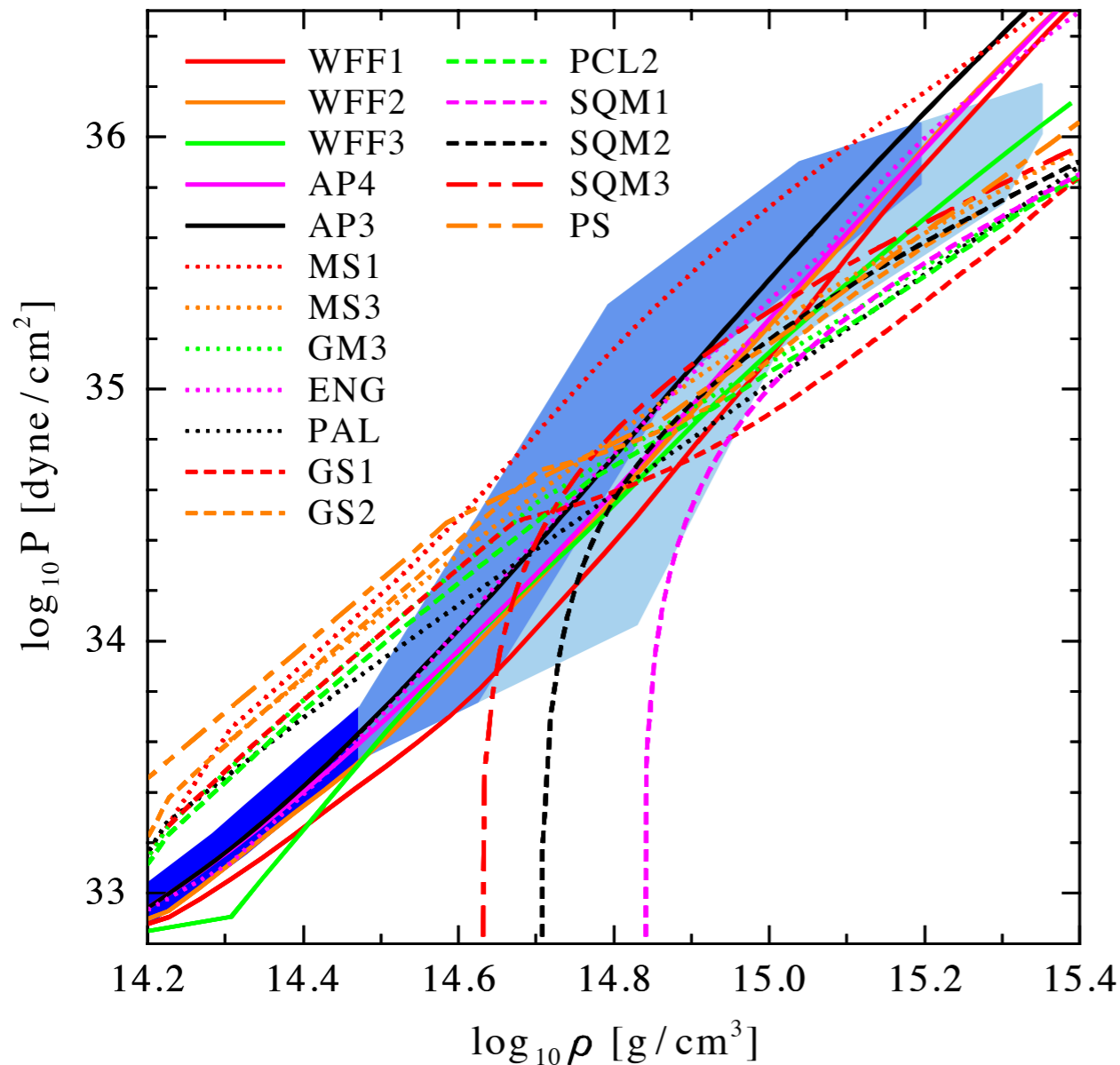
$$v_s(\rho) = \sqrt{dP/d\varepsilon} < c$$



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

increased M_{\max} systematically reduces width of band

Constraints on neutron star radii

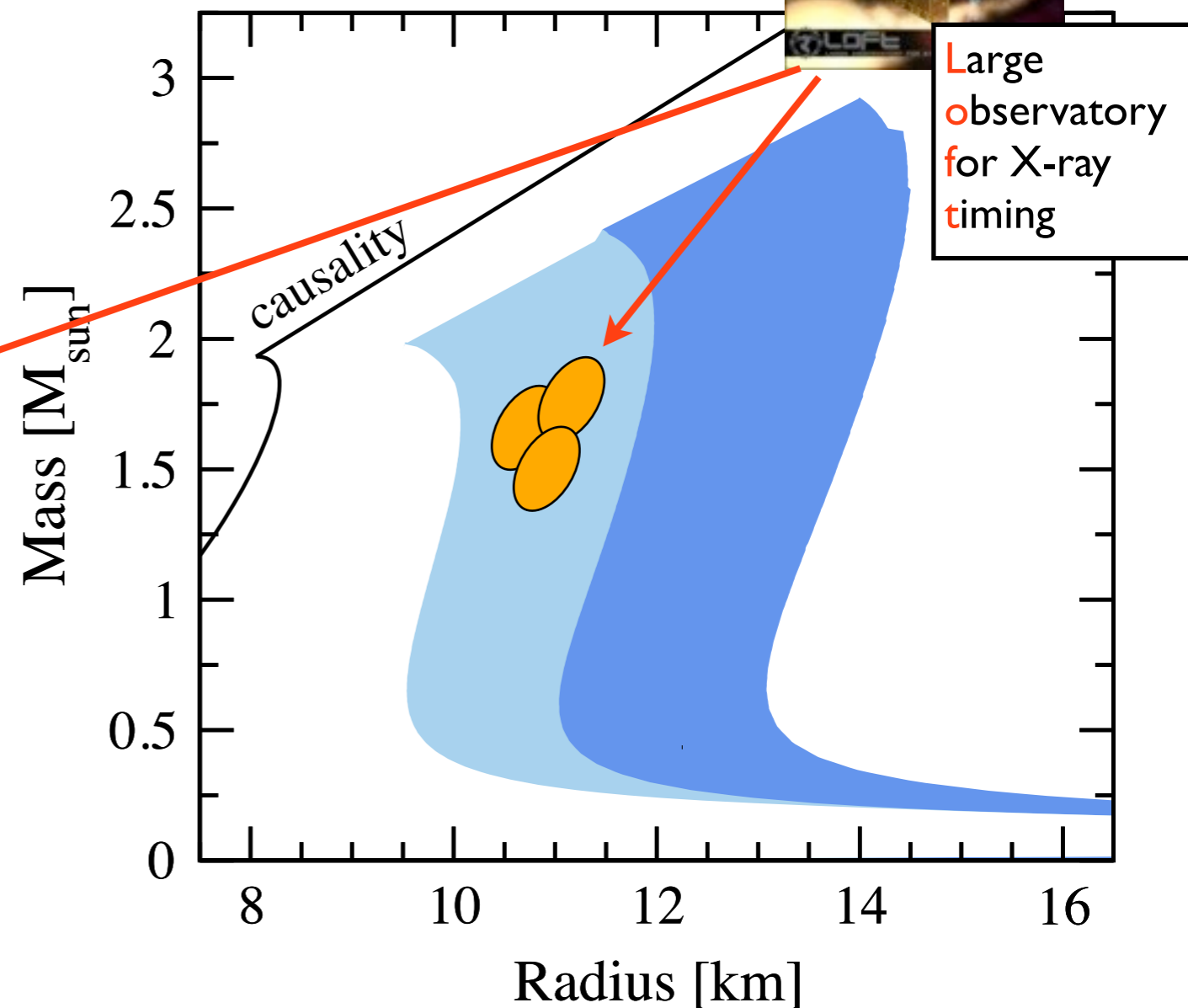
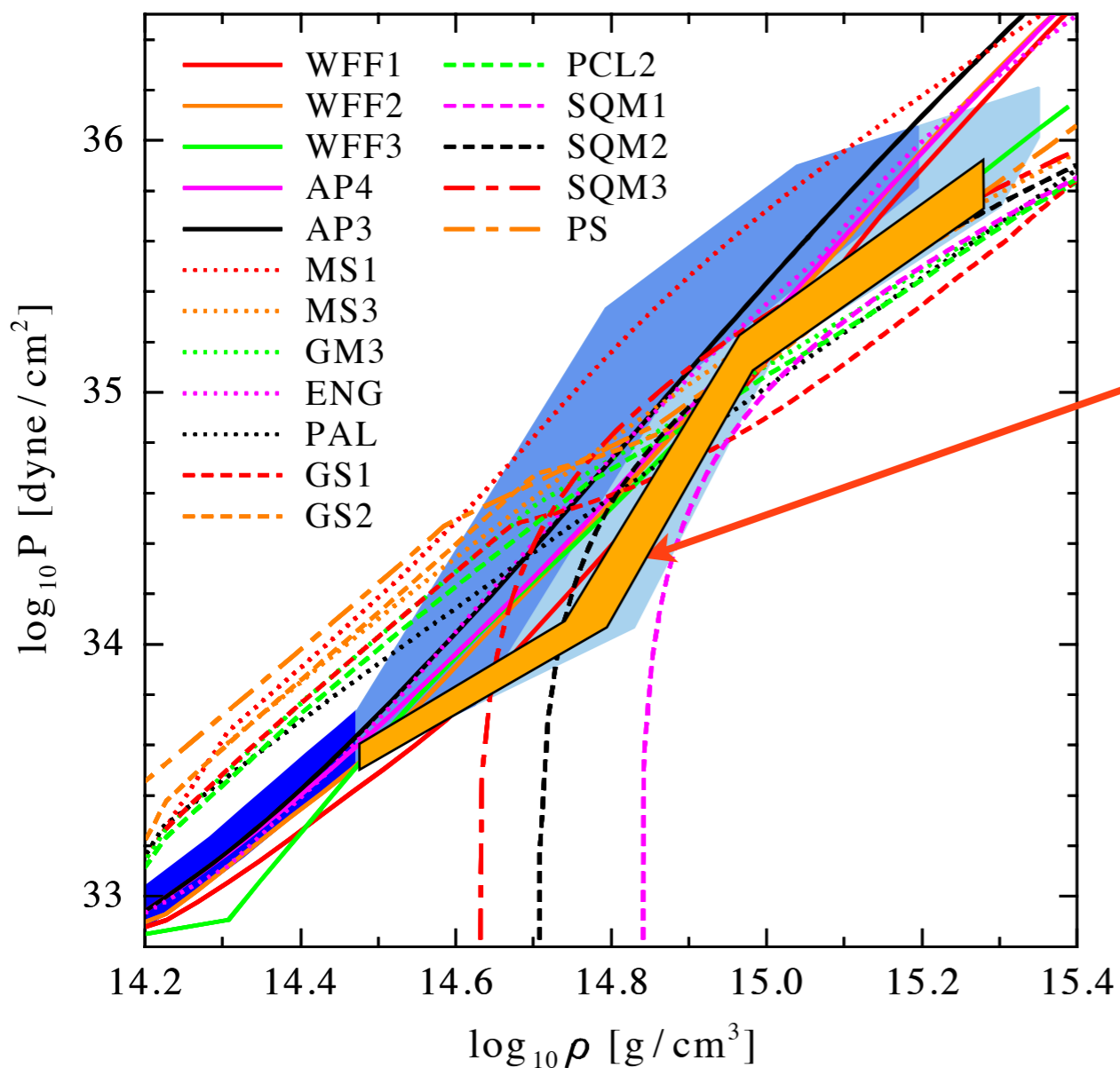


KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

see also KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

- low-density part of EOS sets scale for allowed high-density extensions
- current radius prediction for typical $1.4 M_{\odot}$ neutron star: 9.7 – 13.9 km

Constraints on neutron star radii



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013)

see also KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

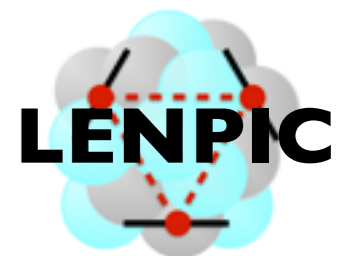
- low-density part of EOS sets scale for allowed high-density extensions
- current radius prediction for typical $1.4 M_{\odot}$ neutron star: 9.7 – 13.9 km
- radius measurements could significantly improve constraints

Summary

- recent advances allow ab initio studies of medium-mass nuclei
- remarkable agreement between different methods for given interaction, uncertainties dominated by differences in nuclear interactions
- results presented for properties of neutron-rich nuclei and matter based on sets of current chiral EFT NN+3N interactions

Future directions

- derivation of systematic uncertainty estimates for many-body observables, order-by-order convergence studies
- exploration of different fitting strategies, include bayesian analysis for statistical interpretation of uncertainties?
- role of regulators, clean separation of short- and long-range physics, naturalness of coupling constants, power counting schemes, inclusion of delta excitations...



In collaboration with:



C. Drischler, T. Krüger, R. Roth,
A. Schwenk



R. Furnstahl, S. More



S. Bogner



E. Epelbaum, H. Krebs



A. Gezerlis



A. Nogga



J. Lattimer



C. Pethick



J. Golak, R. Skibinski



G. Hagen, T. Papenbrock



international collaborator in

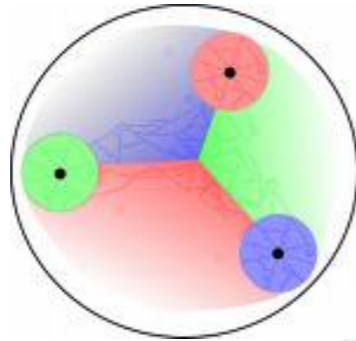


computing support:

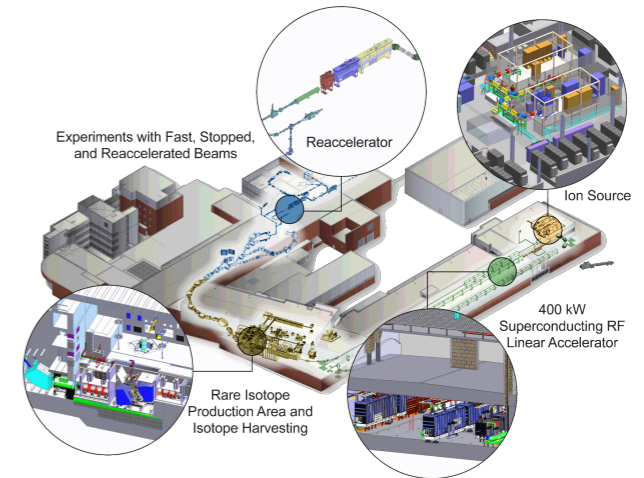


Thank you!

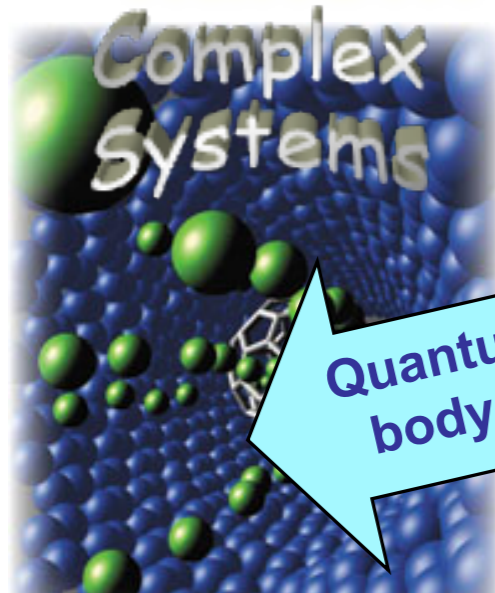
New frontiers from rare isotope facilities



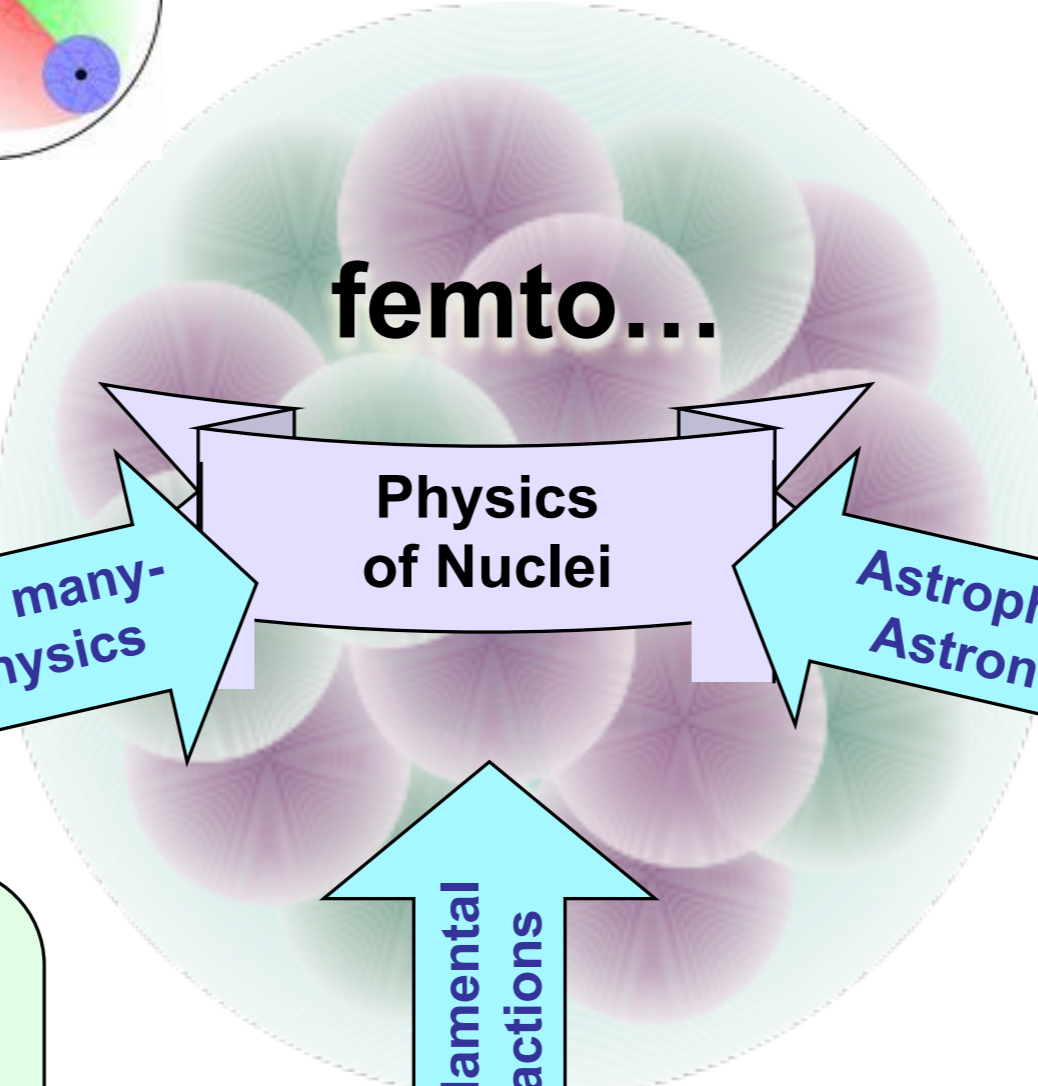
subfemto...



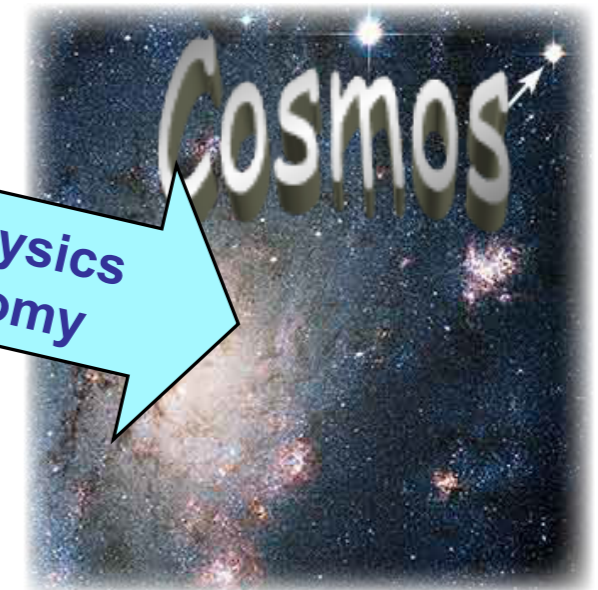
nano...



femto...



Giga...



Physics of Nuclei

Quantum many-body physics

Astrophysics Astronomy

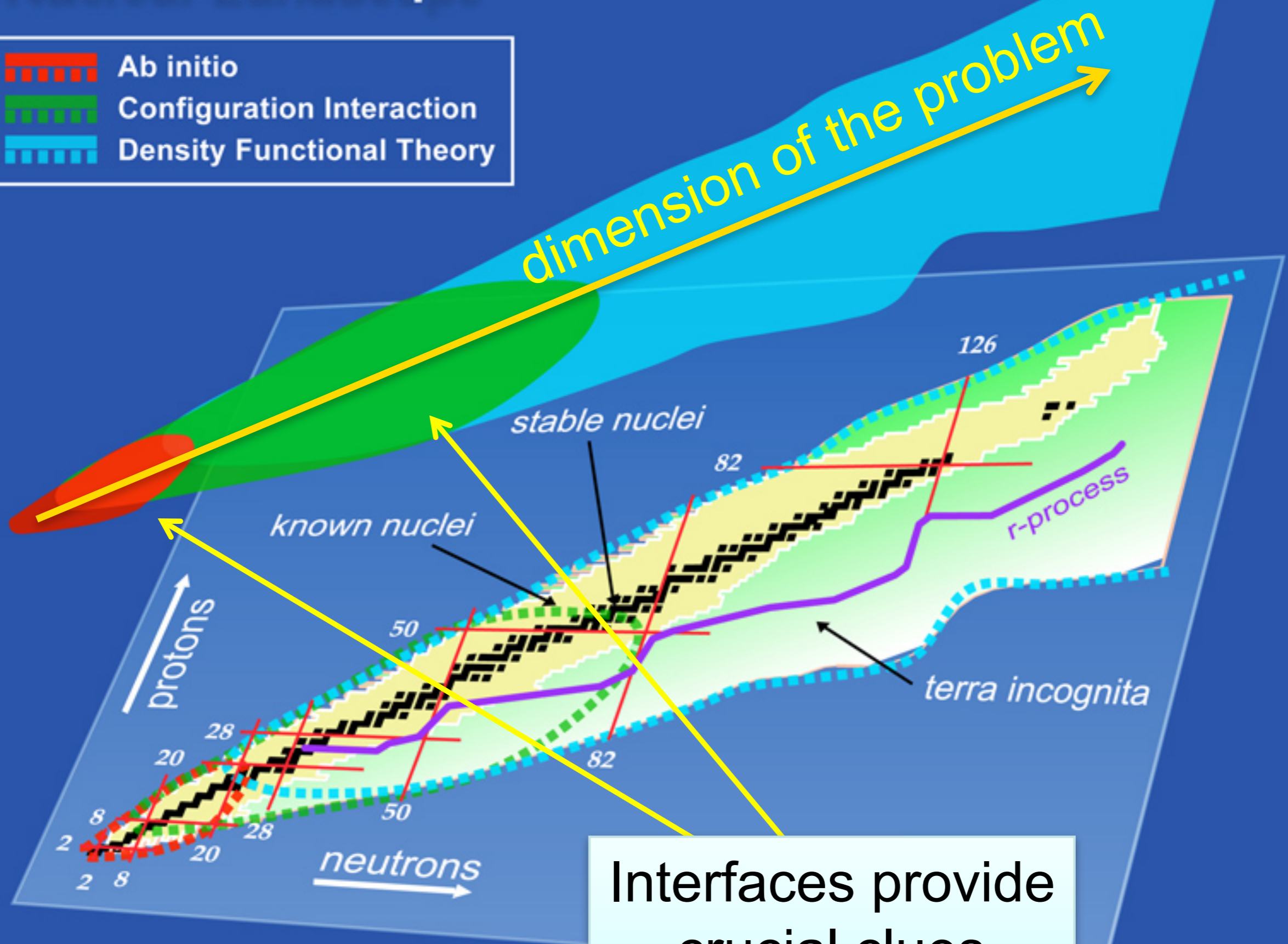
Fundamental interactions

How do collective phenomena emerge from simple constituents?
How can complex systems display astonishing simplicities?
What are unique properties of open systems?

What is the New Standard Model?

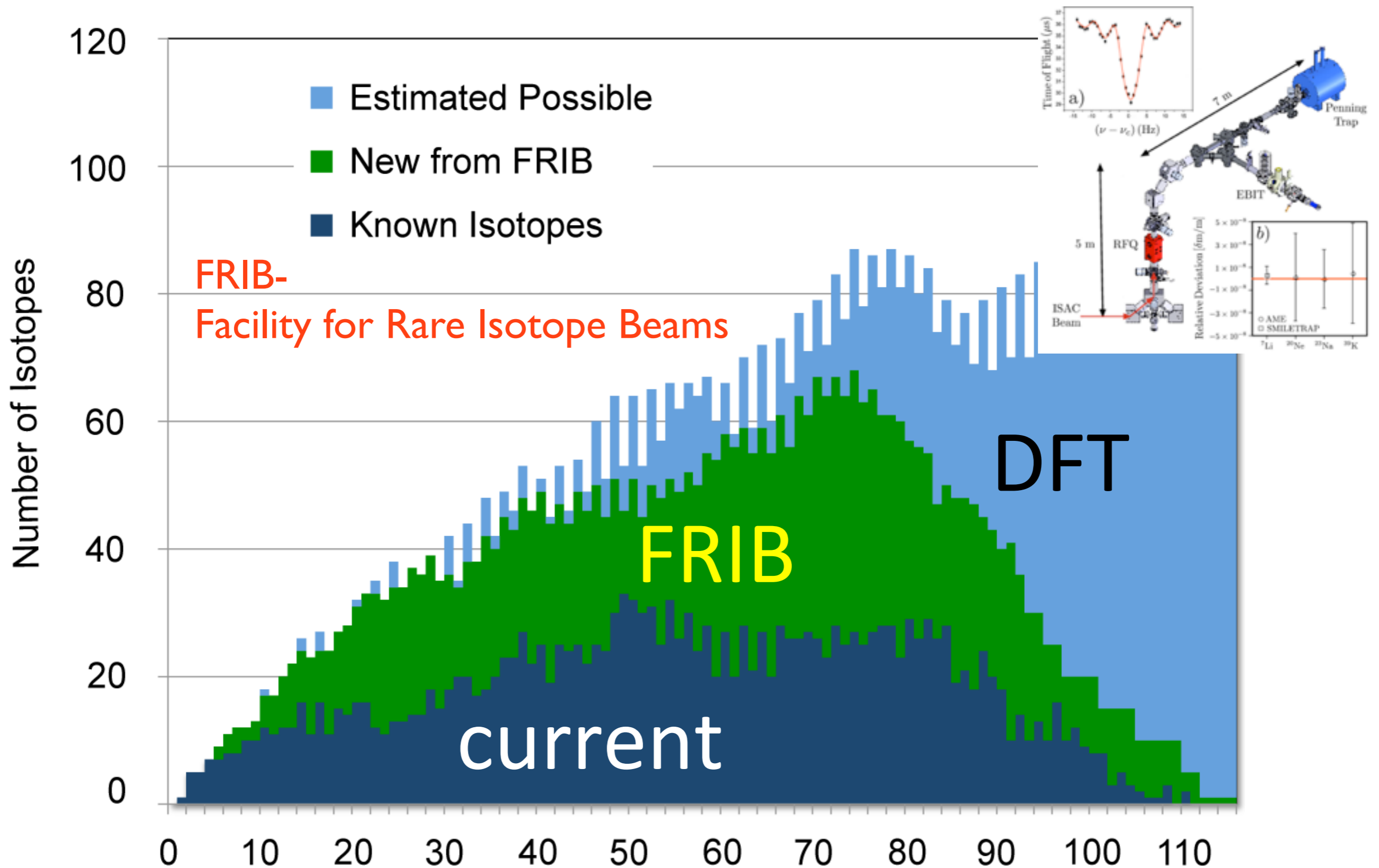
How do nuclei shape the physical universe?
What is the origin of the elements?

Nuclear Landscape



Interfaces provide crucial clues

New frontiers from rare isotope facilities



Exciting recent developments on many fronts...

LETTER

nature

doi:10.1038/nature12522

Evidence for a new nuclear ‘magic number’ from the level structure of ^{54}Ca

D. Steppenbeck¹, S. Takeuchi², N. Aoi³, P. Doornenbal², M. Matsushita¹, H. Wang², H. Baba², N. Fukuda², S. Go¹, M. Honma⁴, J. Lee², K. Matsui⁵, S. Michimasa¹, T. Motobayashi², D. Nishimura⁶, T. Otsuka^{1,5}, H. Sakurai^{2,5}, Y. Shiga⁷, P.-A. Söderström², T. Sumikama⁸, H. Suzuki², R. Taniuchi⁵, Y. Utsuno⁹, J. J. Valiente-Dobón¹⁰ & K. Yoneda²

LETTER

nature

doi:10.1038/nature11188

The limits of the nuclear landscape

Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2,†}

LETTER

nature

doi:10.1038/nature12226

Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wolf¹ & K. Zuber¹⁰

LETTER

nature

doi:10.1038/nature09466

A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

RESEARCH ARTICLE SUMMARY

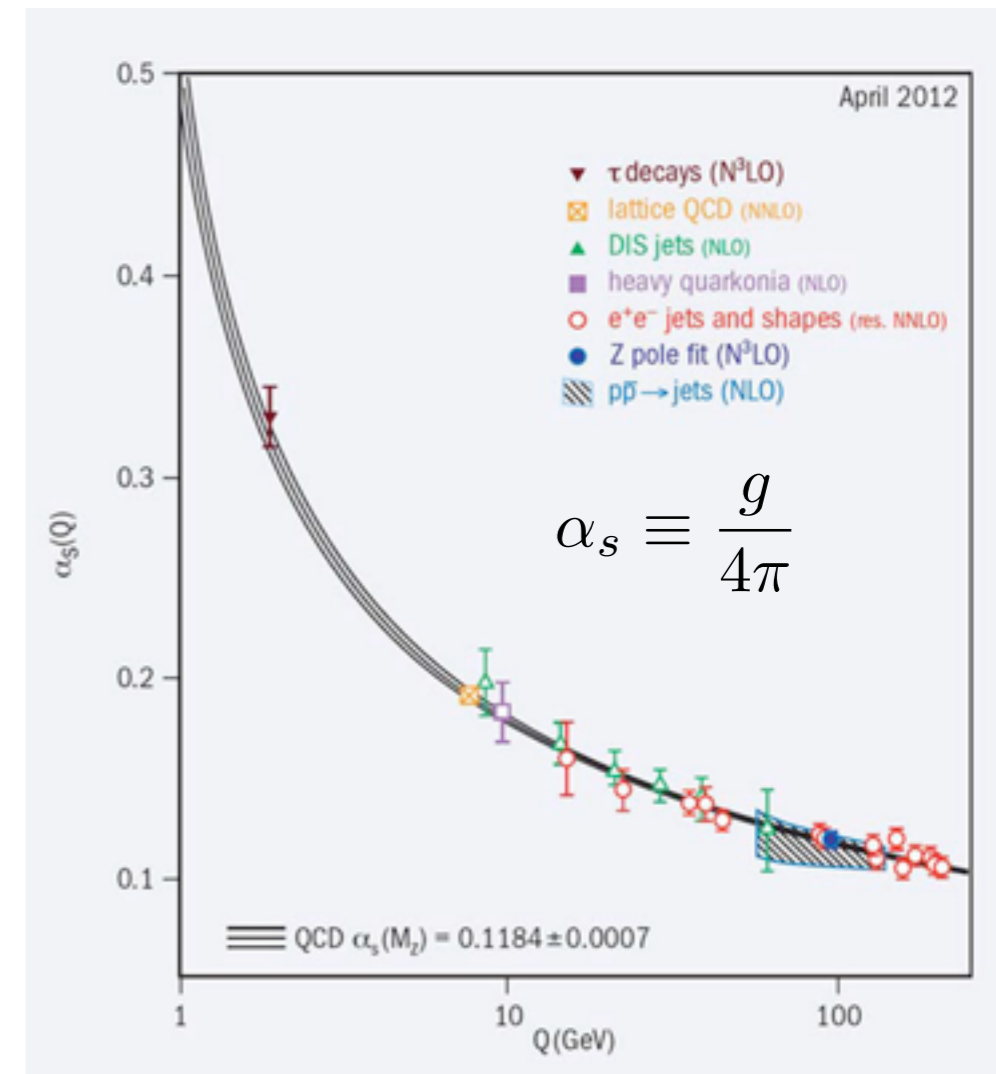
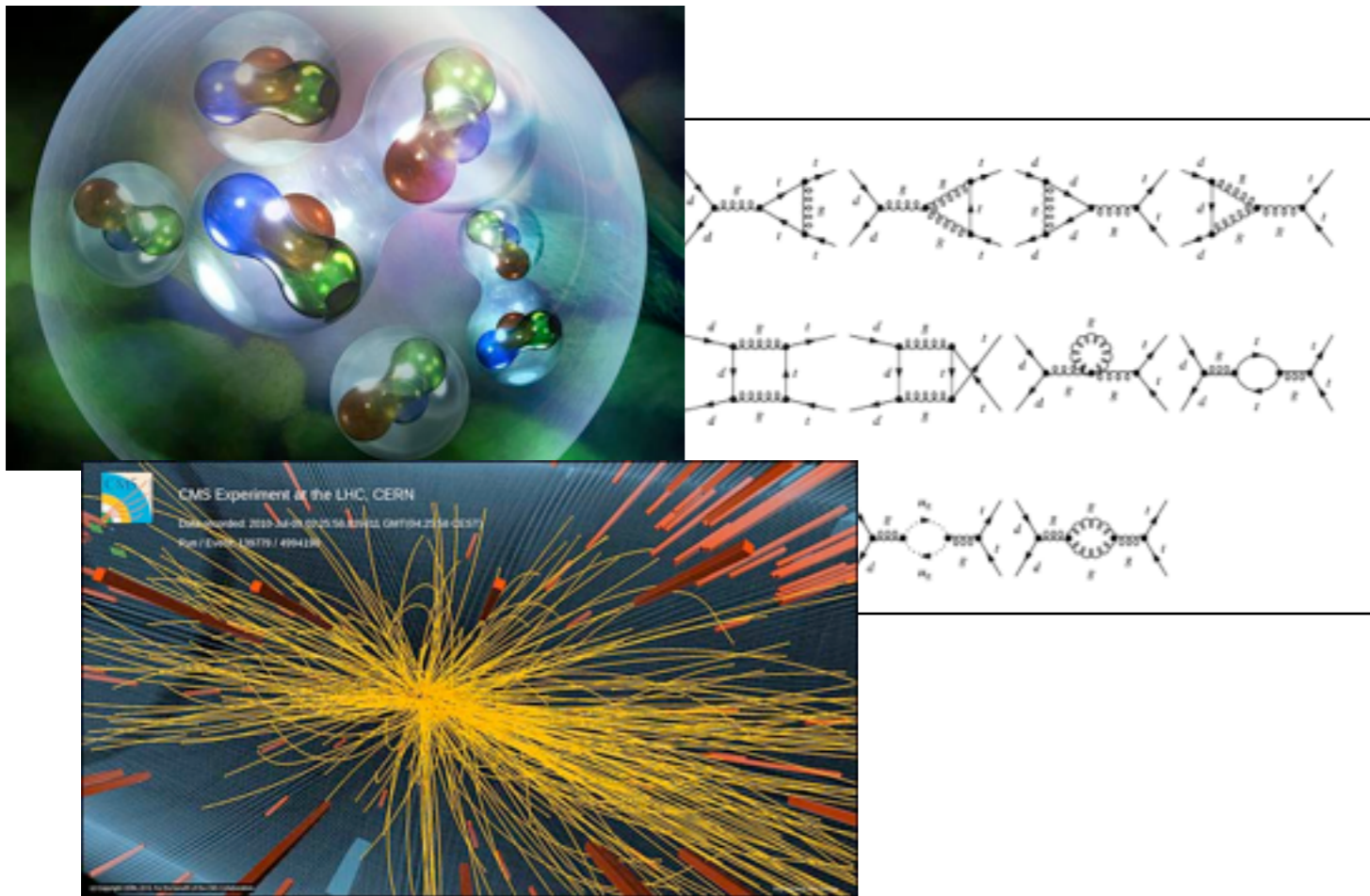
Science

A Massive Pulsar in a Compact Relativistic Binary

John Antoniadis,* Paulo C. C. Freire, Norbert Wex, Thomas M. Tauris, Ryan S. Lynch, Marten H. van Kerkwijk, Michael Kramer, Cees Bassa, Vik S. Dhillon, Thomas Driebe, Jason W. T. Hessels, Victoria M. Kaspi, Vladislav I. Kondratiev, Norbert Langer, Thomas R. Marsh, Maura A. McLaughlin, Timothy T. Pennucci, Scott M. Ransom, Ingrid H. Stairs, Joeri van Leeuwen, Joris P. W. Verbiest, David G. Whelan

Theory of the strong interaction: Quantum chromodynamics

$$\mathcal{L}_{QCD} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \bar{q}(i\gamma^\mu \partial_\mu - m)q + g\bar{q}\gamma^\mu T_a q A_\mu^a$$

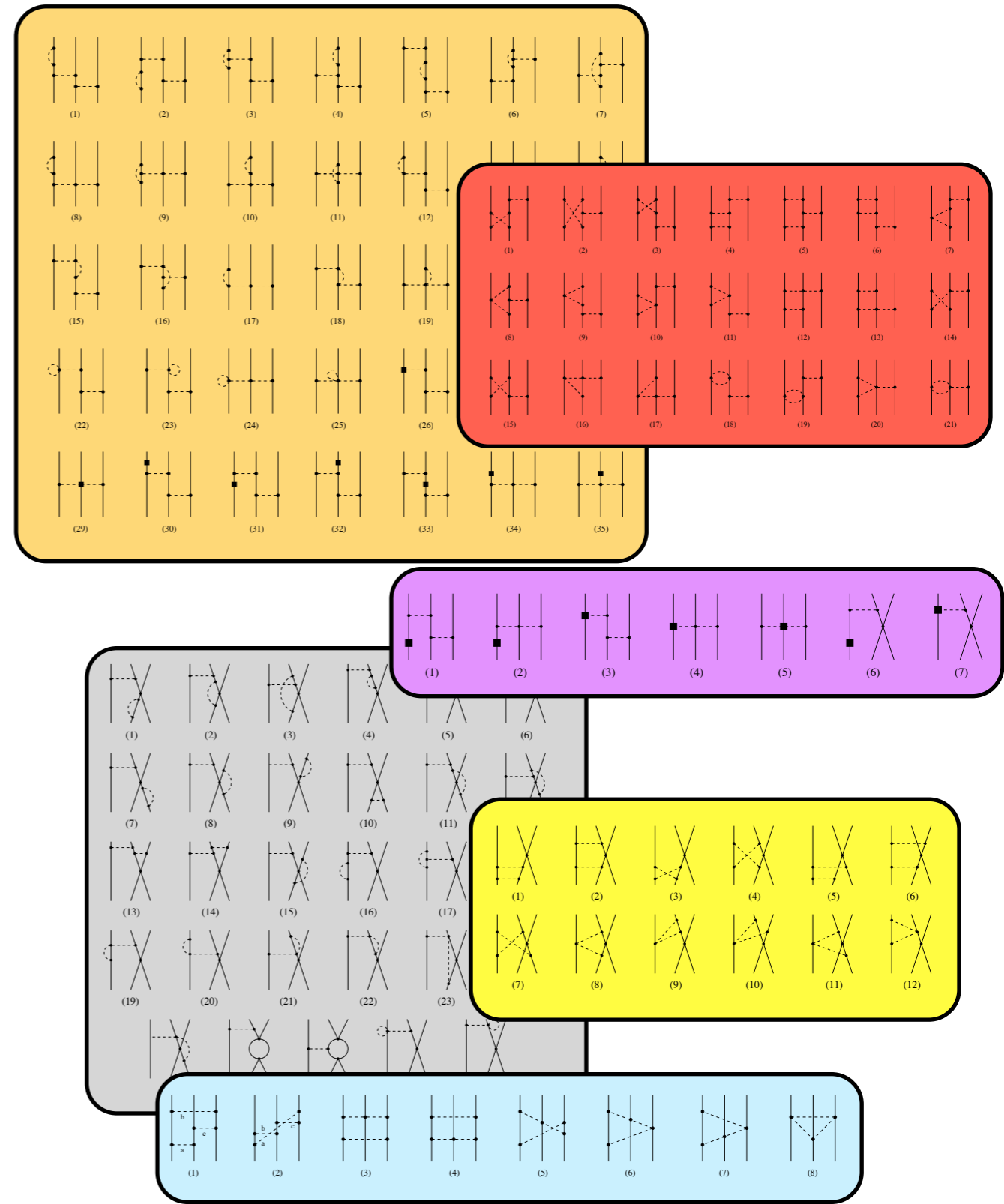


- theory perturbative at high energies
- highly non-perturbative at low energies

Chiral 3N forces at subleading order (N^3LO)

	2N forces	3N forces	4N forces
$\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
$\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
$\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
$\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

2011



Bernard et al., PRC 77, 064004 (2008)
 Bernard et al., PRC 84, 054001 (2011)

Chiral 3N forces at subleading order (N^3LO)

	2N forces	3N forces	4N forces
$\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
$\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
$\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
$\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

2011

ALL TERMS PREDICTED

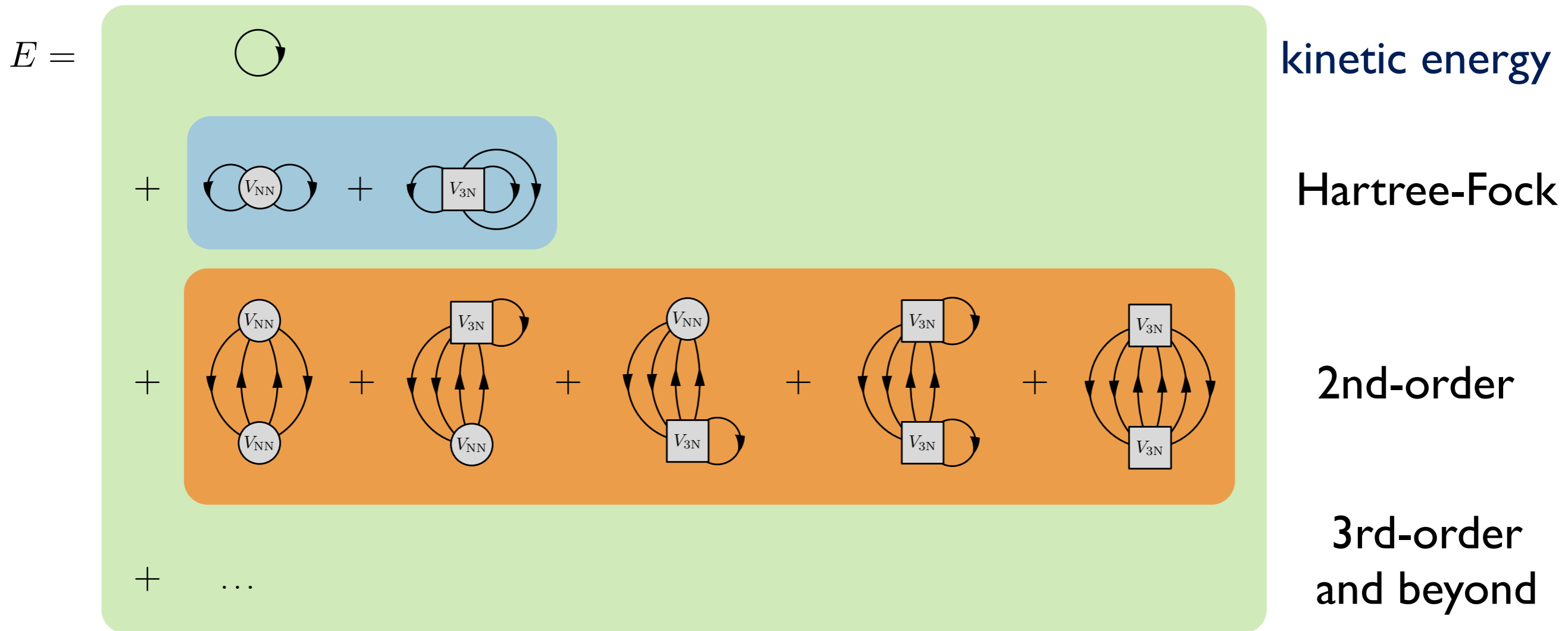
key for

- consistency
- tests
- improved precision
- uncertainty estimates of the theory

Equation of state: Many-body perturbation theory

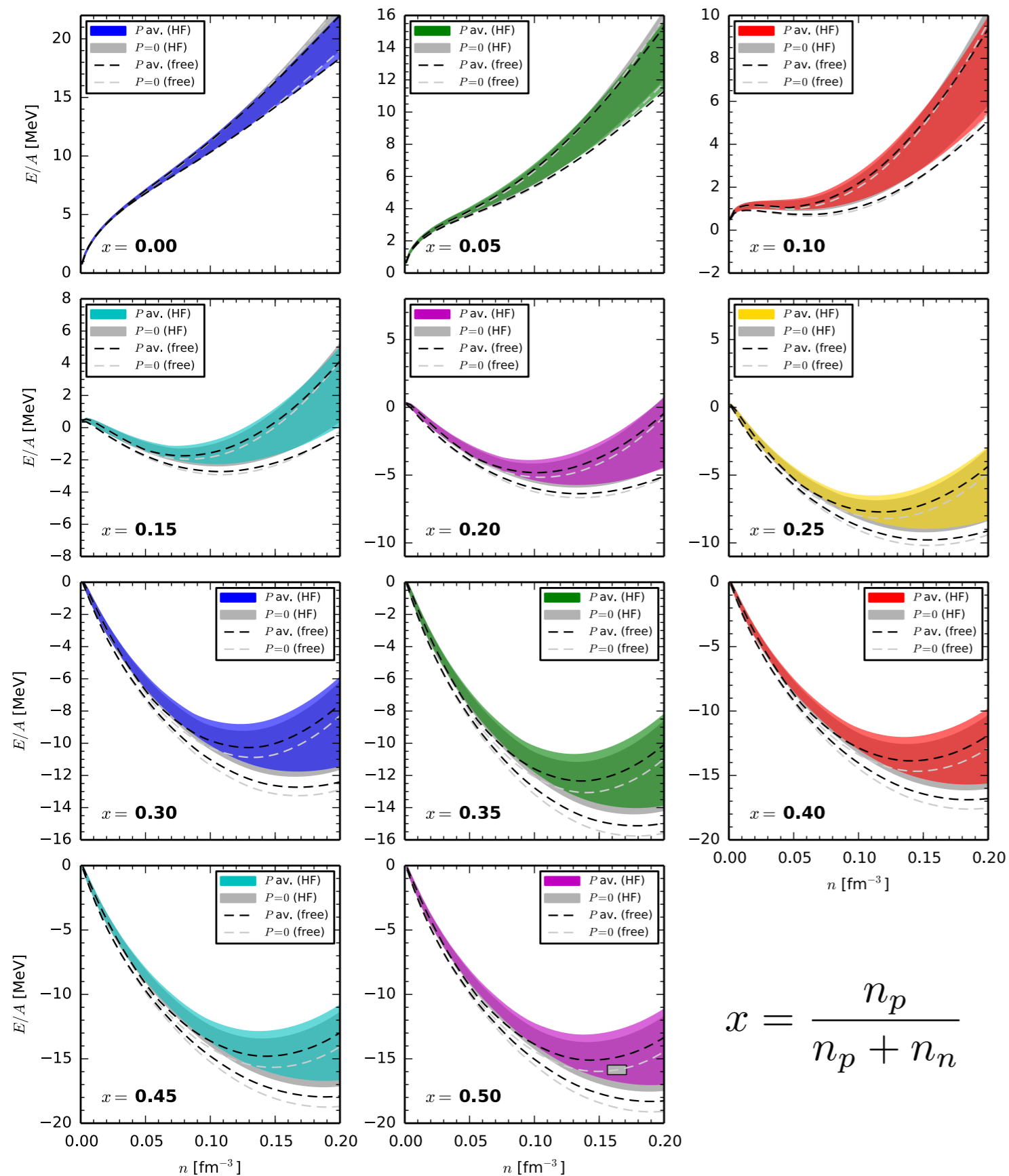
central quantity of interest: energy per particle E/N

$$H(\lambda) = T + V_{\text{NN}}(\lambda) + V_{\text{3N}}(\lambda) + \dots$$

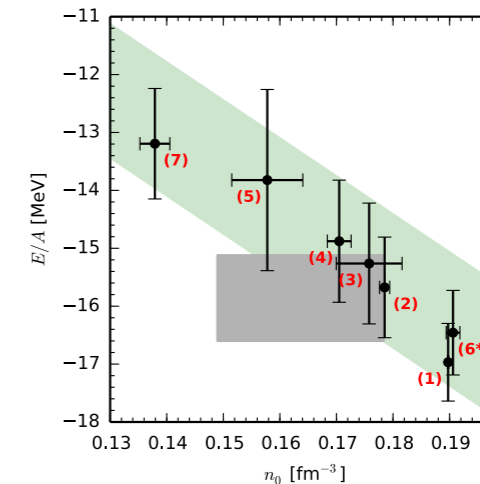


- “hard” interactions require non-perturbative summation of diagrams
- with low-momentum interactions much more perturbative
- inclusion of 3N interaction contributions crucial!

First application to isospin asymmetric nuclear matter



- uncertainty bands determined by set of 7 Hamiltonians

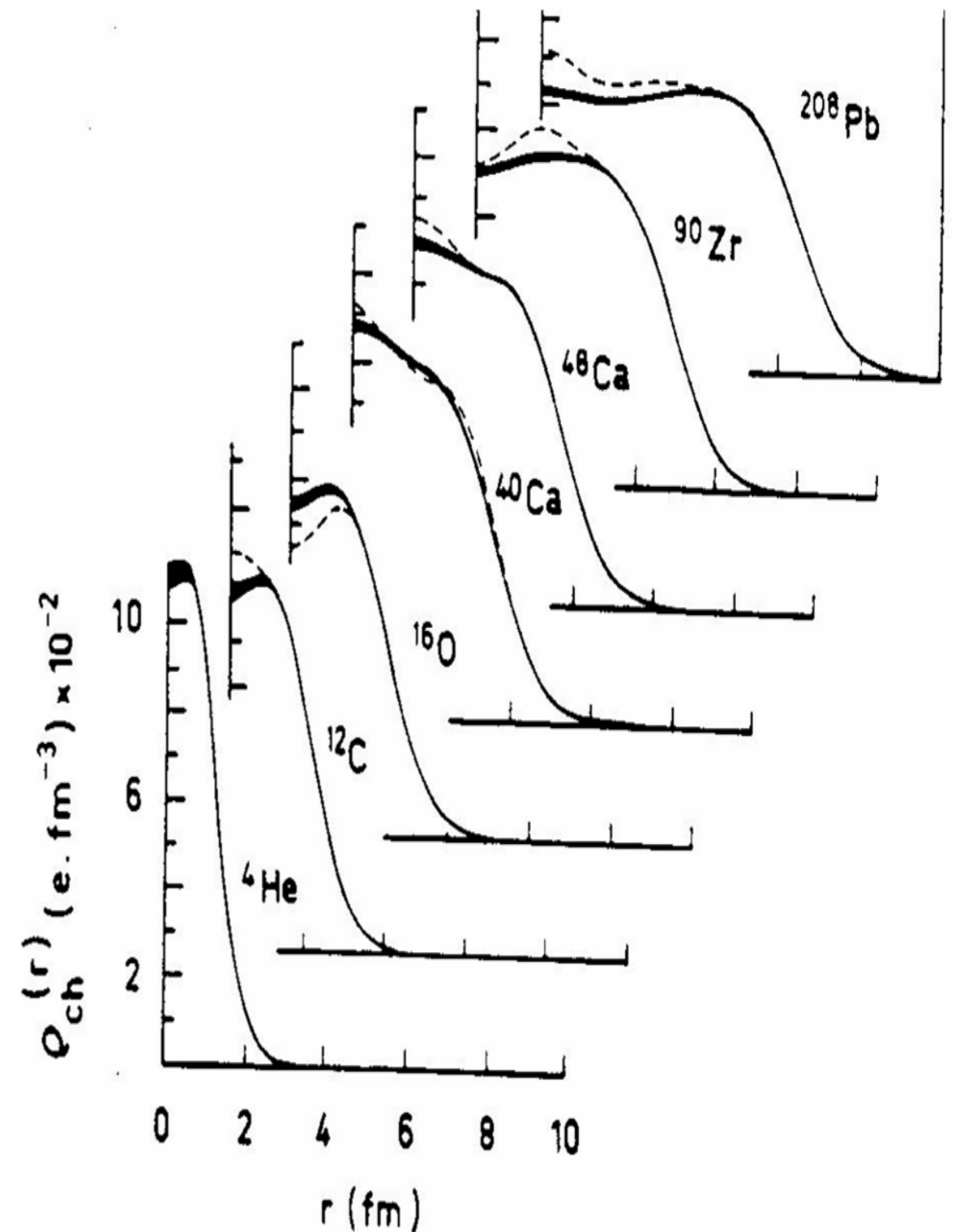
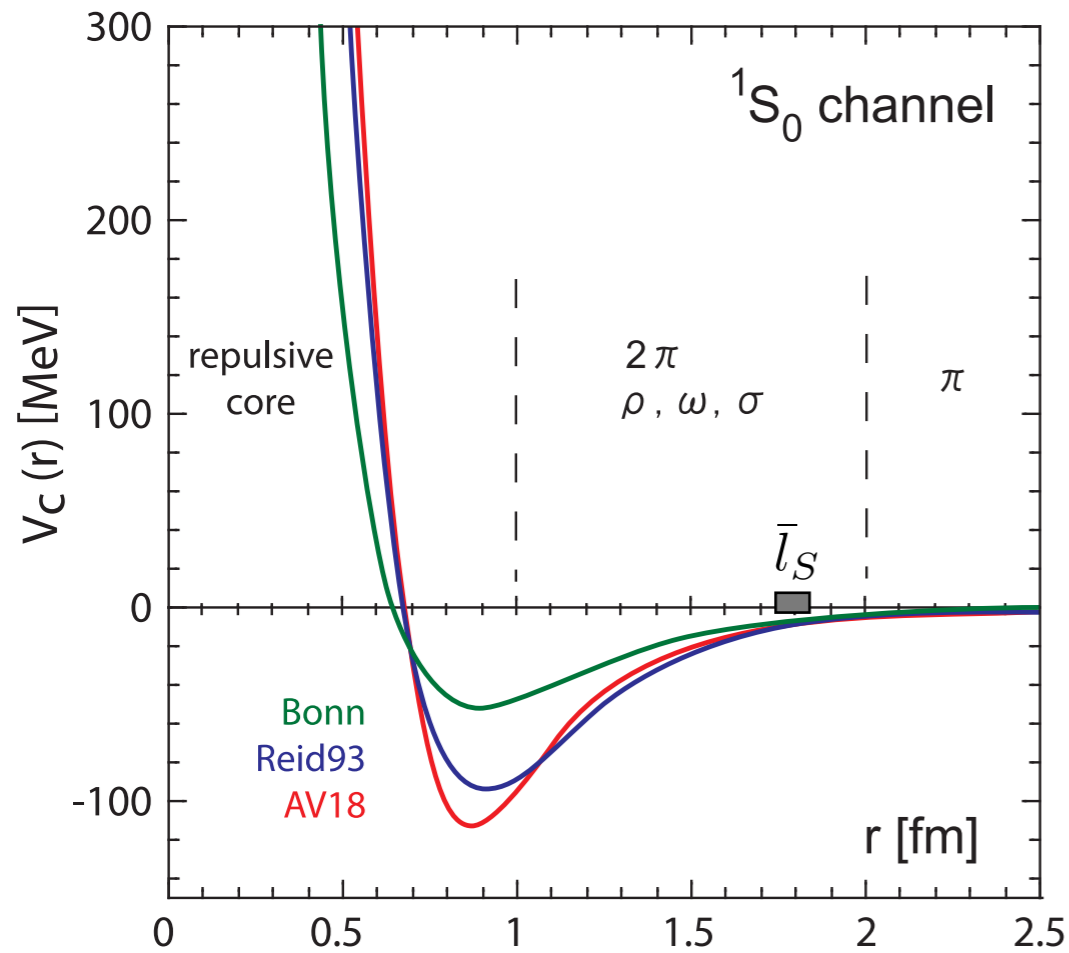


- many-body framework allows treatment of any decomposed 3N interaction

Drischler, KH, Schwenk,
in preparation

$$x = \frac{n_p}{n_p + n_n}$$

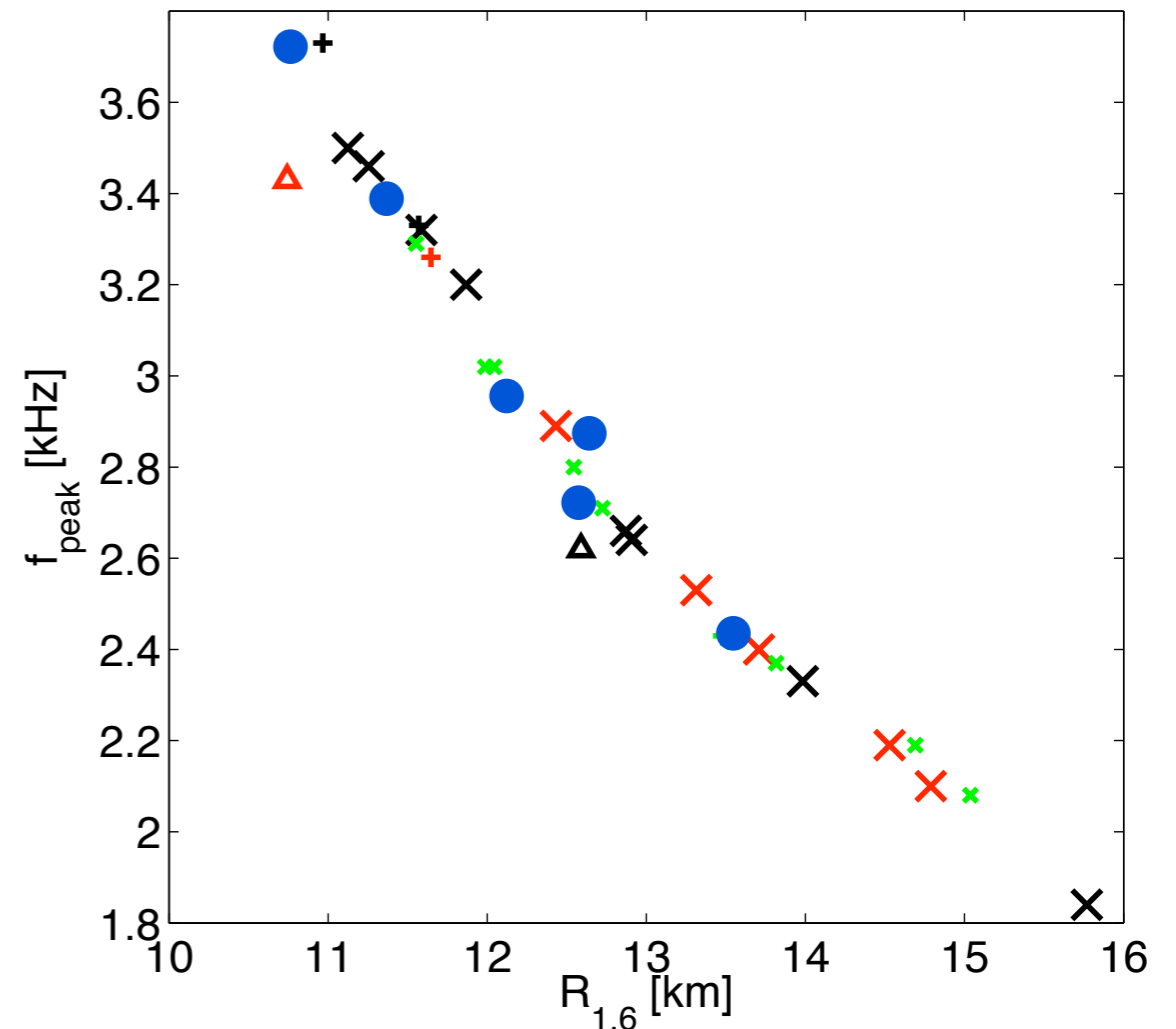
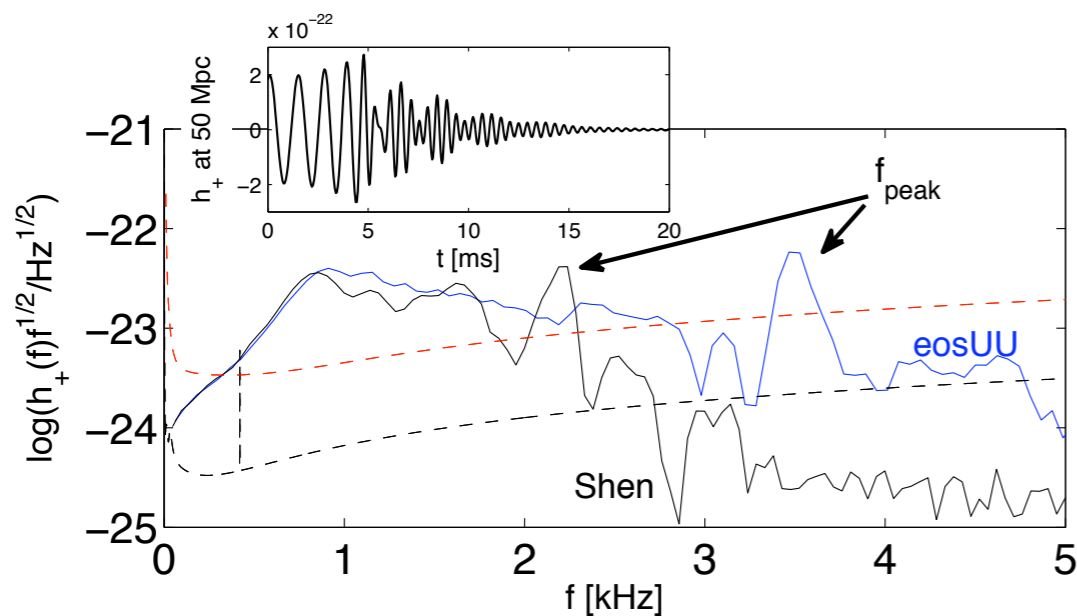
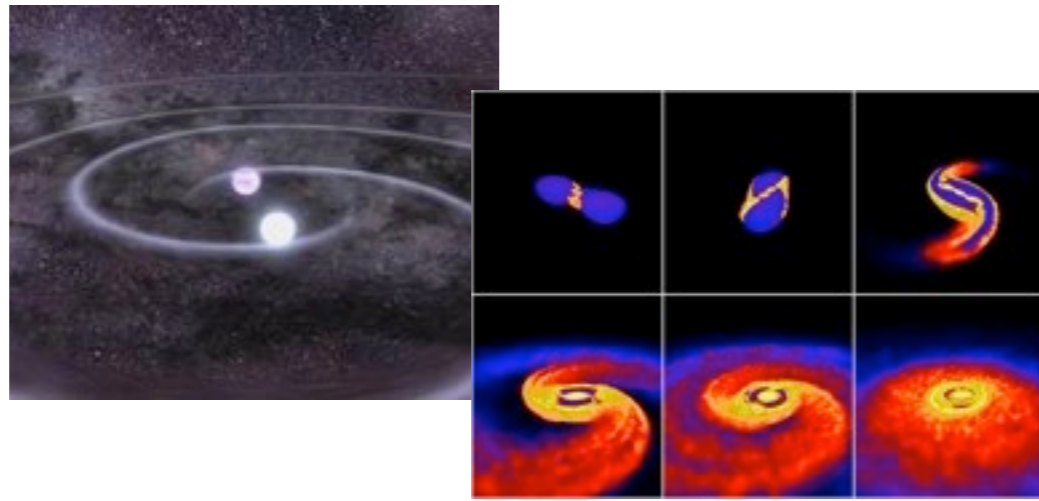
Equation of state of symmetric nuclear matter, nuclear saturation



“Very soft potentials must be excluded because they do not give saturation; they give too much binding and too high density. In particular, a substantial tensor force is required.”

Hans Bethe (1971)

Gravitational wave signals from neutron star binary mergers



Bauswein and Janka, PRL 108, 011101 (2012),
 Bauswein, Janka, KH, Schwenk, PRD 86, 063001 (2012)

- simulations of NS binary mergers show strong correlation between f_{peak} of the GW spectrum and the radius of a NS
- measuring f_{peak} is key step for constraining EOS systematically at large ρ