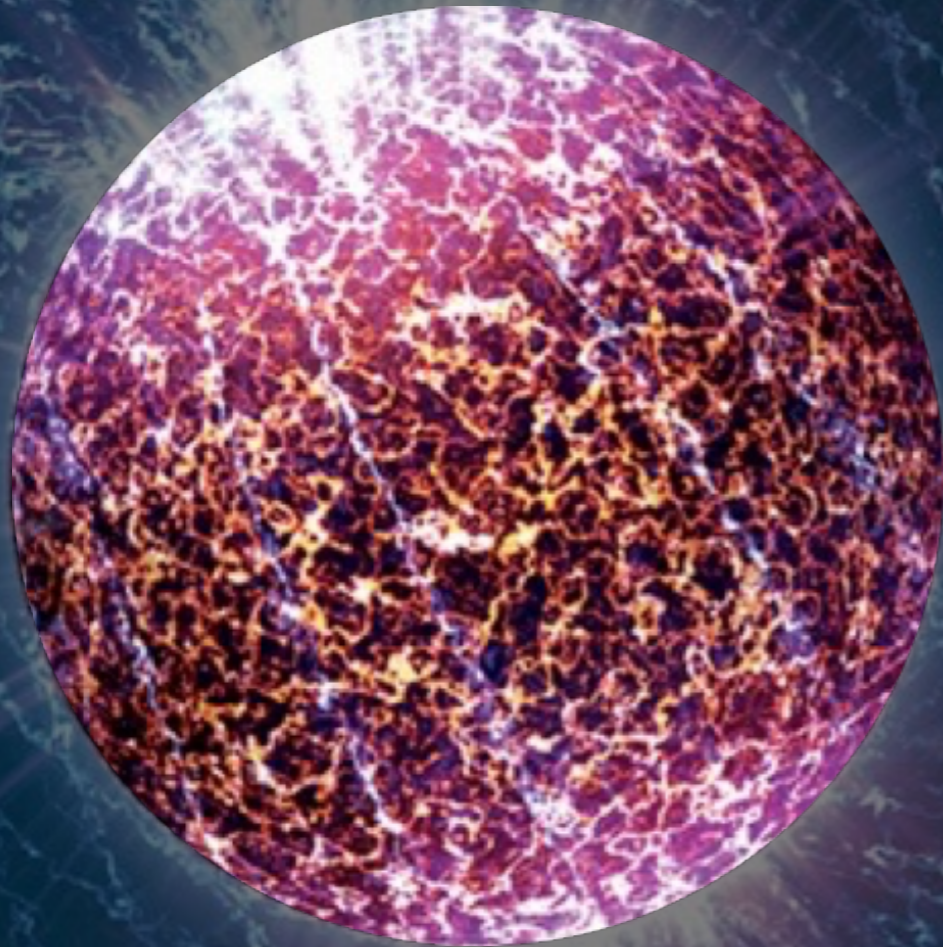


Neutron stars radius measurements:

New results and future prospects,

*but I'll talk about
masses too...*



Sebastien Guillot

Pontificia Universidad Católica de Chile

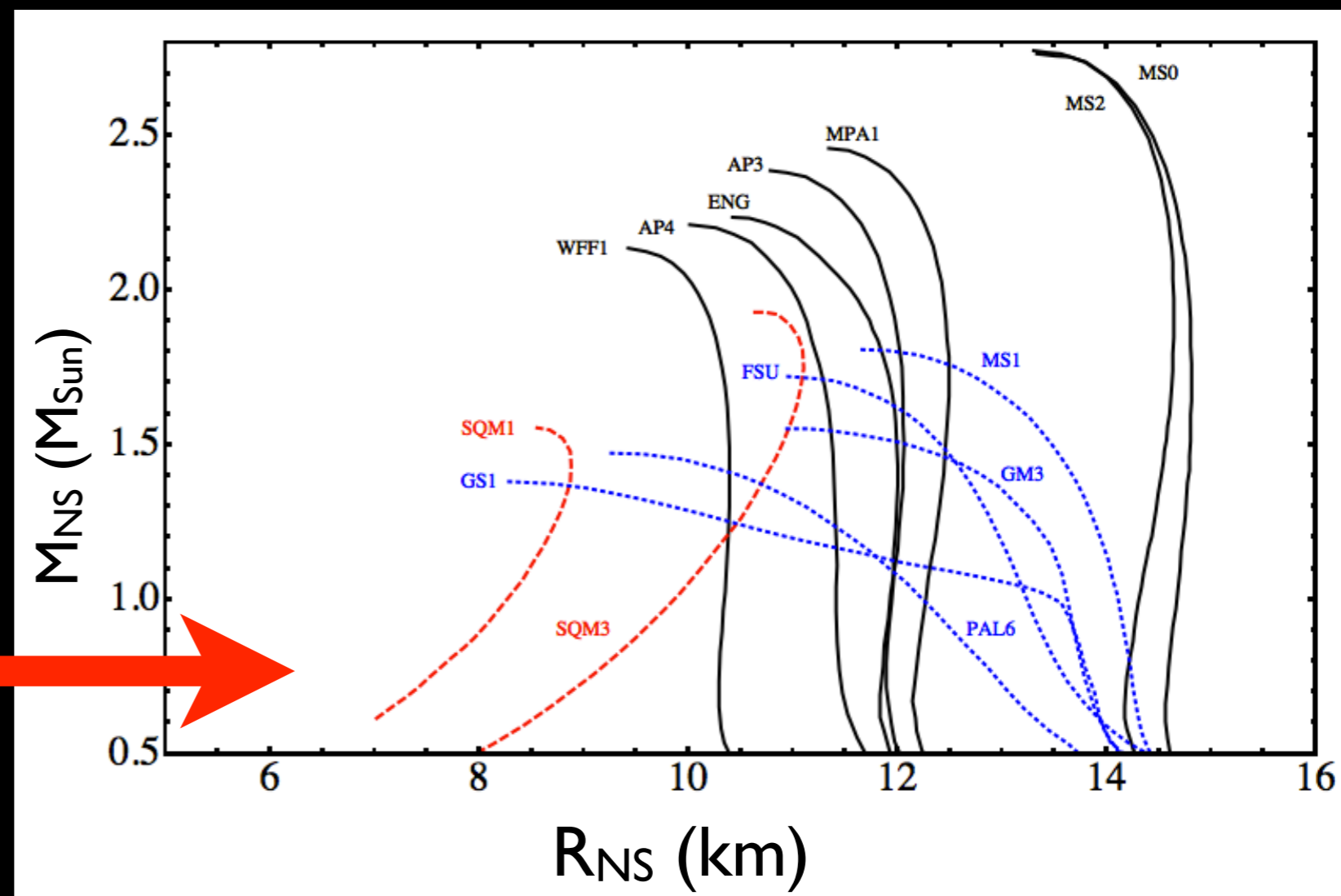
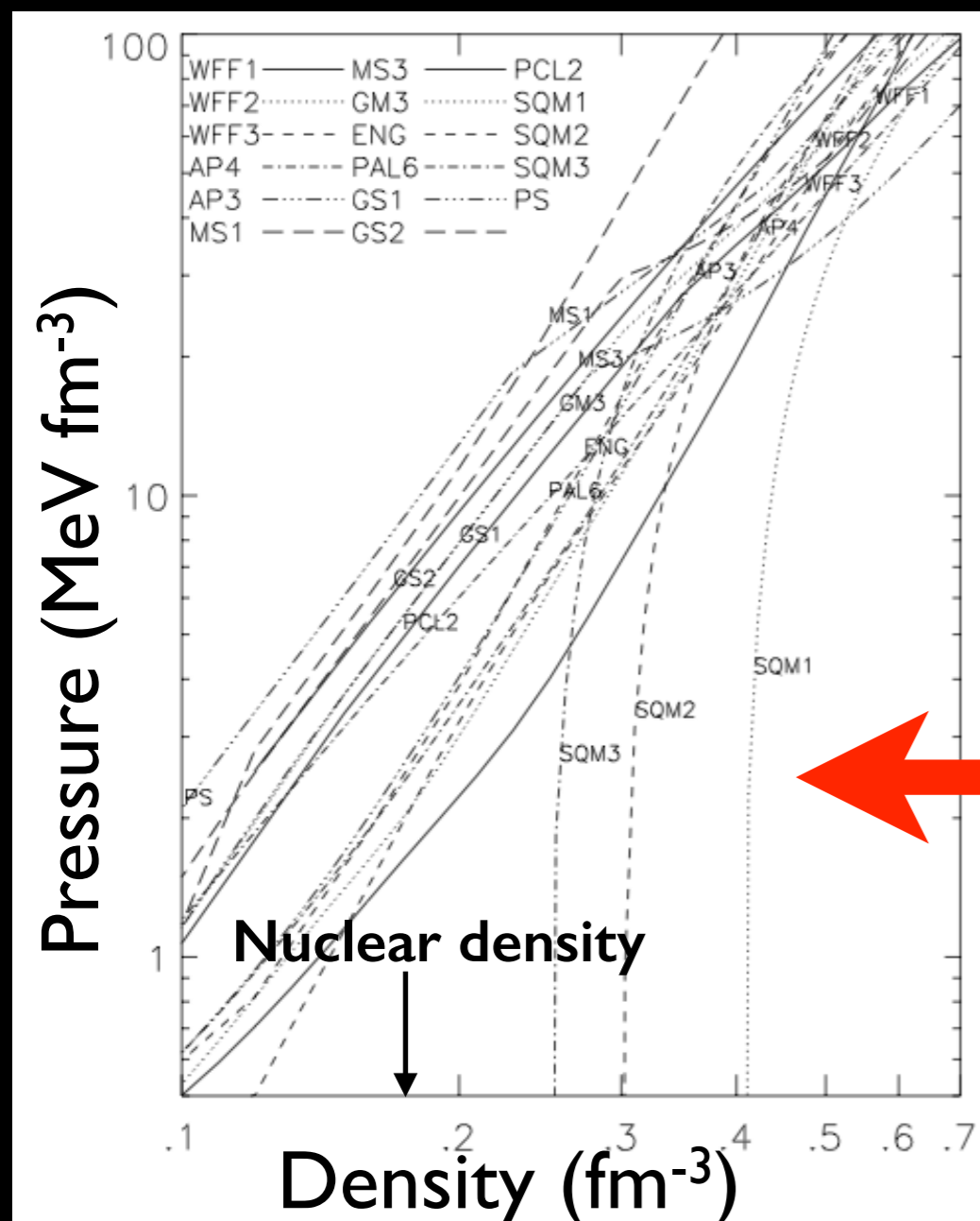
Some collaborators

R. Rutledge, N. Webb, M. Servillat

F. Özel, C. Heinke, D. Psaltis, T. Güver

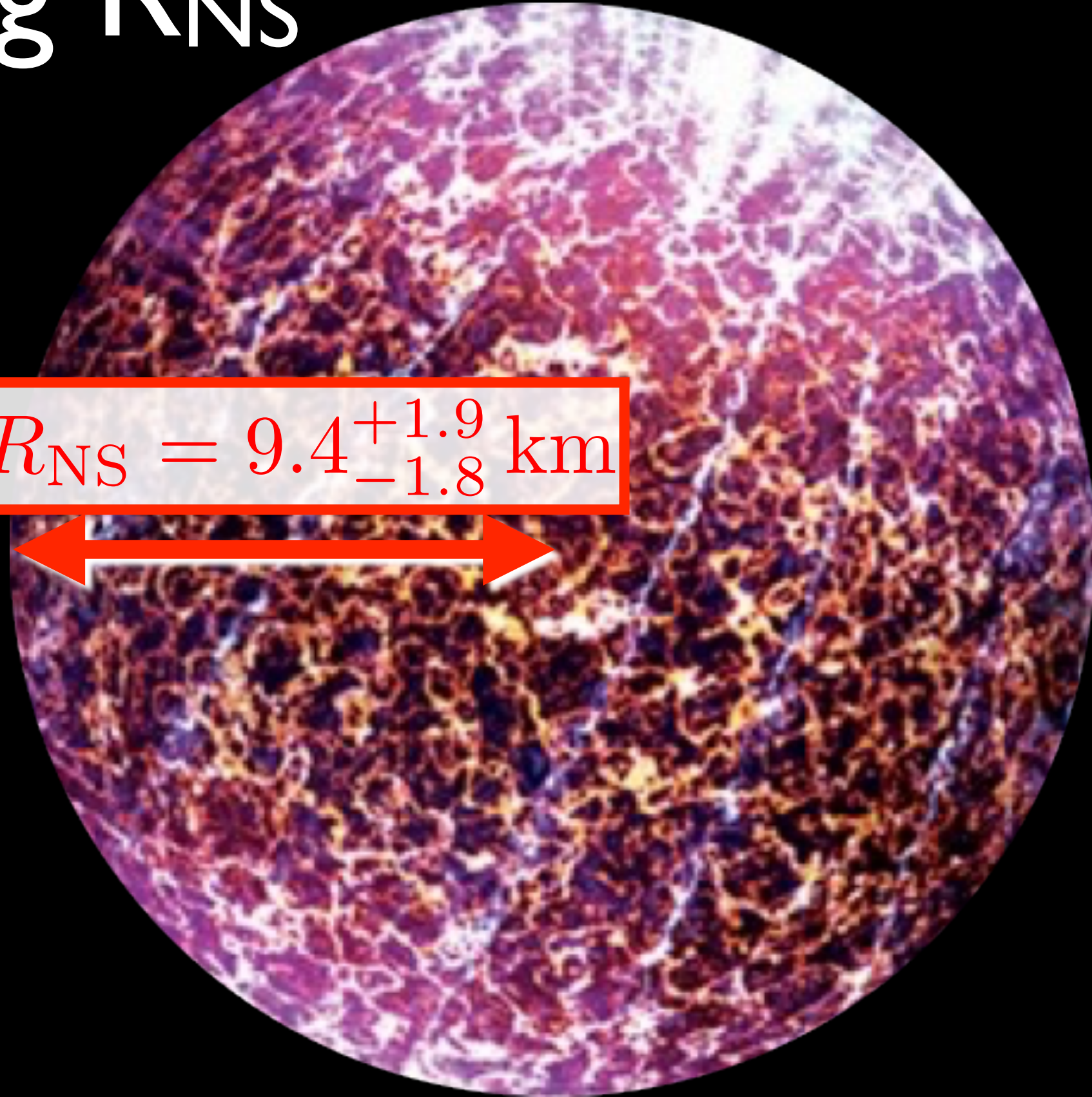
J. Margueron, N. Baillot-d'Étivaux

The nuclear matter equation of state is still unknown and many proposed theories exist.



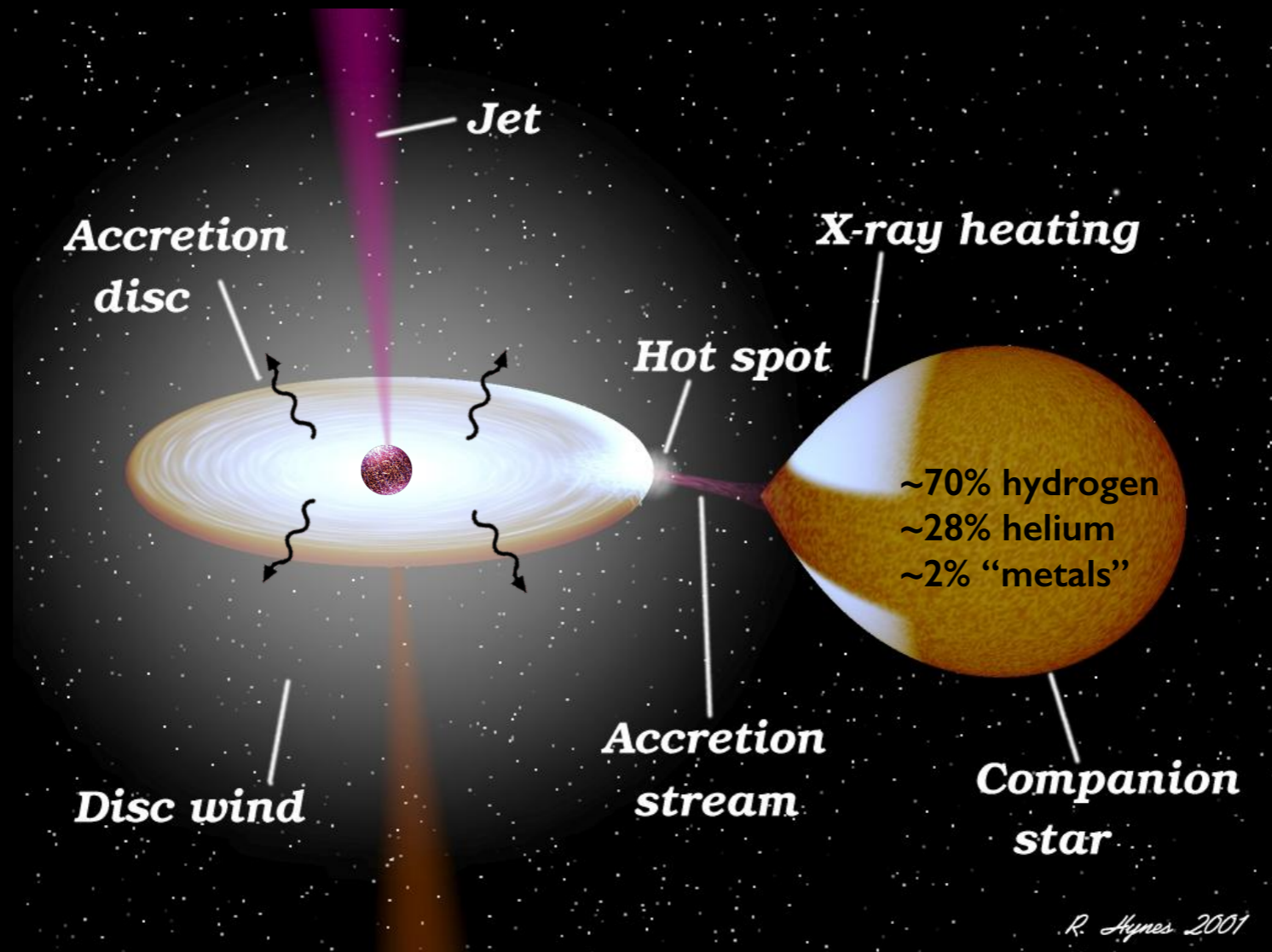
Measuring R_{NS}

Presented at
NuSYM 2013


$$R_{NS} = 9.4^{+1.9}_{-1.8} \text{ km}$$

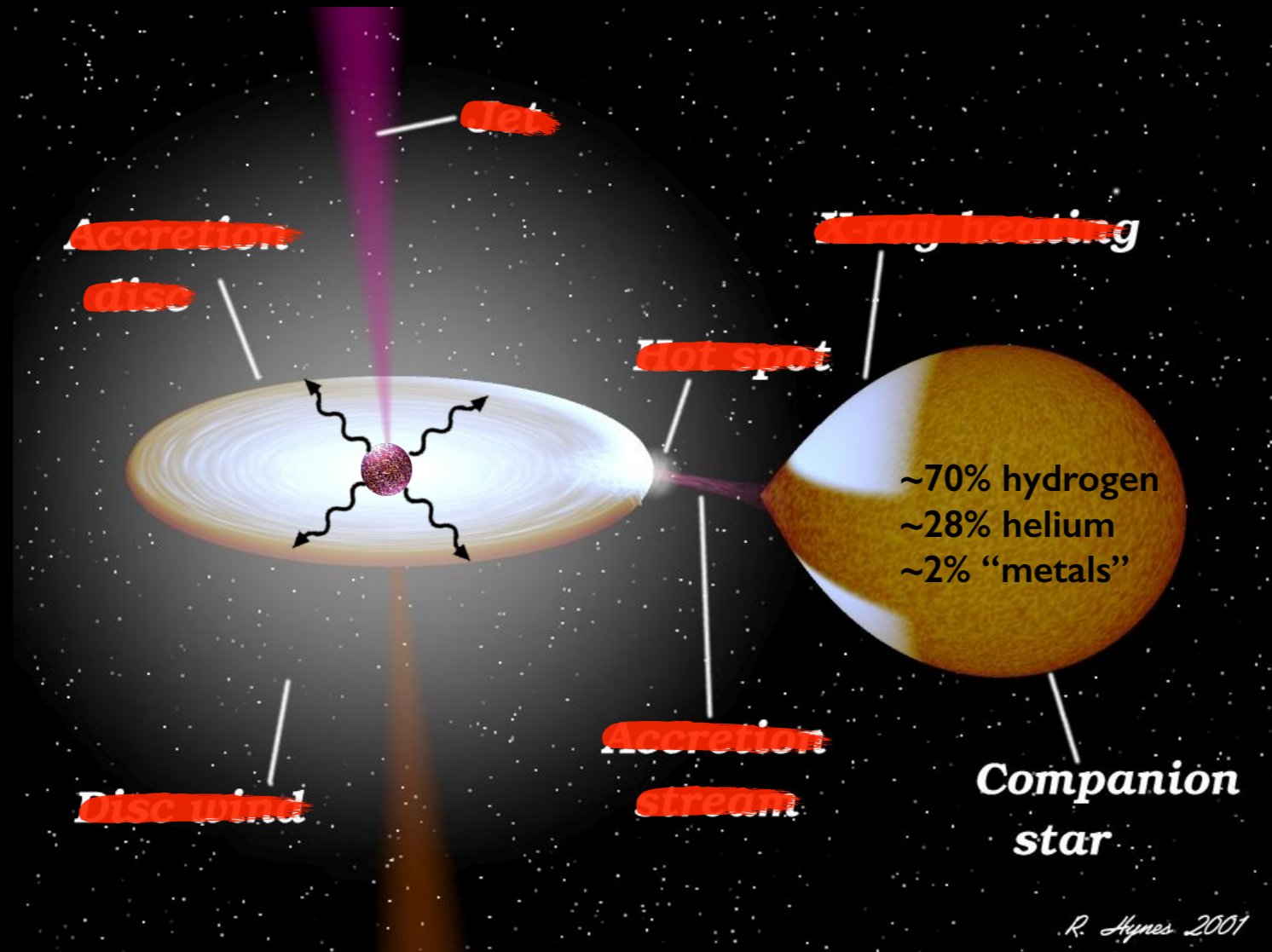
Guillot et al. 2013
Guillot & Rutledge 2014

Low-mass X-ray binaries experience high- and low-accretion states.



LMXB

Quiescent low-mass X-ray binaries are ideal systems for Mass-Radius measurements.

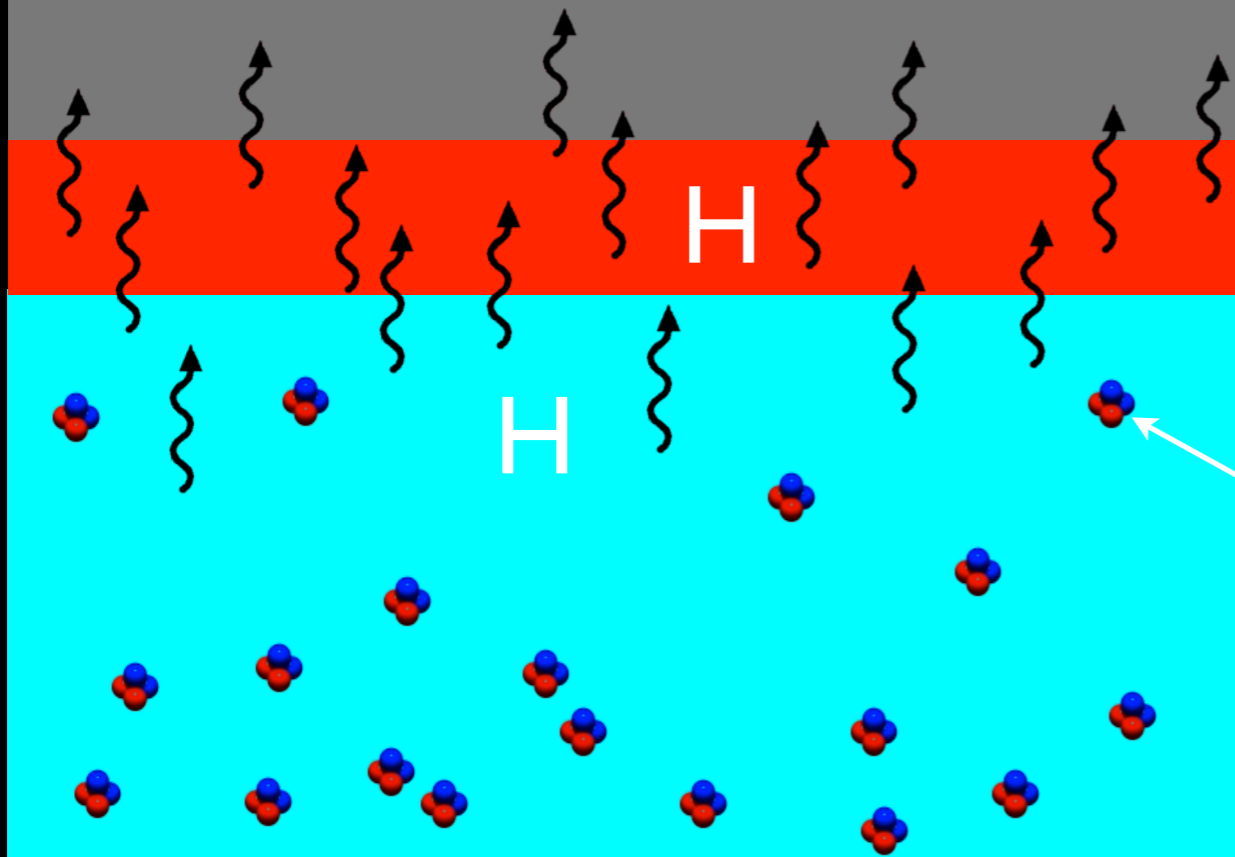


qLMXB

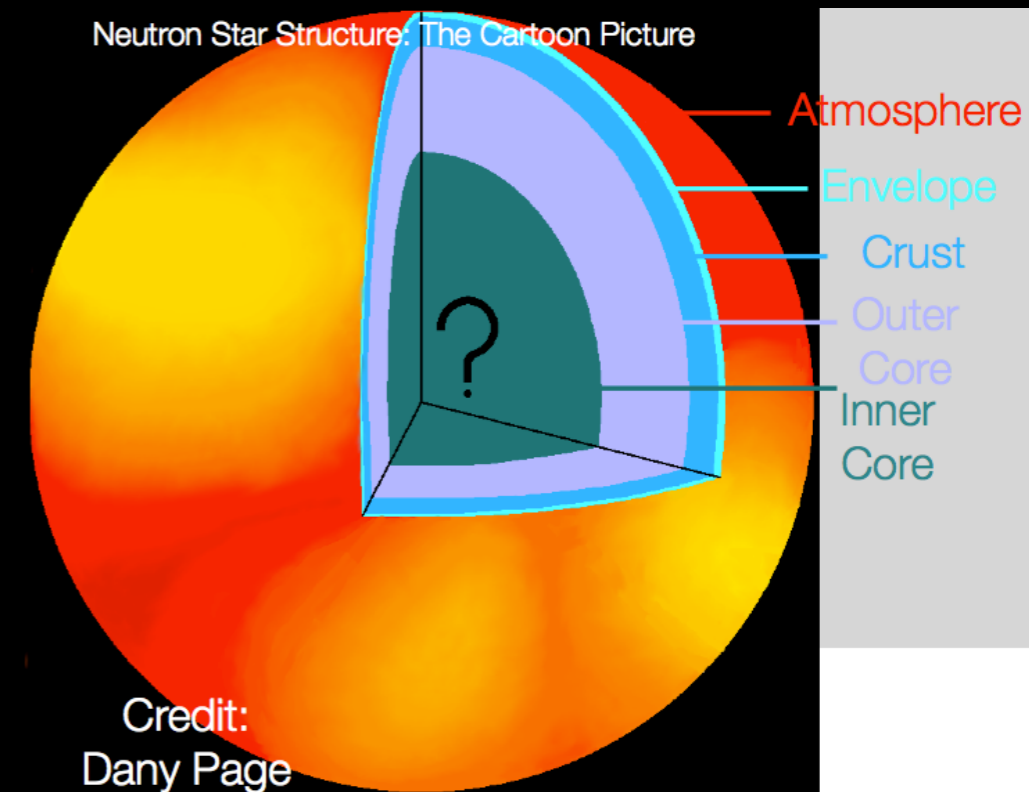
The atmosphere of the neutron star in a qLMXB is composed of pure hydrogen.


H-atmosphere
thermal emission
seen by observer

Gravity

Neutron Star Structure: The Cartoon Picture

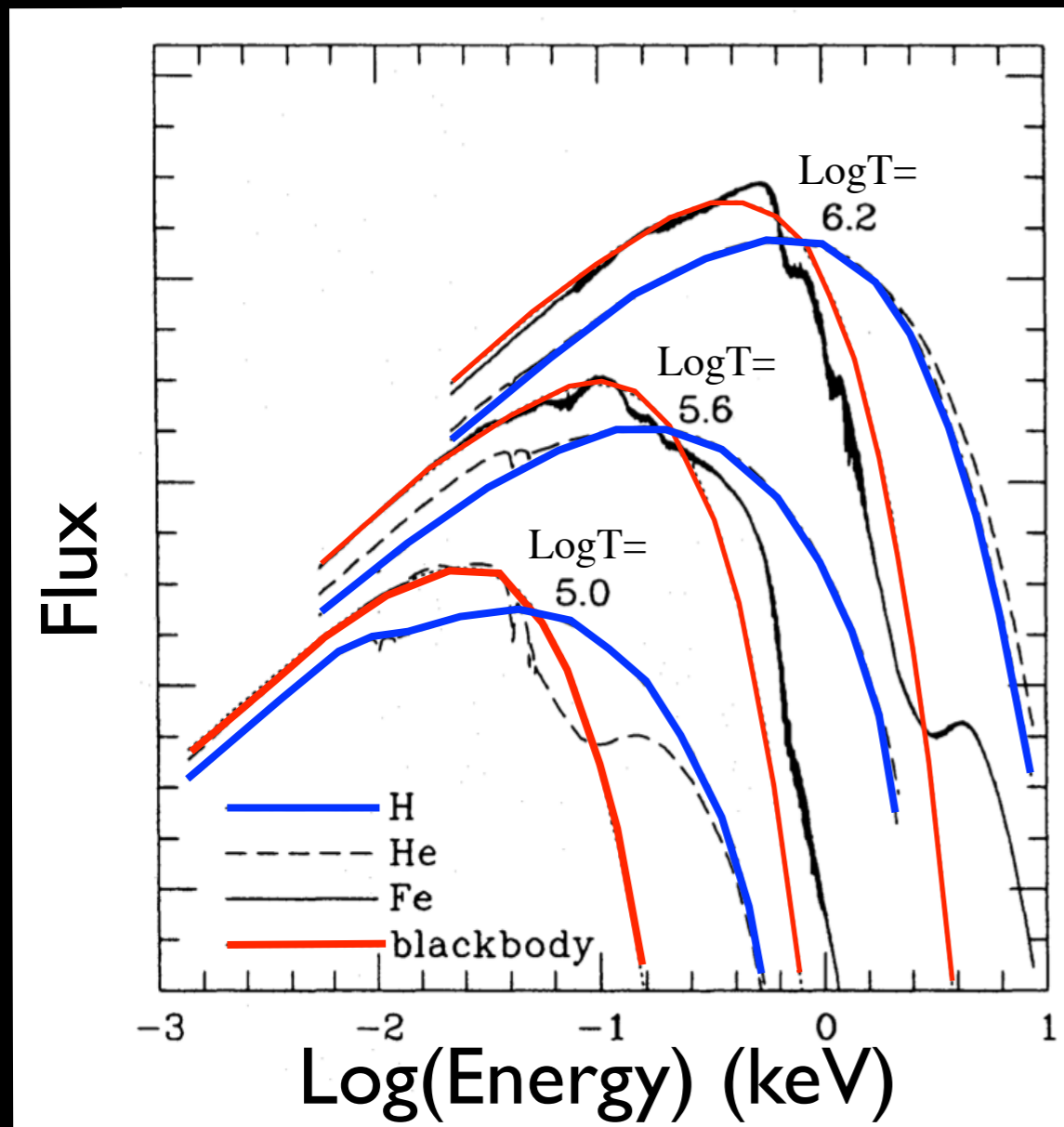


Photosphere \approx 1 cm

Helium


The thermal emission from a NS surface is modelled with non-magnetic NS atmosphere models.

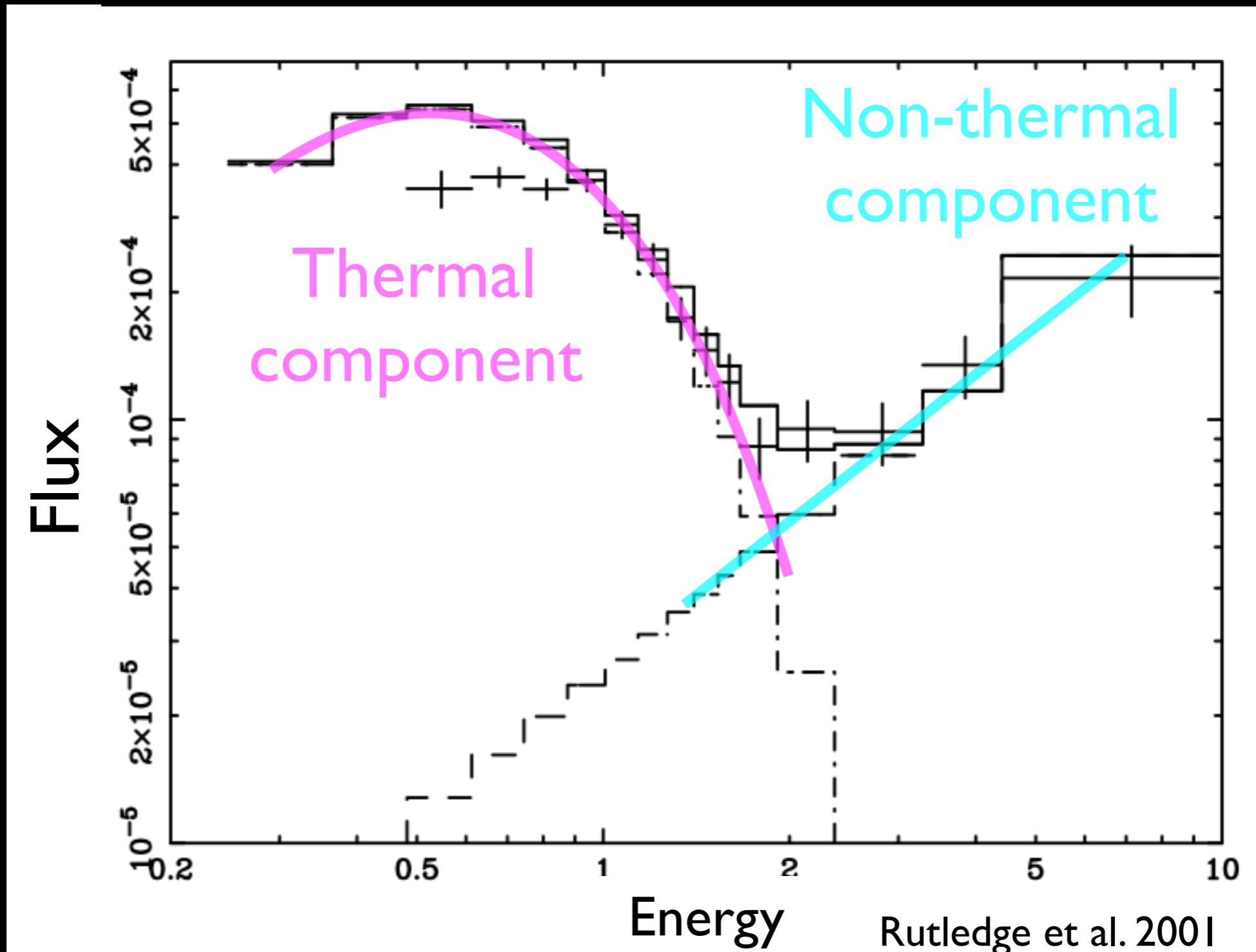
Models by Zavlin et al. (1996), Heinke et al. (2006), Haakonsen et al. (2012)



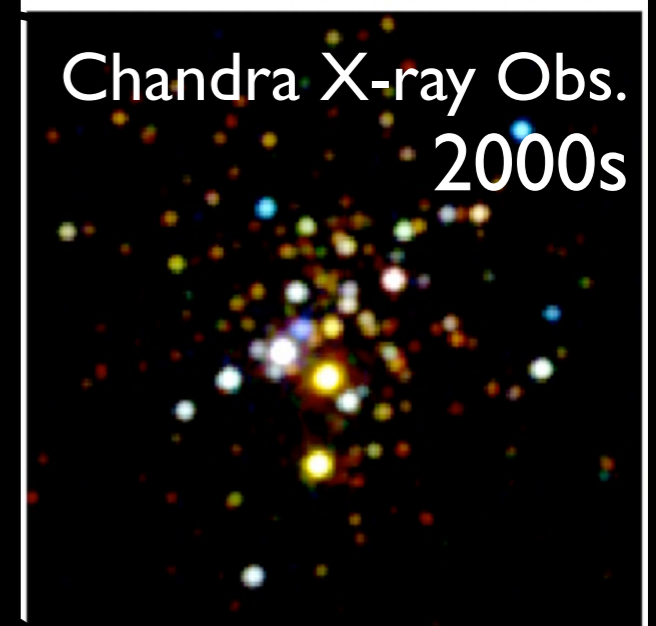
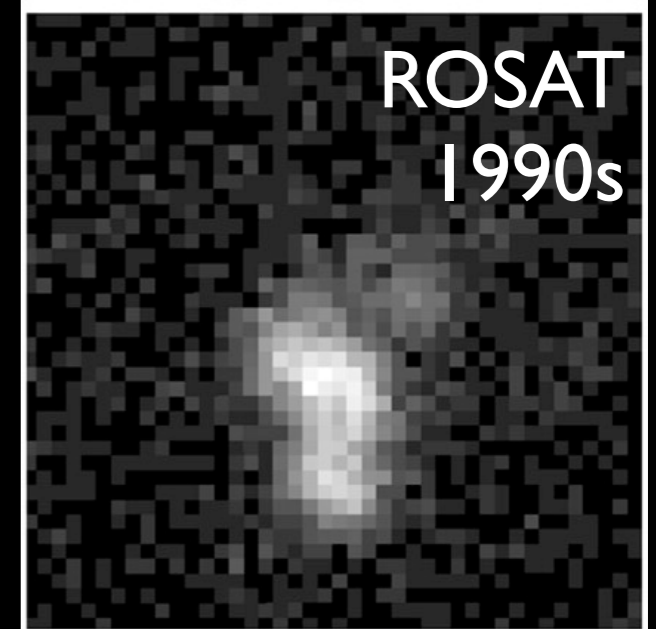
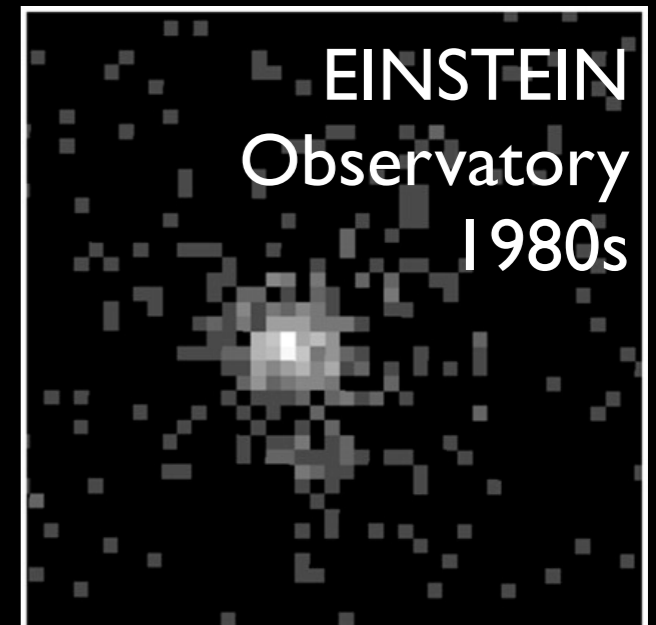
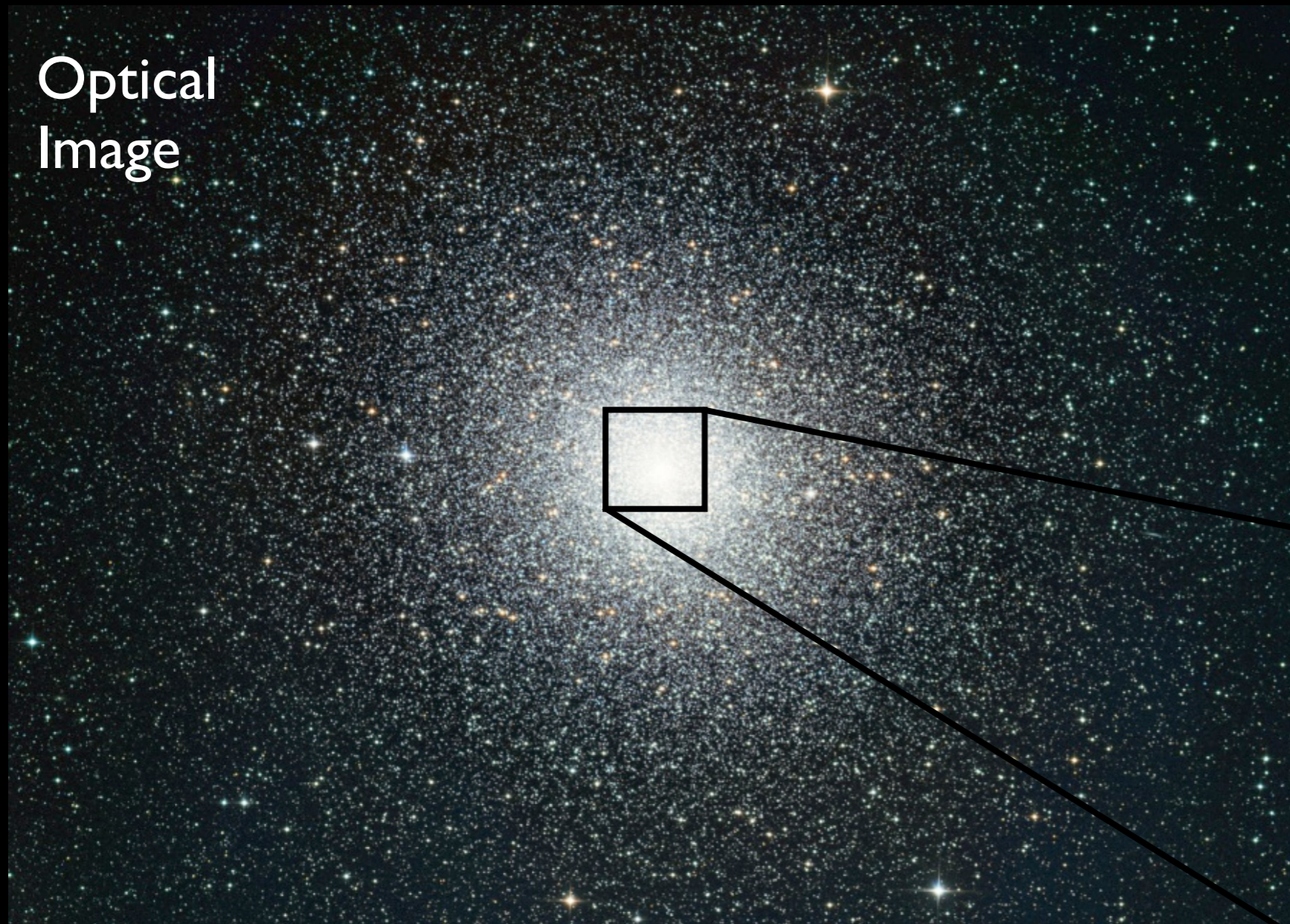
Spectral fitting of the thermal emission gives us T_{eff} and $F_X \propto (R_\infty/D)^2$

$$R_\infty = R_{\text{NS}} (1 + z) = R_{\text{NS}} \left(1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$

The first R_{NS} measurement was obtained from the known (bursting) field LMXB Cen X-4 observed during quiescence

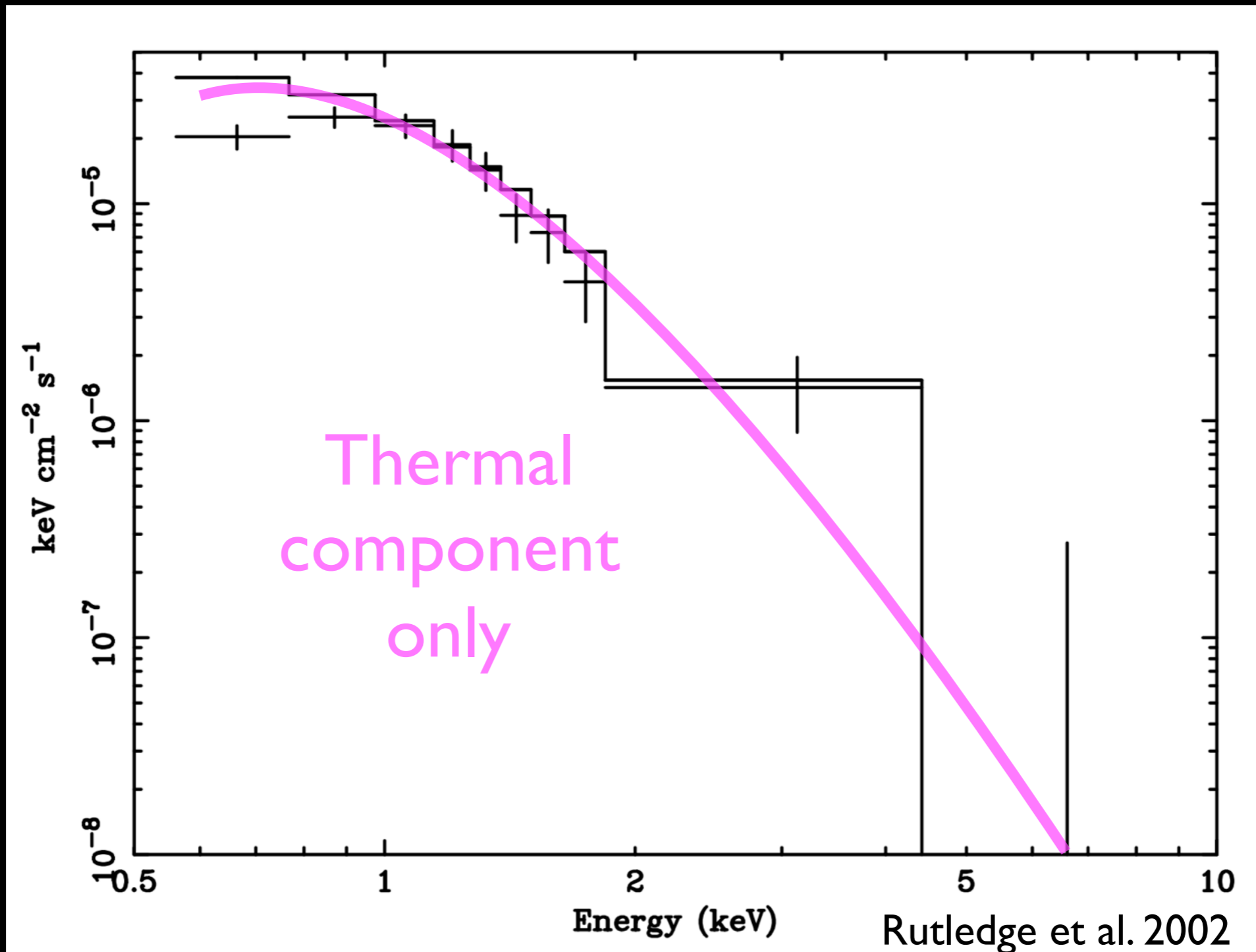


The solution consists in measuring R_{NS} from quiescent LMXBs hosted inside globular clusters

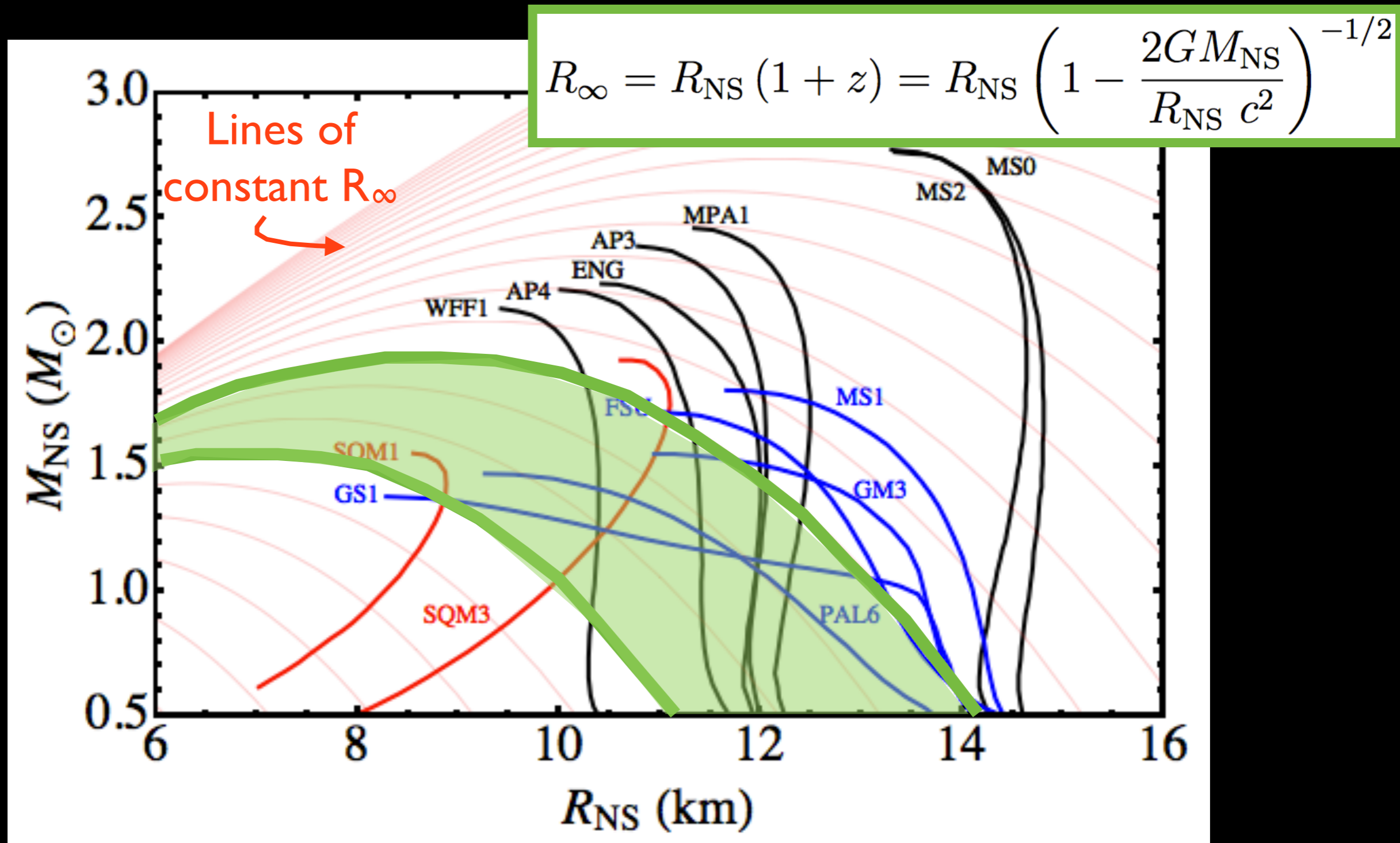


Curious about distances? Ask me!

The first globular cluster qLMXB was discovered in Omega Centauri

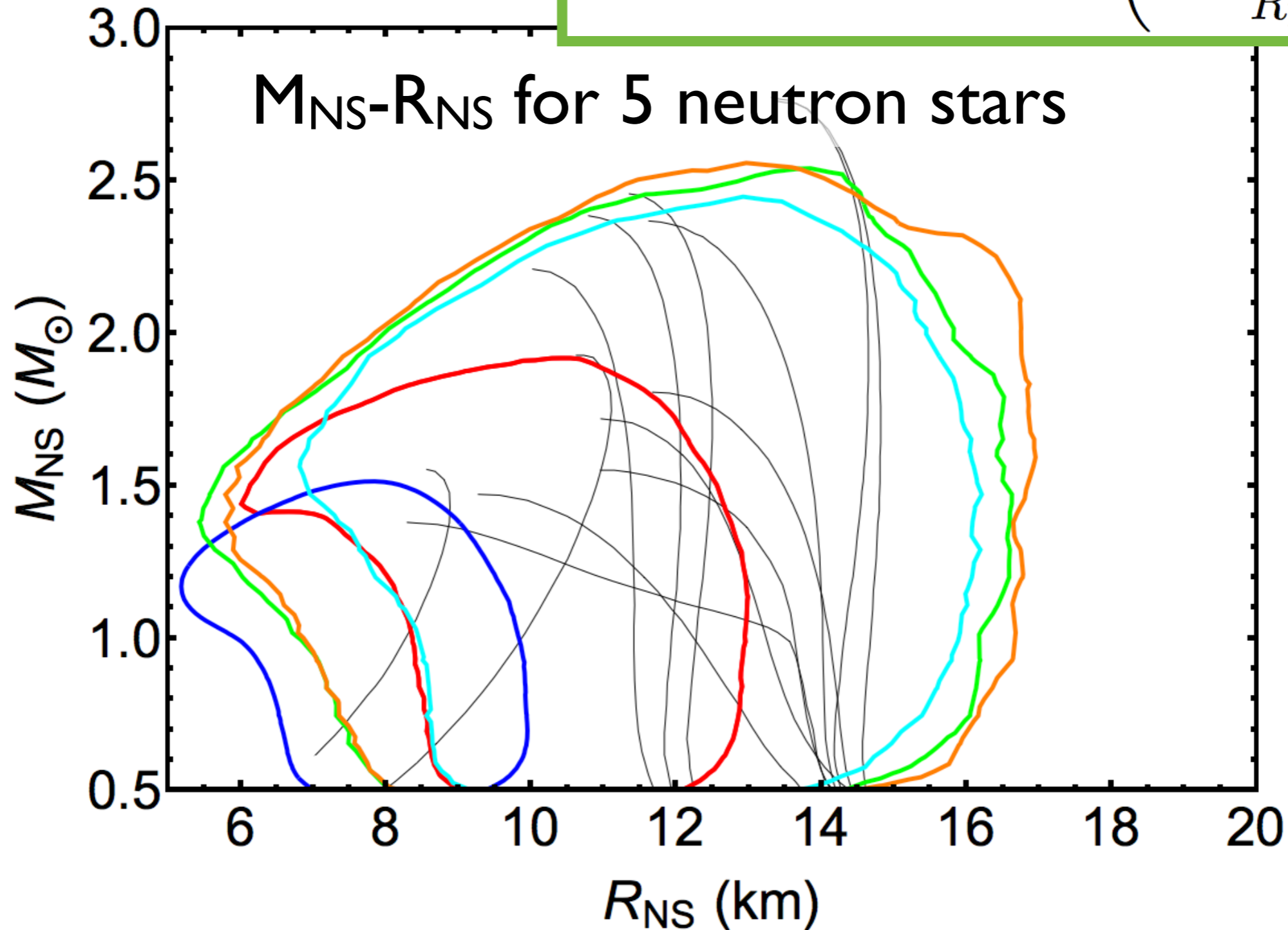


Quiescent LMXBs are routinely used for $M_{\text{NS}}-R_{\text{NS}}$ measurements, but only place weak constraints on the dense matter EoS.



Quiescent LMXBs are routinely used for $M_{\text{NS}}-R_{\text{NS}}$ measurements.

$$R_{\infty} = R_{\text{NS}} (1 + z) = R_{\text{NS}} \left(1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$



We simultaneously fitted the spectra of 6 qLMXBs with a H-atmosphere model.



One radius to fit them all!

Five parameters per target:

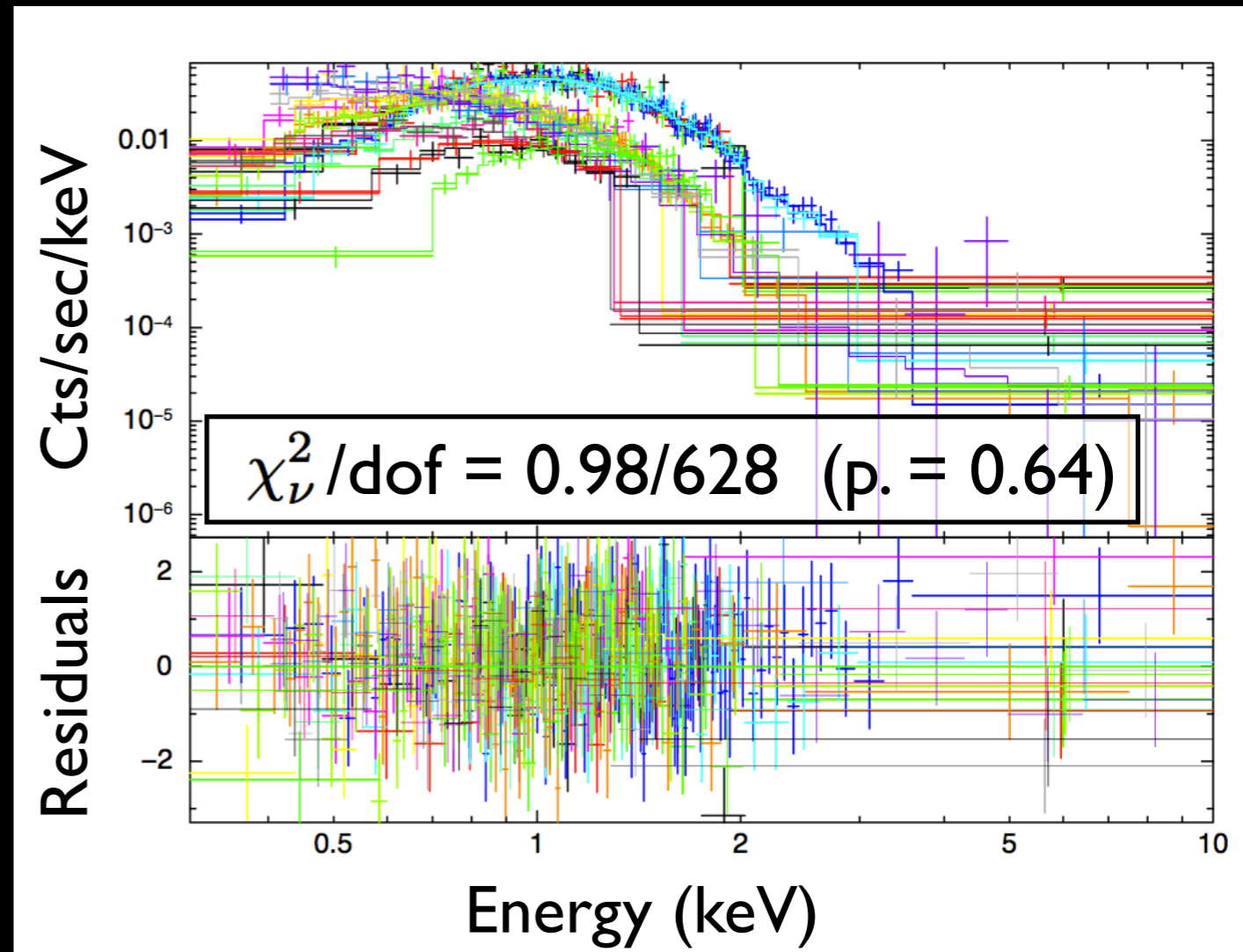
Temperature T_{eff}

Mass M_{NS}

Galactic absorption

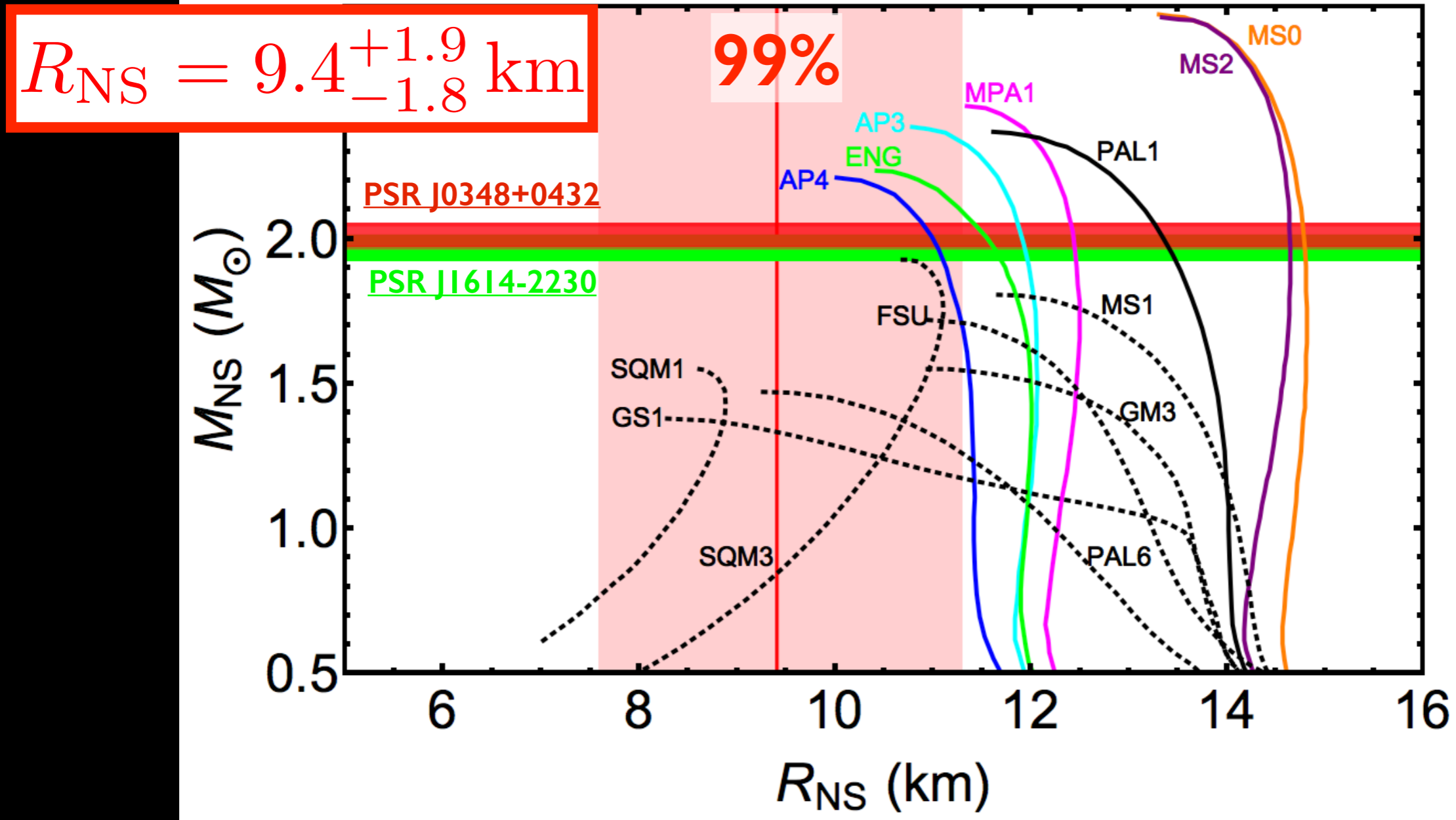
Distance of host GC

Power-law component



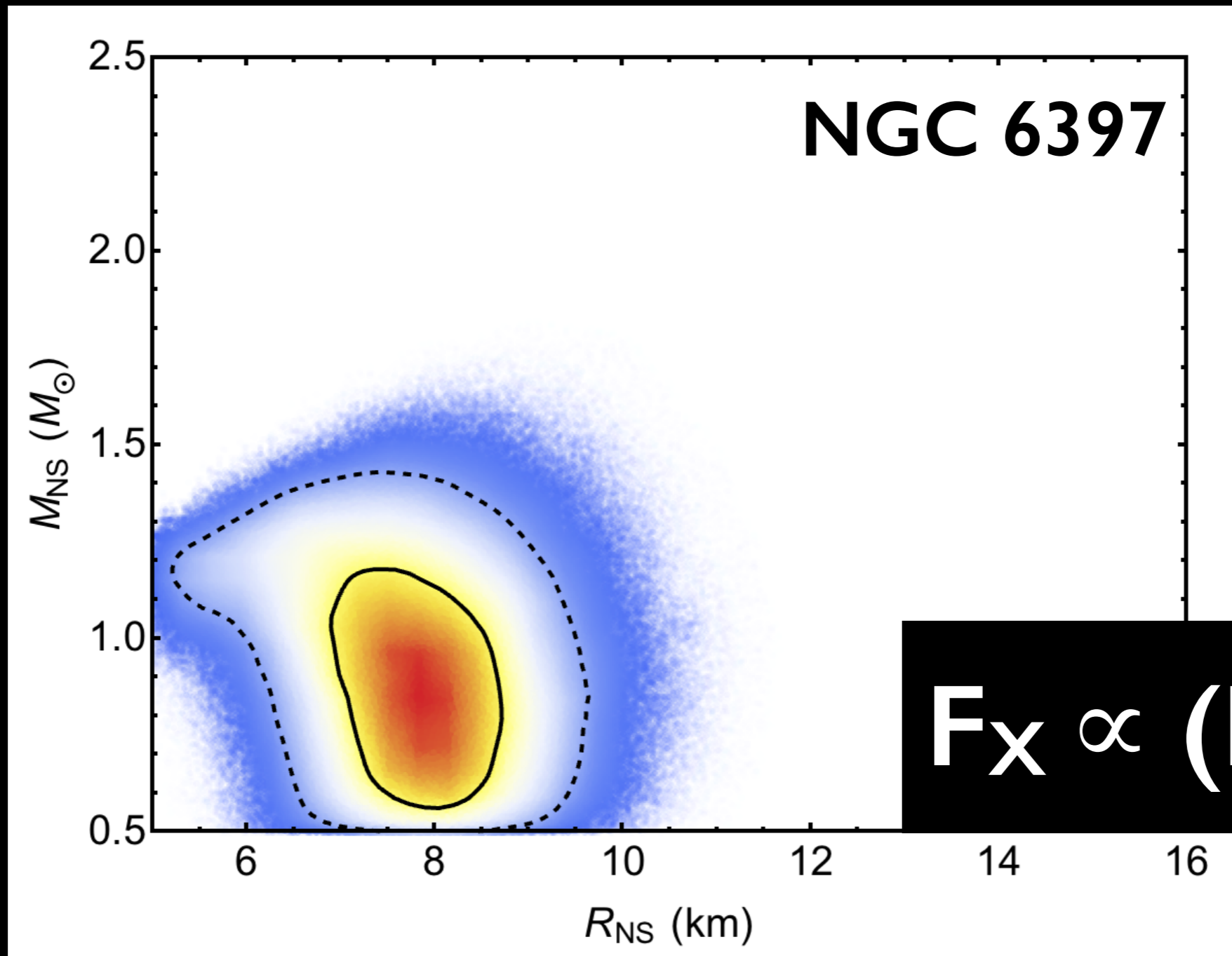
Spectral fitting with
Markov-Chain Monte-Carlo

If the EoS is “quasi-vertical” in $M_{\text{NS}}-R_{\text{NS}}$ space, our most conservative radius measurement provides constraints.



R_{NS} in the 7.6-11.3 km range at the 99%-confidence level

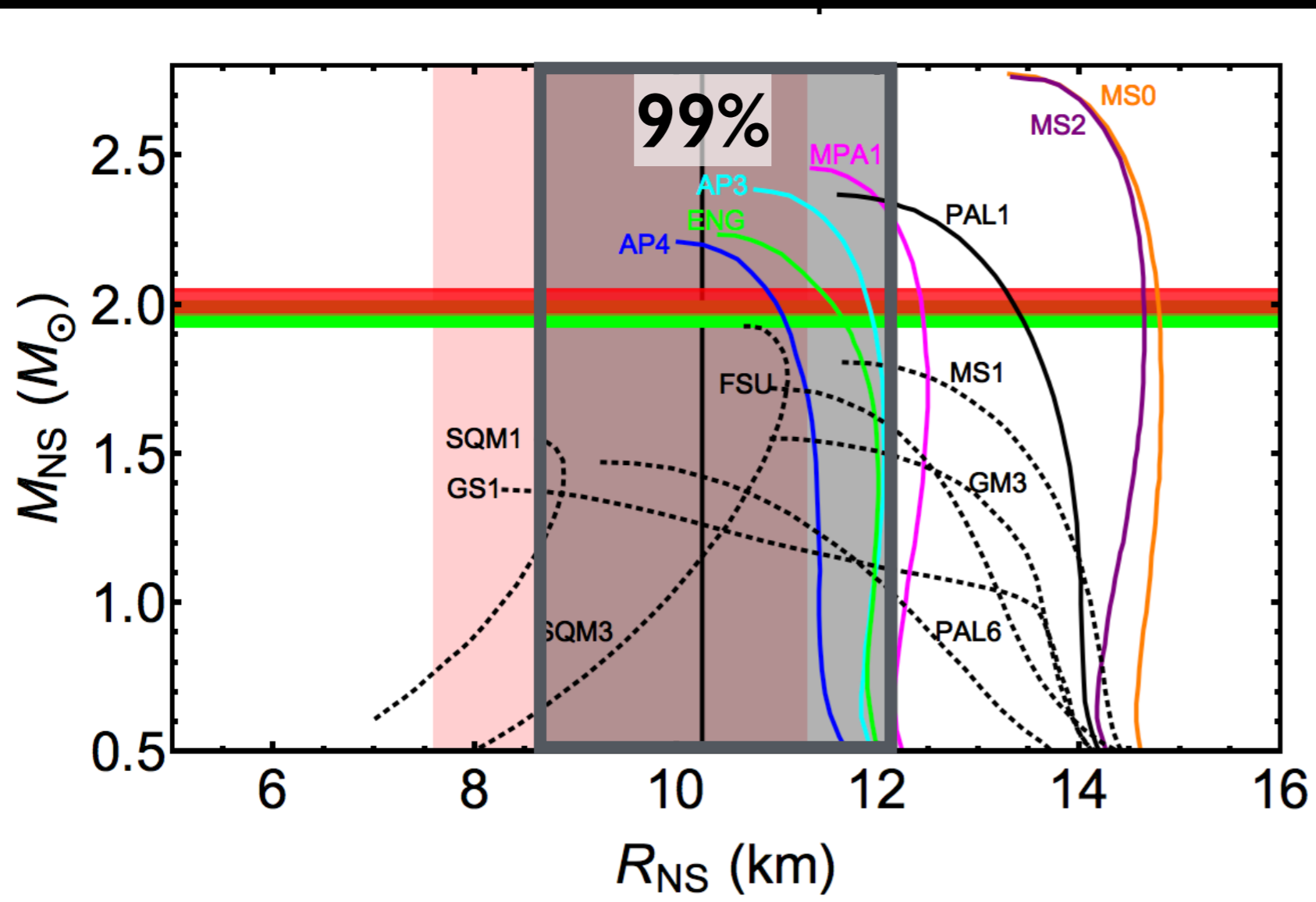
One of our 6 sources creates tension with the others.



$$F_X \propto (R_{\infty}/D)^2$$

Using recent distance measurements to the globular clusters, R_{NS} is increased by $\sim 10\%$.

$$F_X \propto (R_\infty/D)^2$$



Guillot & Rutledge 2014

$$R_{\text{NS}} = 9.4^{+1.9}_{-1.8} \text{ km}$$

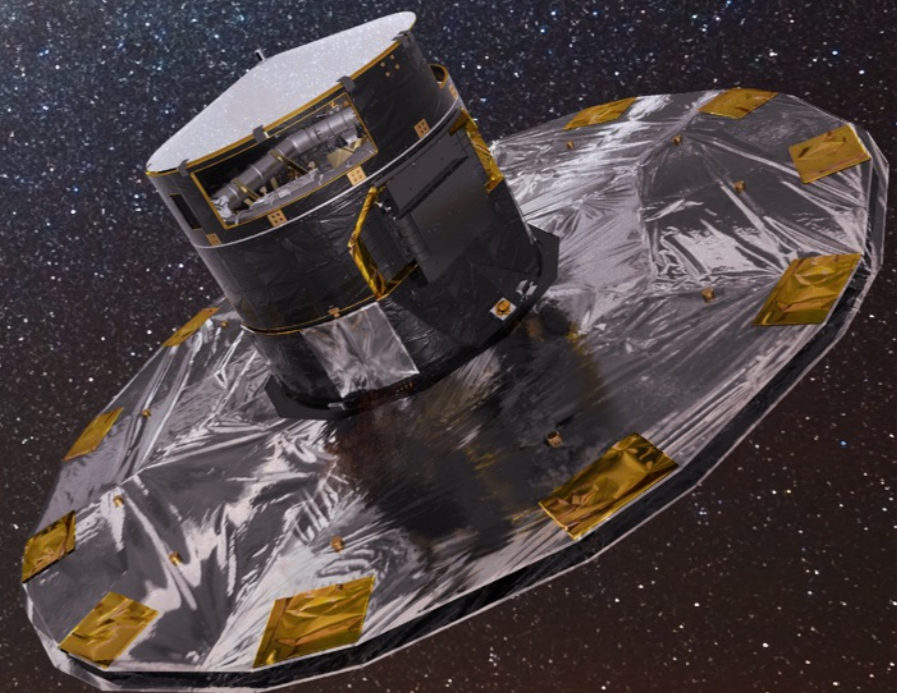
Same sources,
updated distances for M13,
NGC 6397 and ω Cen:

$$R_{\text{NS}} = 10.3^{+1.9}_{-1.7} \text{ km}$$

We are waiting for GAIA's data releases.

Property	Easy cluster	Difficult cluster	true (input) value
# of stars	16838	3513	—
μ_{RA}	$-4998.7 \pm 0.8 \mu\text{as/yr}$	$-4993 \pm 3 \mu\text{as/yr}$	$-5000 \mu\text{as/yr}$
μ_{Dec}	$-5000.2 \pm 0.7 \mu\text{as/yr}$	$-4994 \pm 3 \mu\text{as/yr}$	$-5000 \mu\text{as/yr}$
π	$199.7 \pm 0.7 \mu\text{as}$	$101.2 \pm 1.4 \mu\text{as}$	200/100 μas
D	$5.007 \pm 0.007 \text{ kpc}$	$9.997 \pm 0.017 \text{ kpc}$	5/10 kpc

Pancino et al., 2013



Other unknowns can bias the measurements of the neutron star radius, so we made some assumptions.

1 Negligible surface magnetic field

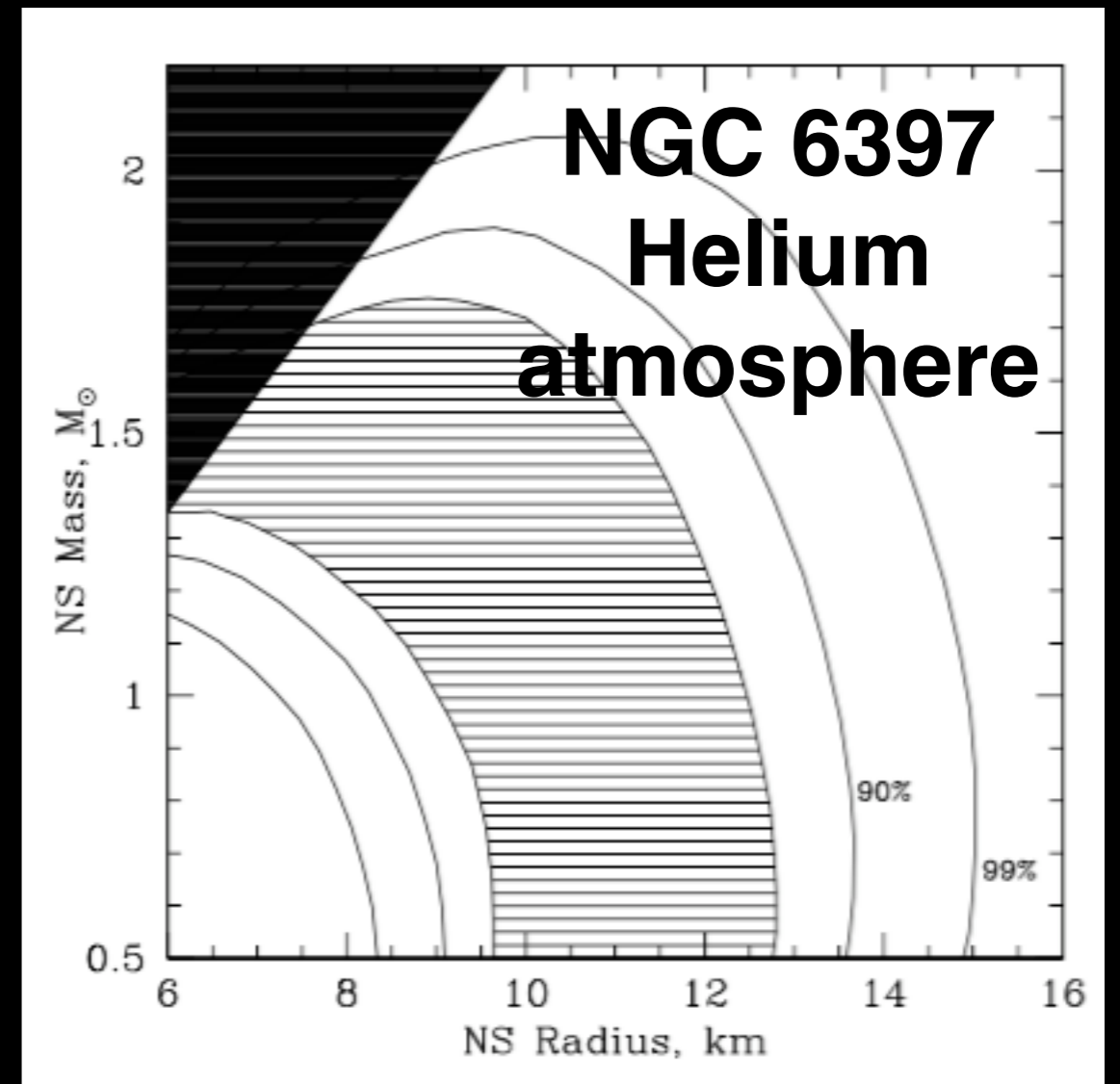
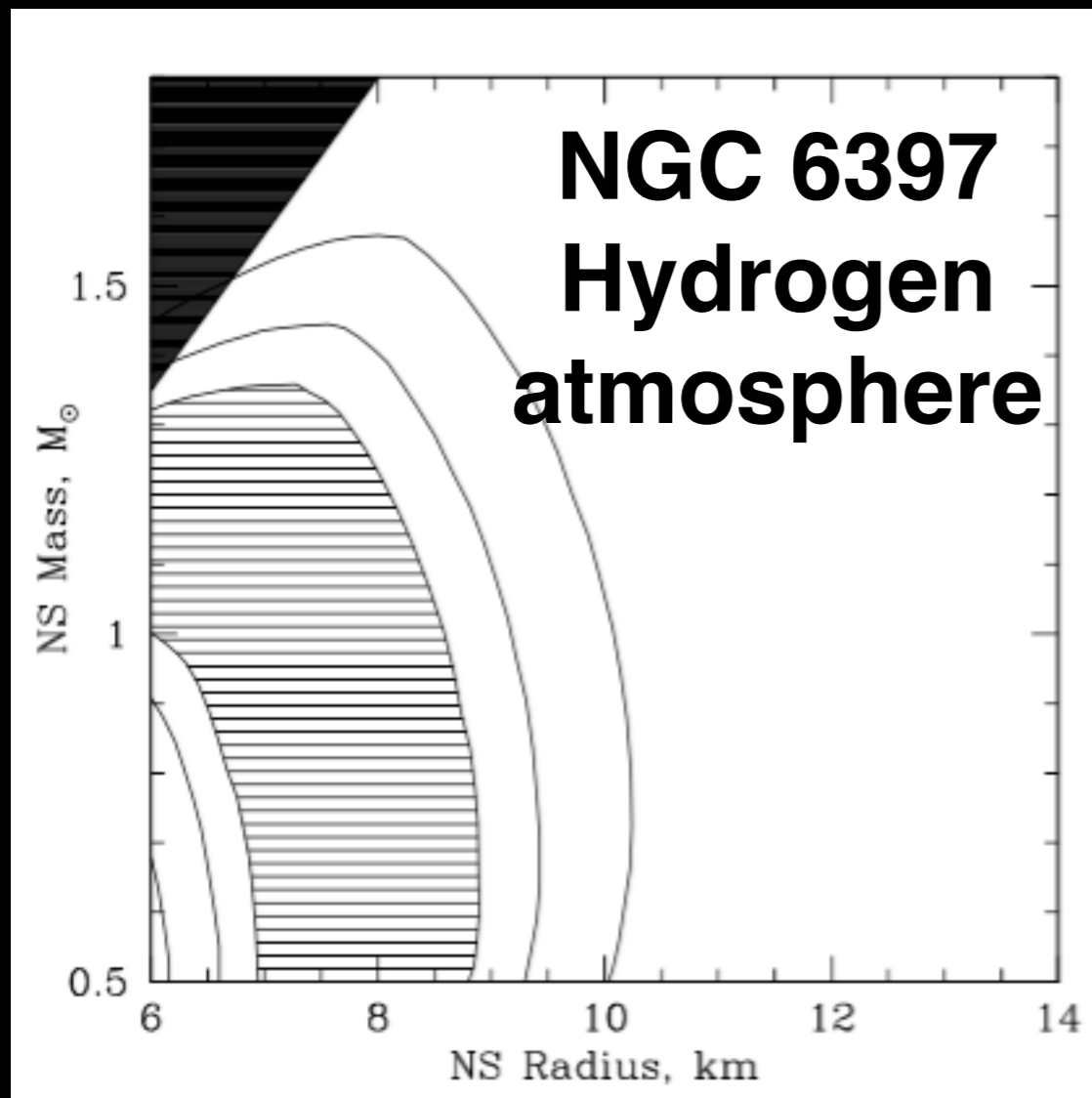
2 Calibration of the X-ray instruments

3 Isotropic neutron star surface emission

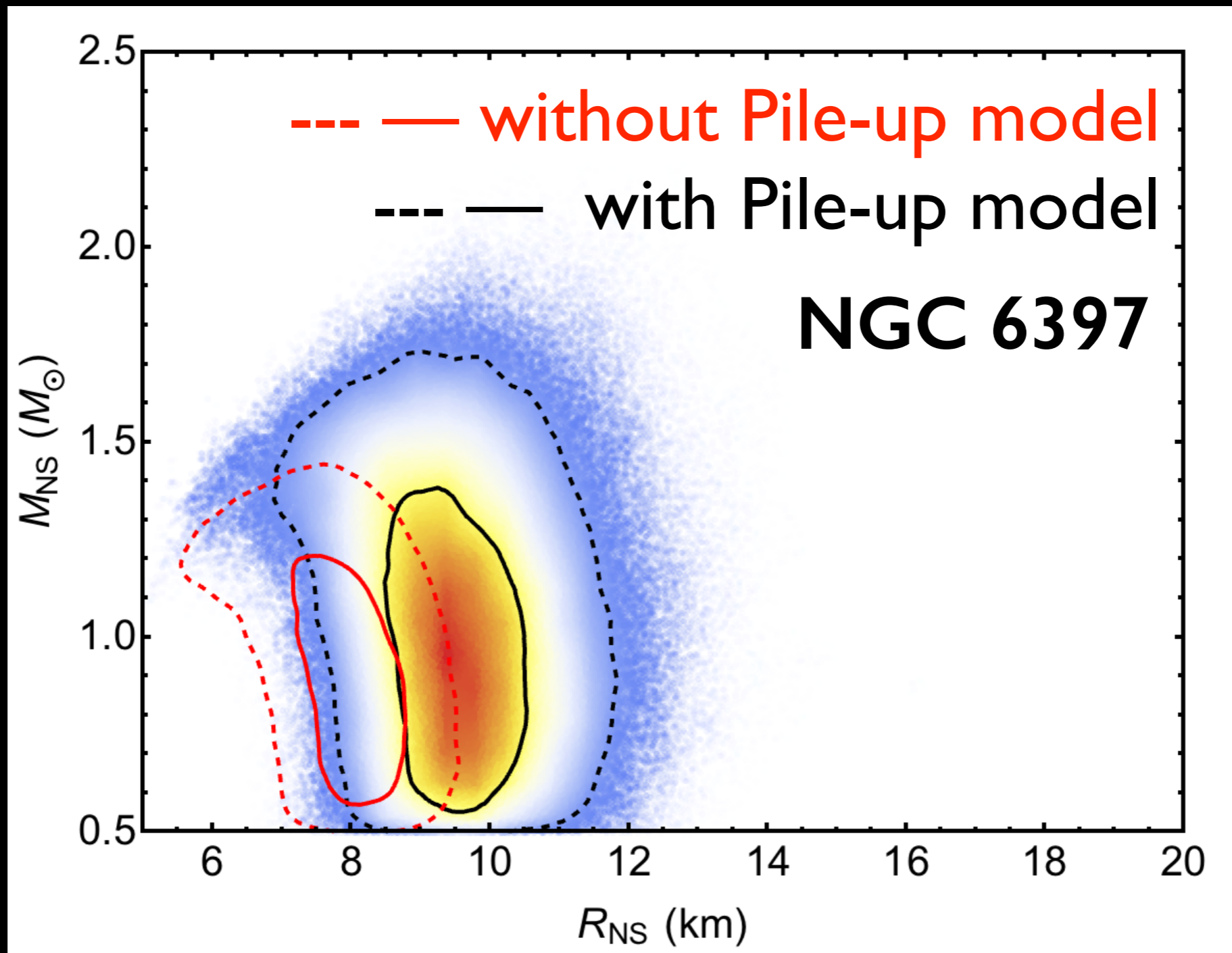
4 Slowly-rotating neutron stars

5 Composition of the neutron star atmosphere

The choice of NS atmosphere composition significantly changes the measured R_∞ , and therefore the $M_{\text{NS}}-R_{\text{NS}}$ contours.

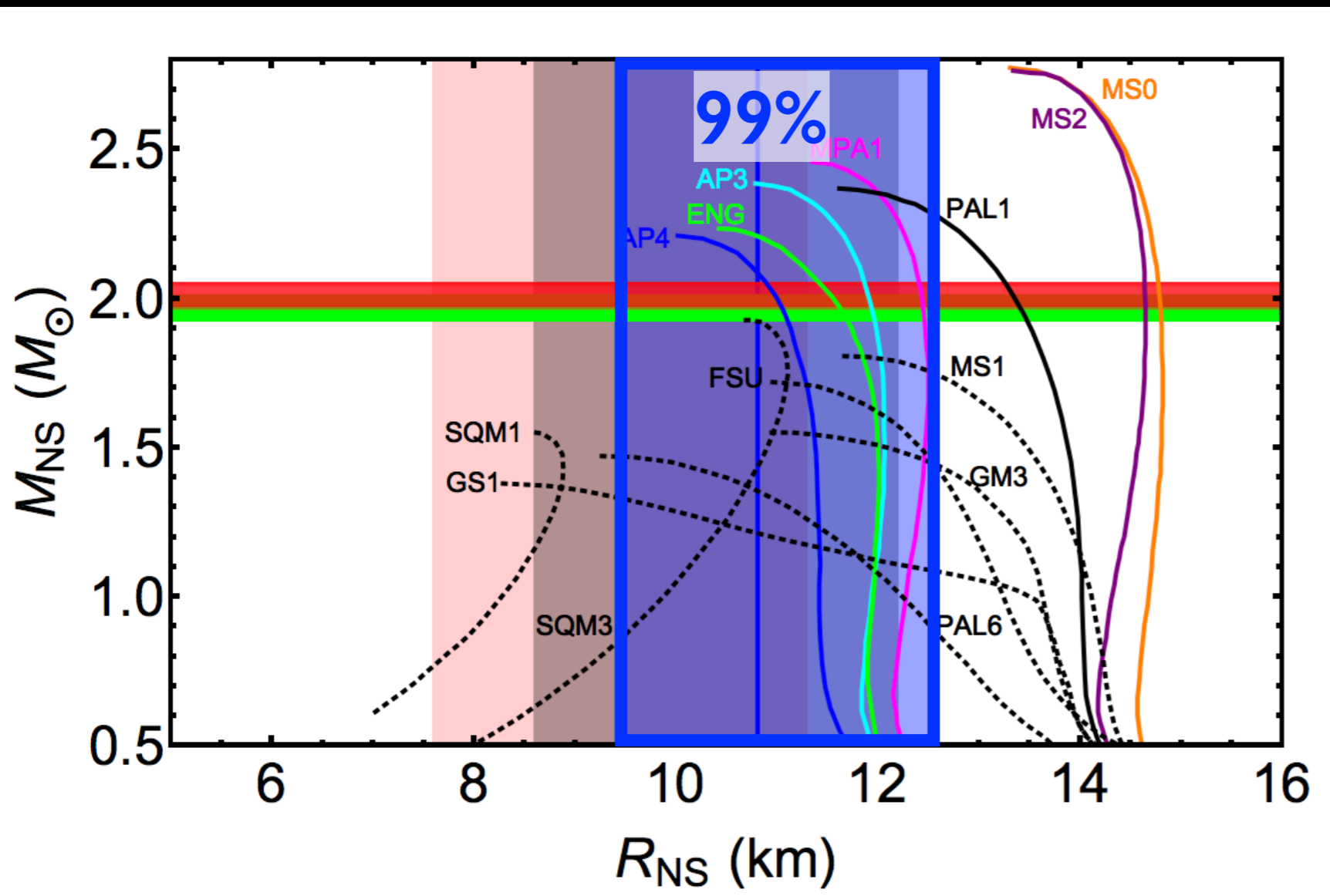


An instrumental effects (pile-up) is affecting the observed spectra of NGC 6397.



Curious about pile-up? Ask me!

The constant R_{NS} solution moves up a bit more when pile-up modelling is included.



Guillot & Rutledge 2014

$$R_{\text{NS}} = 9.4^{+1.9}_{-1.8} \text{ km}$$

Updated distances

$$R_{\text{NS}} = 10.3^{+1.9}_{-1.7} \text{ km}$$

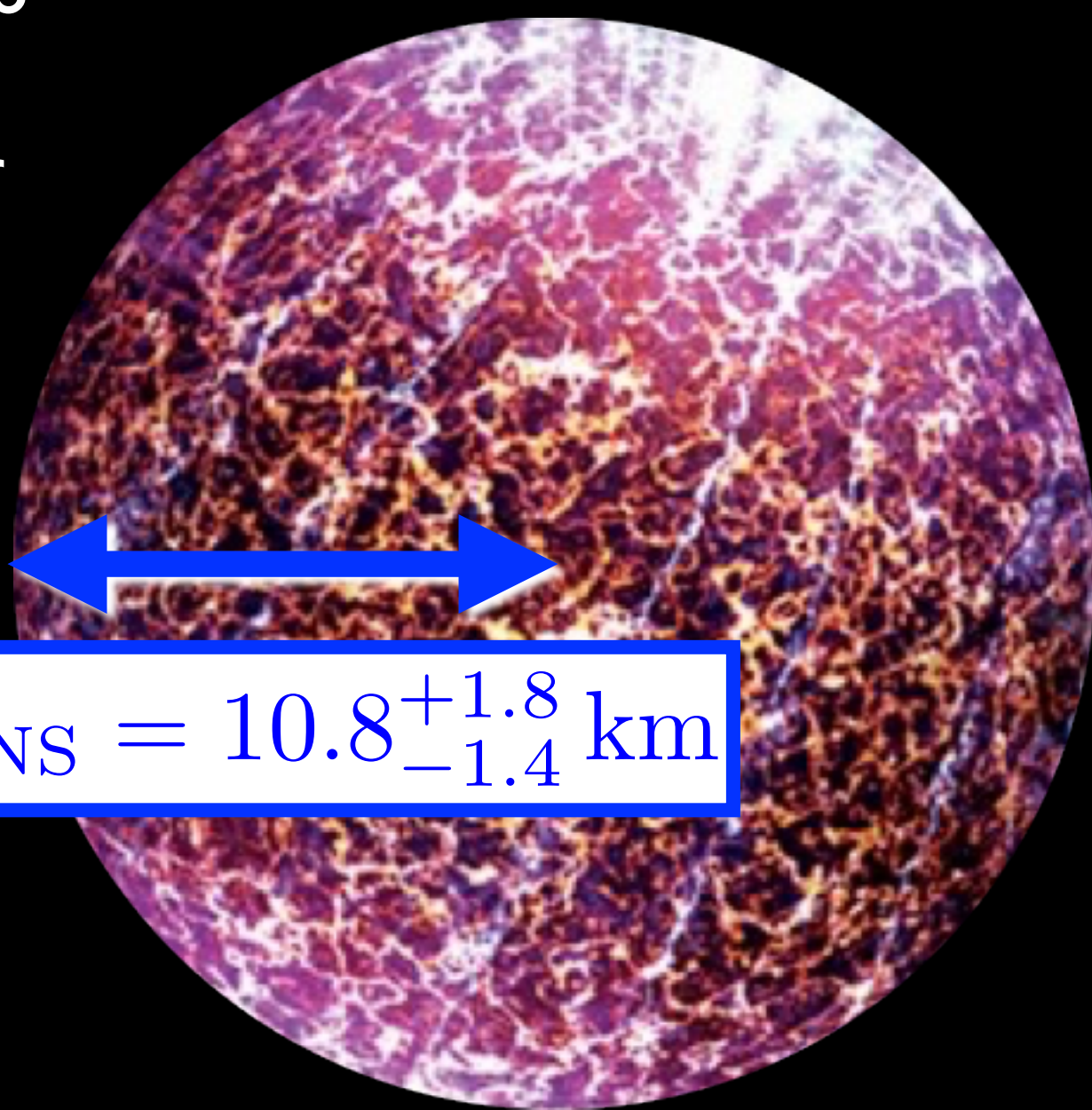
With Pile-up model

$$R_{\text{NS}} = 10.8^{+1.8}_{-1.4} \text{ km}$$

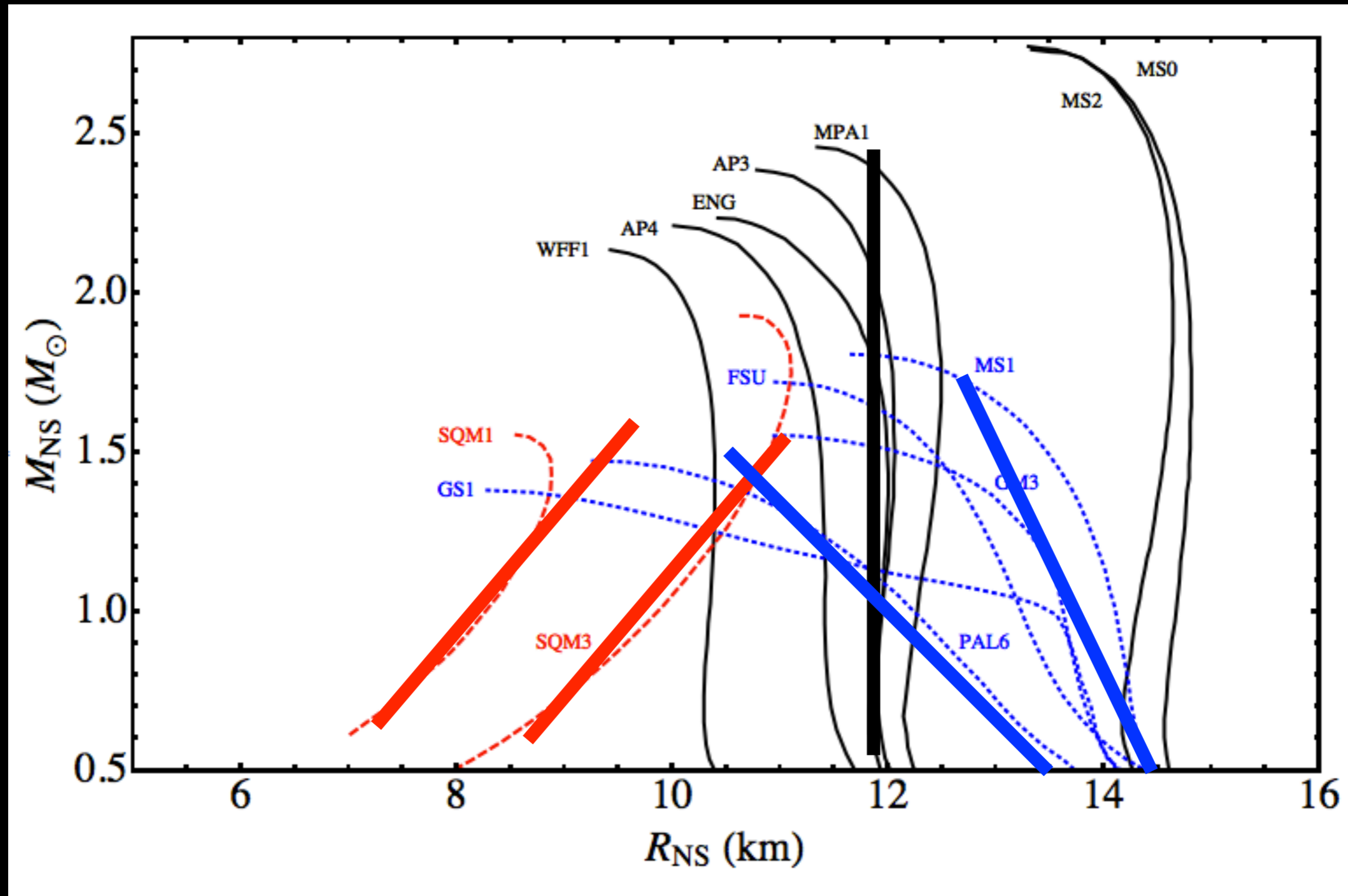
Measuring R_{NS}

Using a Markov-Chain Monte Carlo method to fit the X-ray spectra of 6 neutron stars, assuming:

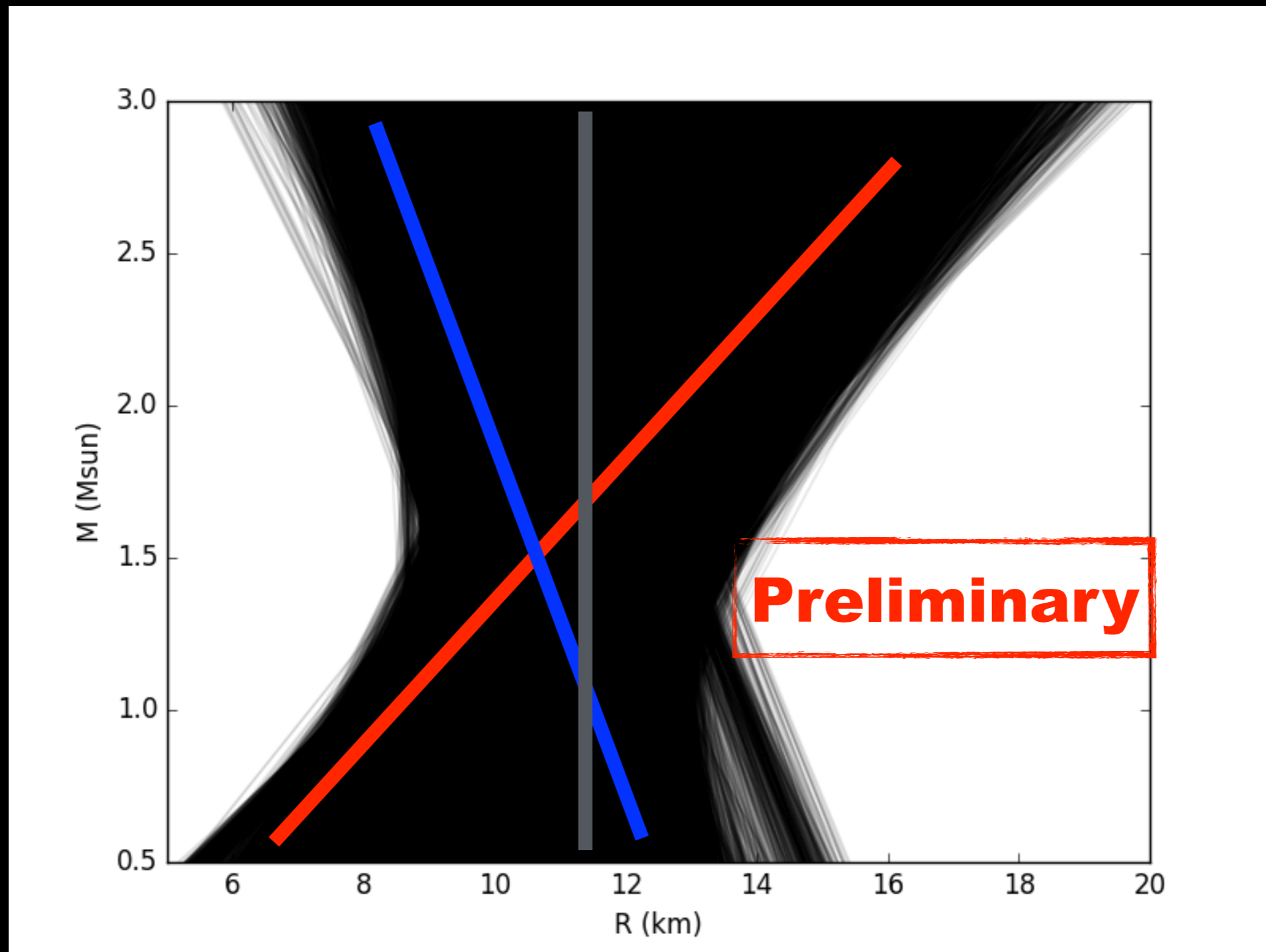
- their atmosphere is composed of pure hydrogen,
- the radius is the same for all neutron stars.


$$R_{NS} = 10.8^{+1.8}_{-1.4} \text{ km}$$

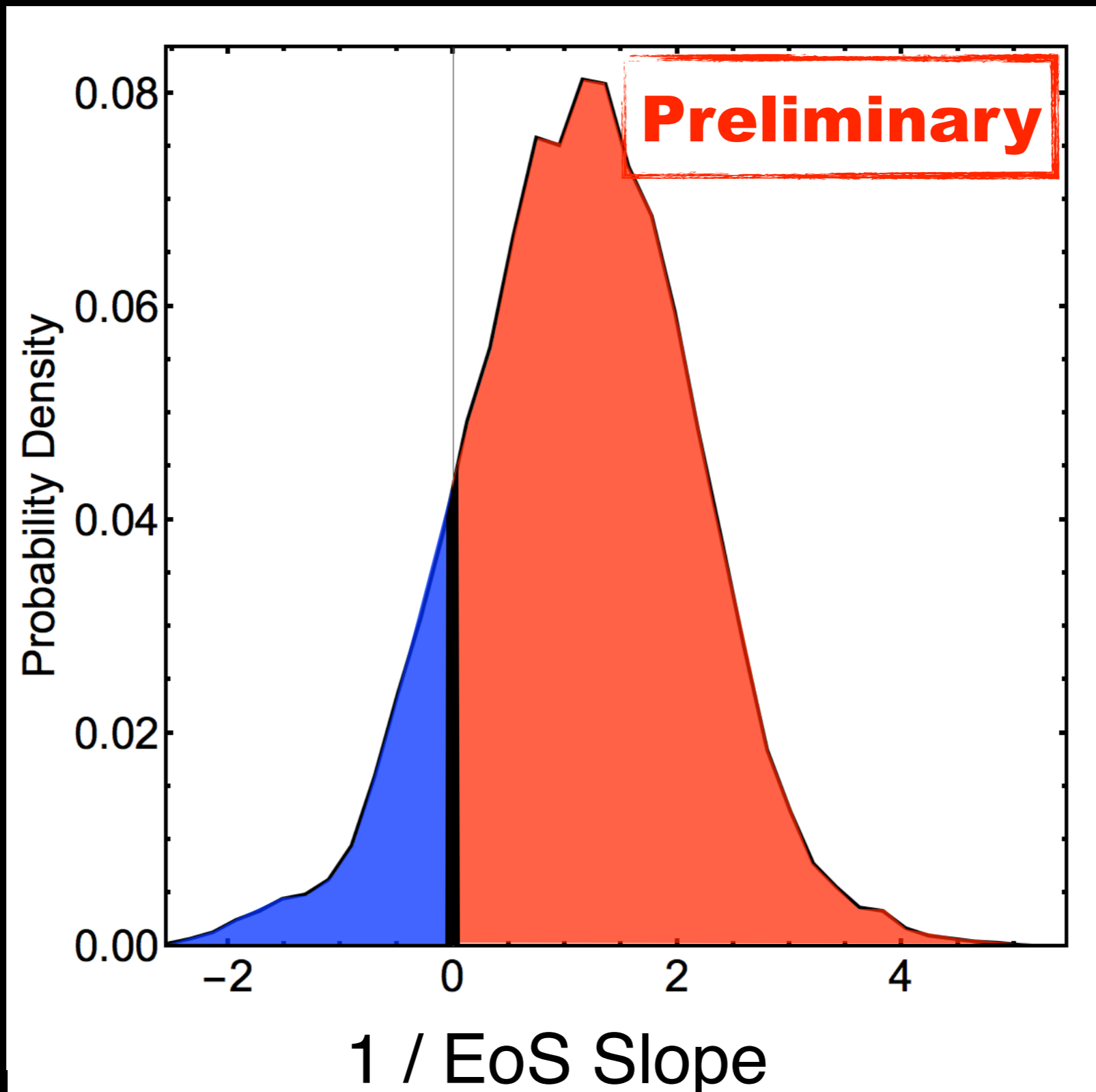
Using the same MCMC approach, I can also test a “*more advanced*” toy-model.



This MCMC approach is used to sample the parameter space of straight EOS.



The distribution of EoS slightly favours positive slopes, but not significantly.



There are several complementary ways to improve constraints on the equation of state from qLMXBs observations.

Deeper X-ray observations to increase the signal-to-noise of the X-ray spectra

More precise distance measurements of the host stellar clusters

Determine the composition of the neutron star atmosphere

Independent measurement of neutron star mass

Use of realistic parameterizations of the equation of state.
See [*Ozel et al. 2016*](#)
and [*Lattimer and Steiner 2014*](#)

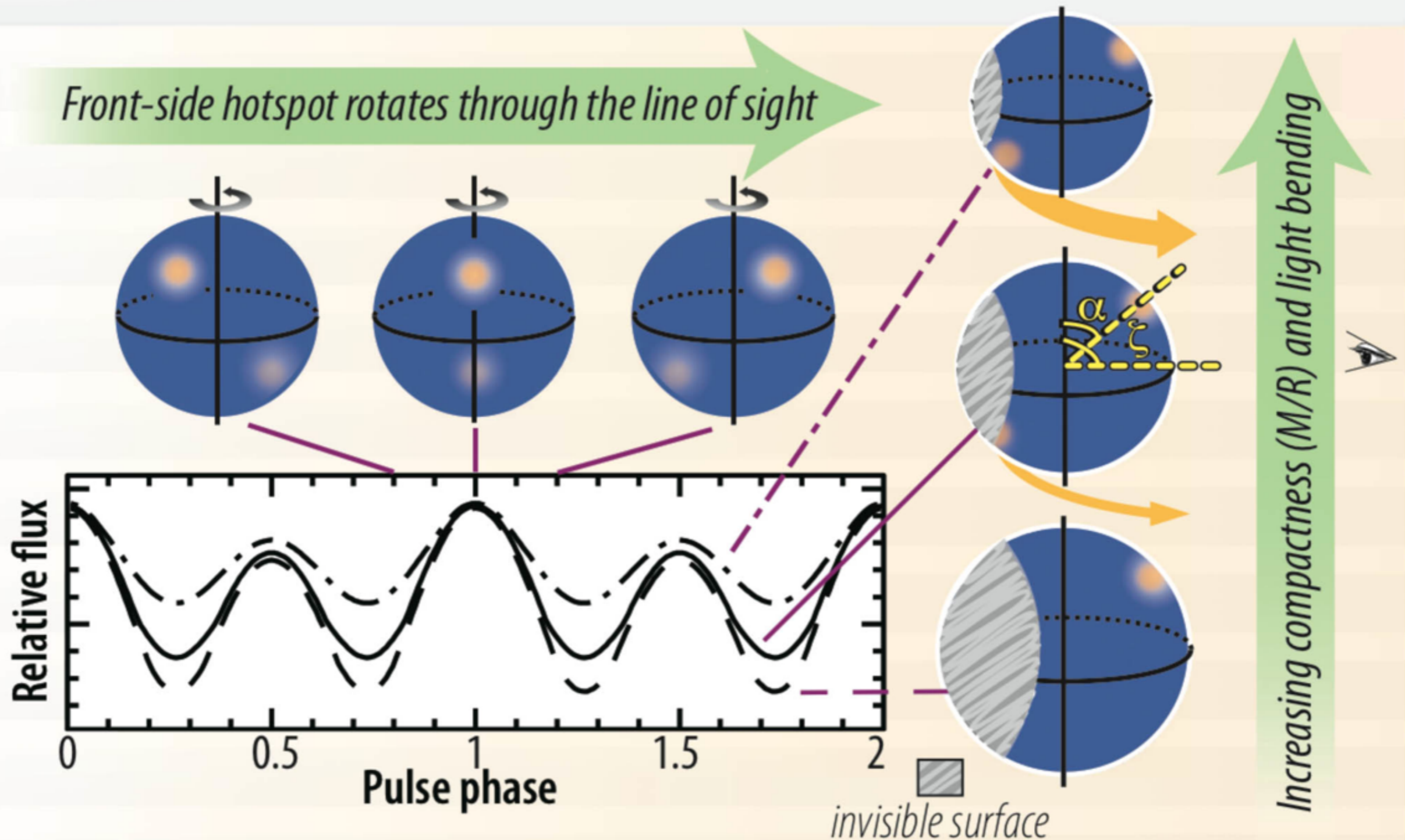
Curious about [*Lattimer and Steiner \(2014\)*](#)? Ask me!

Another method to
measure $M_{\text{NS}}/R_{\text{NS}}$

with a different class of neutron stars.

Analyzing the pulsed emission caused by hot spots on a rotating neutron star can be used to measure the compactness.

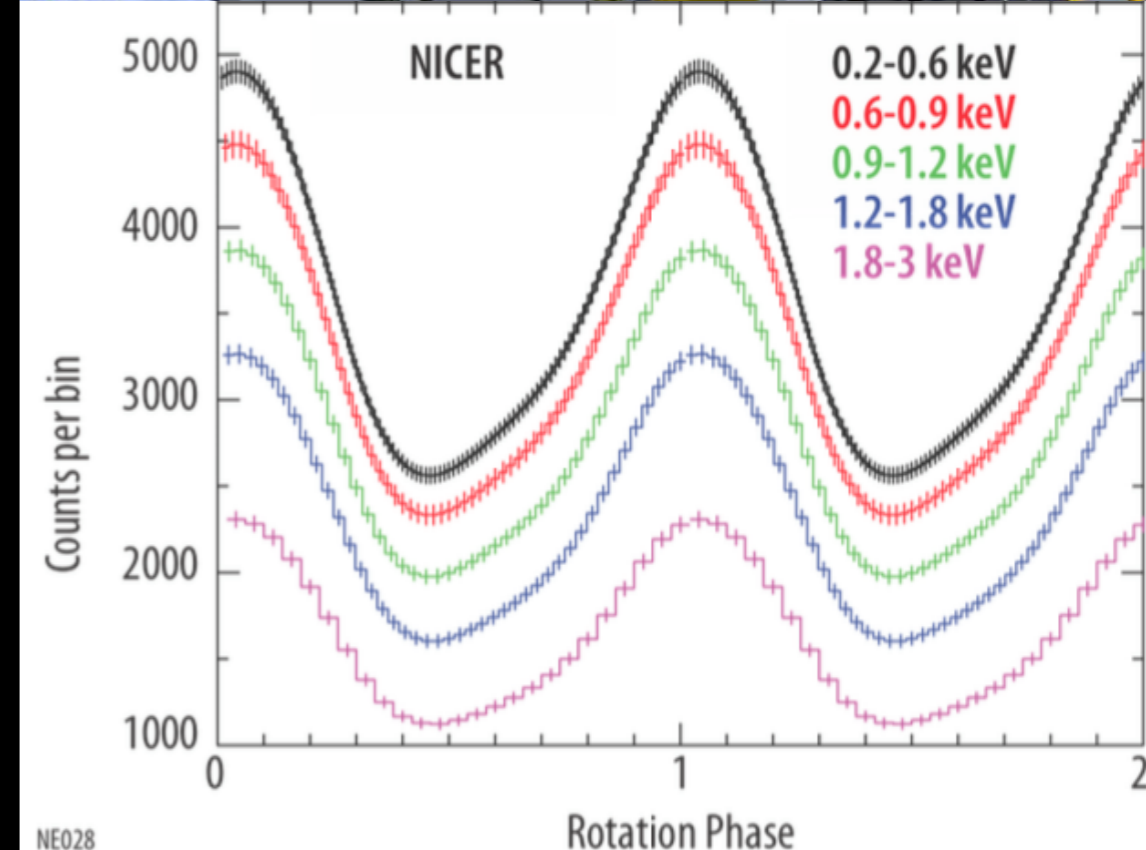
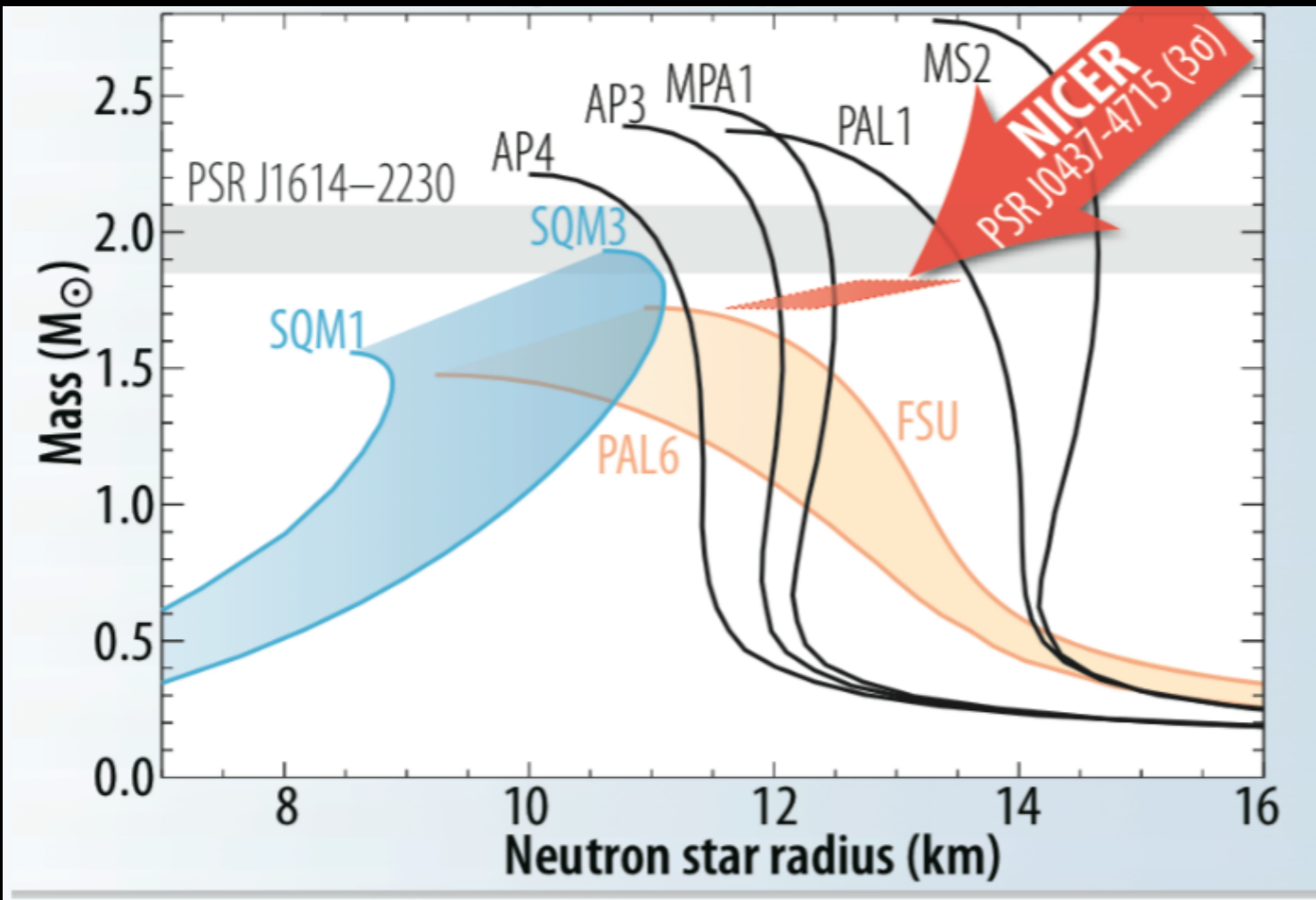
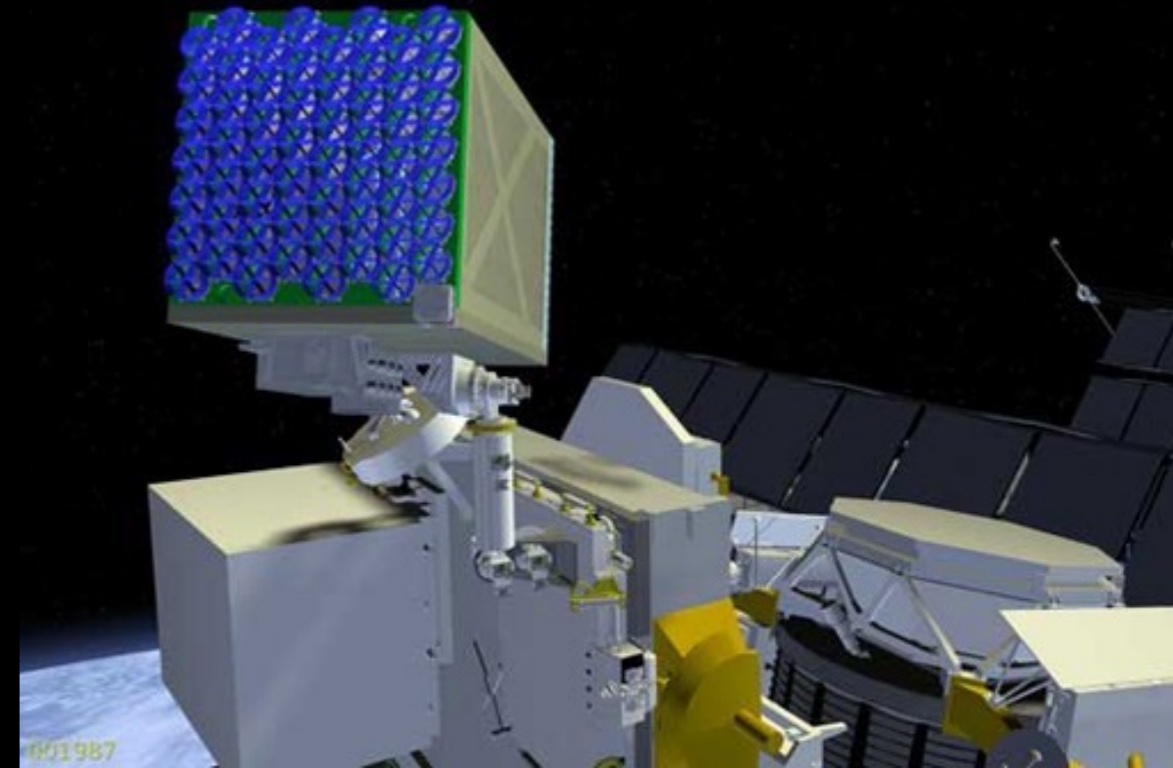
Thermal Lightcurve Model



The Neutron Star Interior Composition Explorer will measure M-R very precisely.

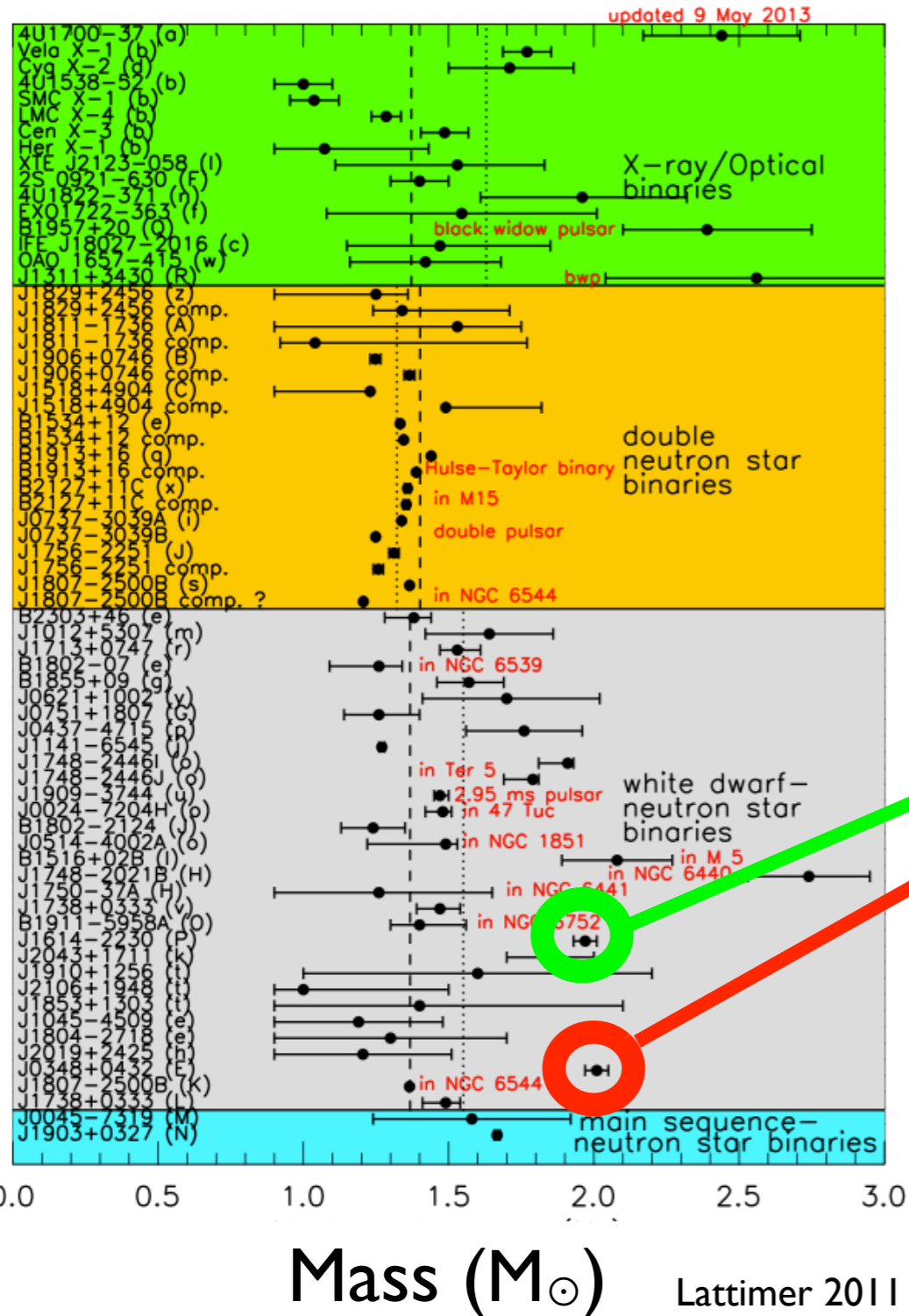
NICER

Launch: Feb. 2017



What about the largest
neutron star masses?

Only new M_{NS} measurements larger than previous ones improve constraints on the dense matter equation of state



NEW MASS

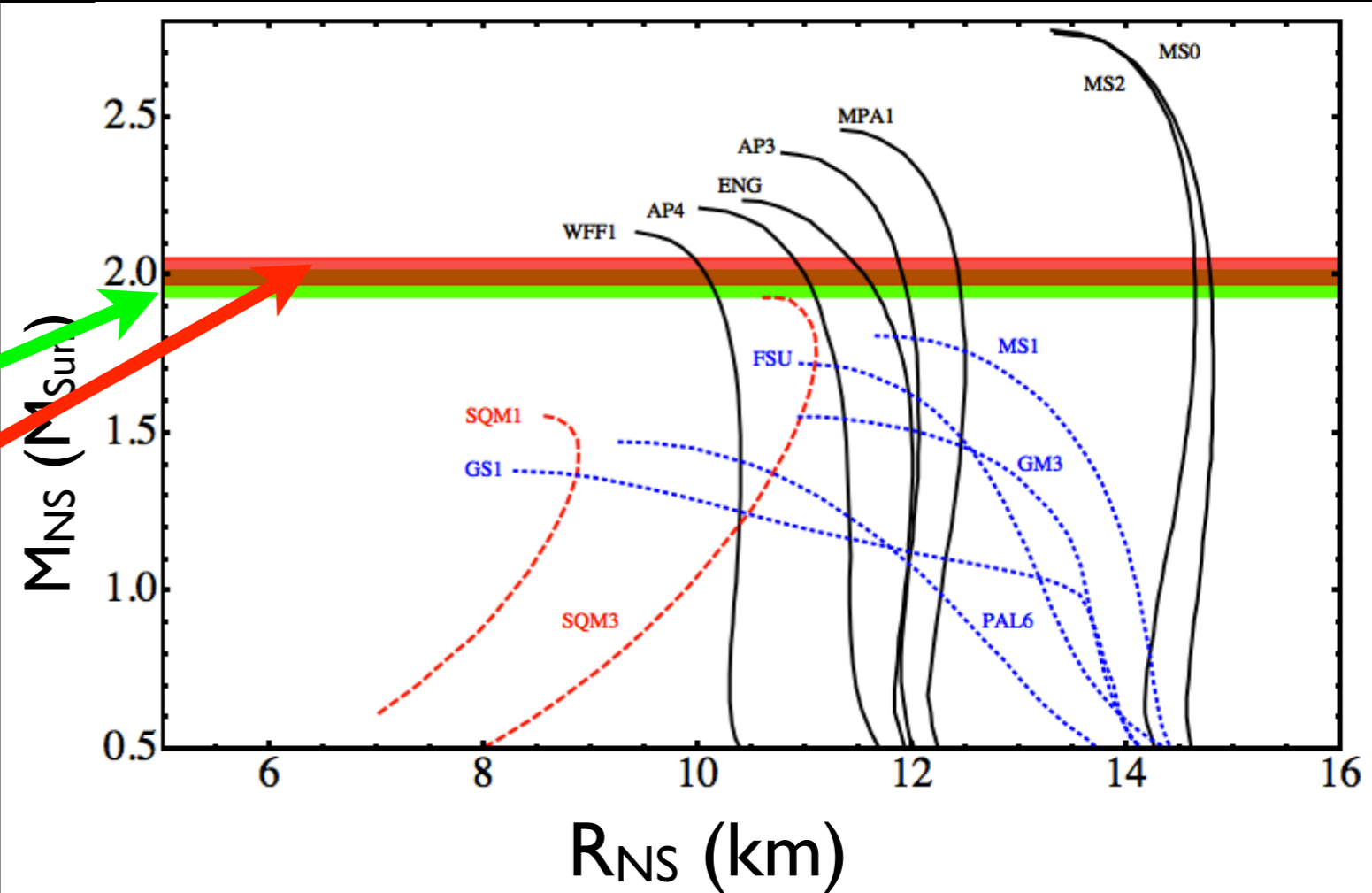
PSR J1614-2230

~~$M_{\text{PSR}} = 1.97 \pm 0.04 M_{\odot}$~~

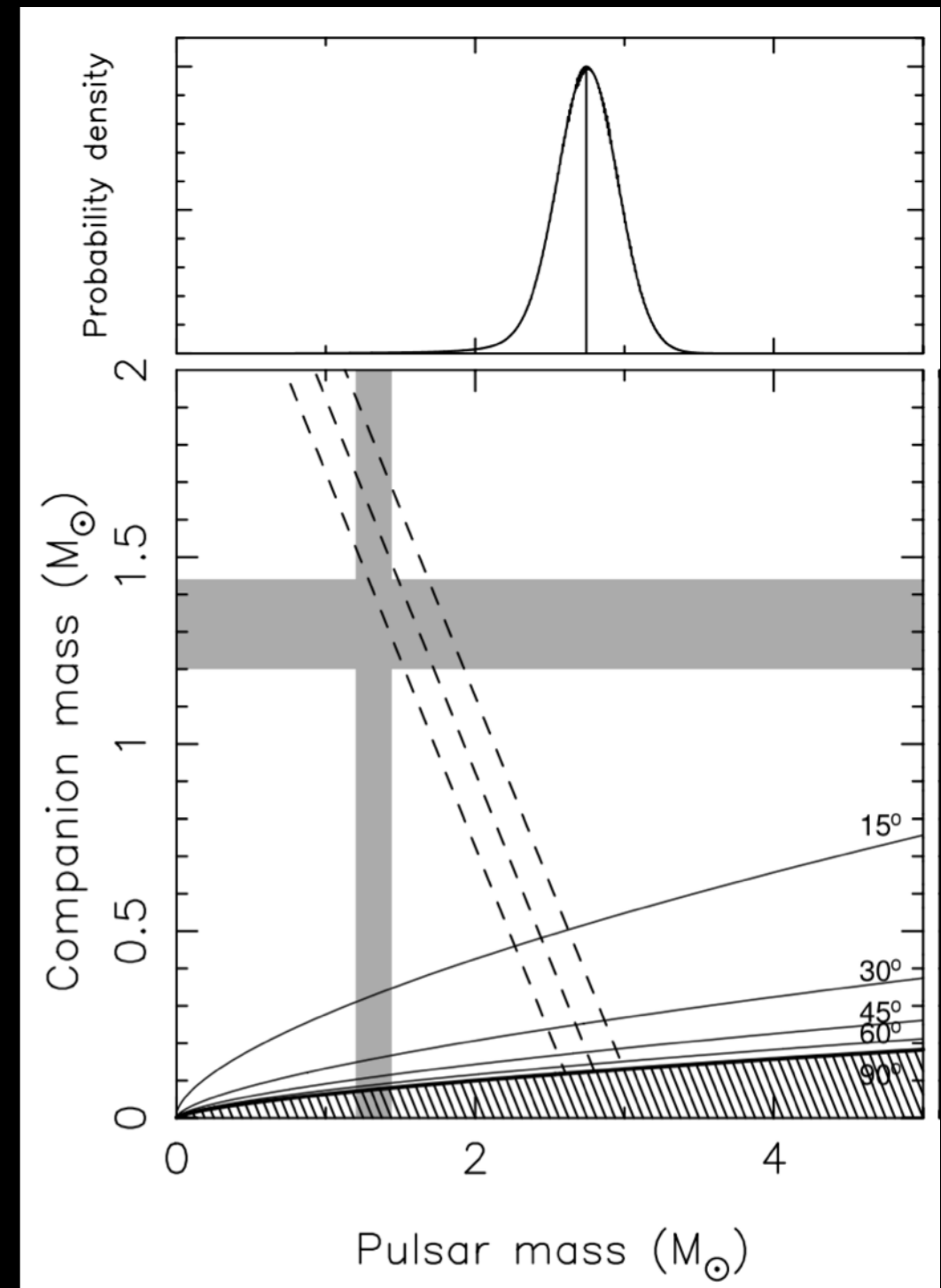
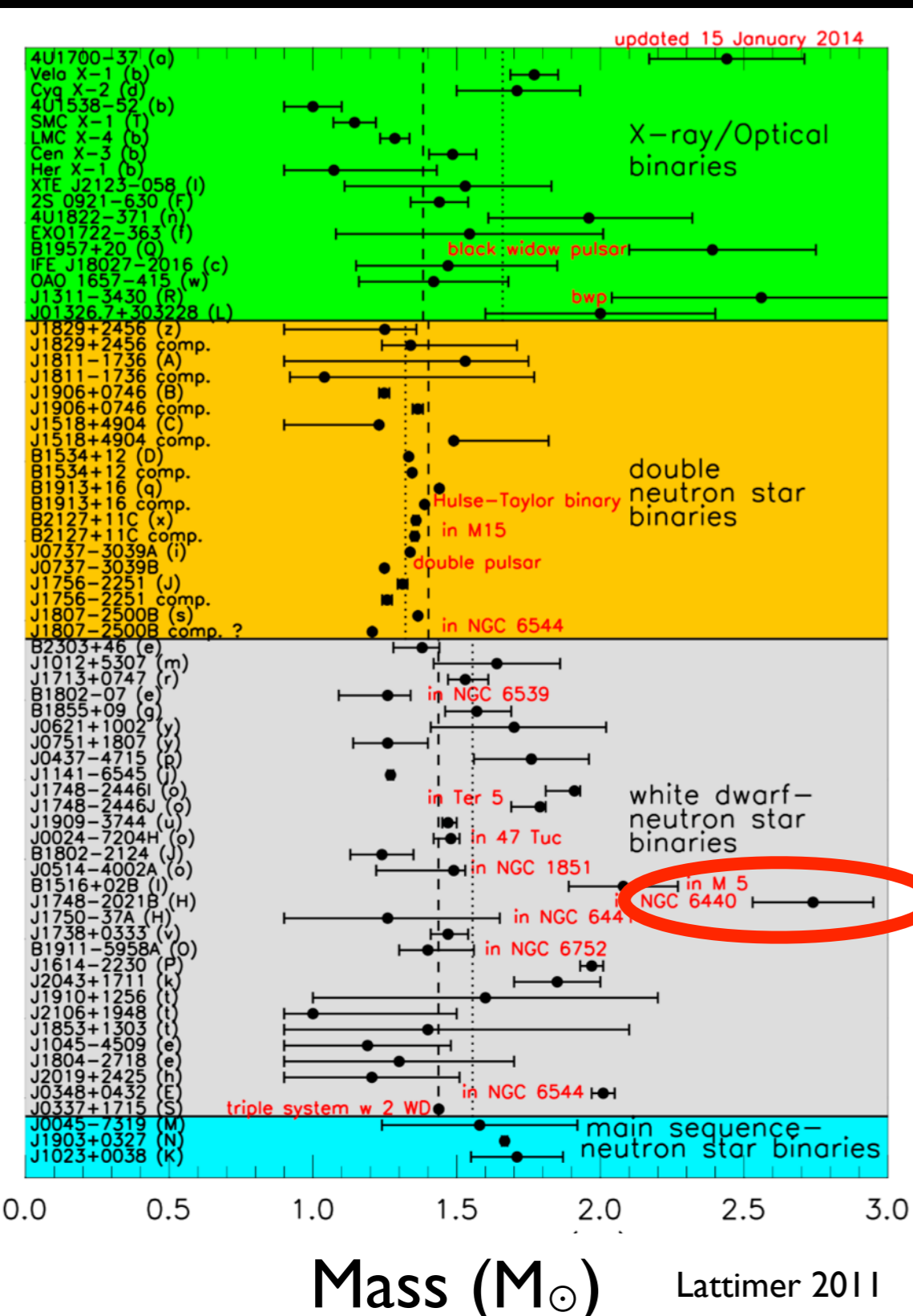
$M_{\text{PSR}} = 1.928 \pm 0.017 M_{\odot}$
(Fonseca et al. 2016)

PSR J0348+0432

$M_{\text{PSR}} = 2.01 \pm 0.04 M_{\odot}$
(Antoniadis et al. 2013)

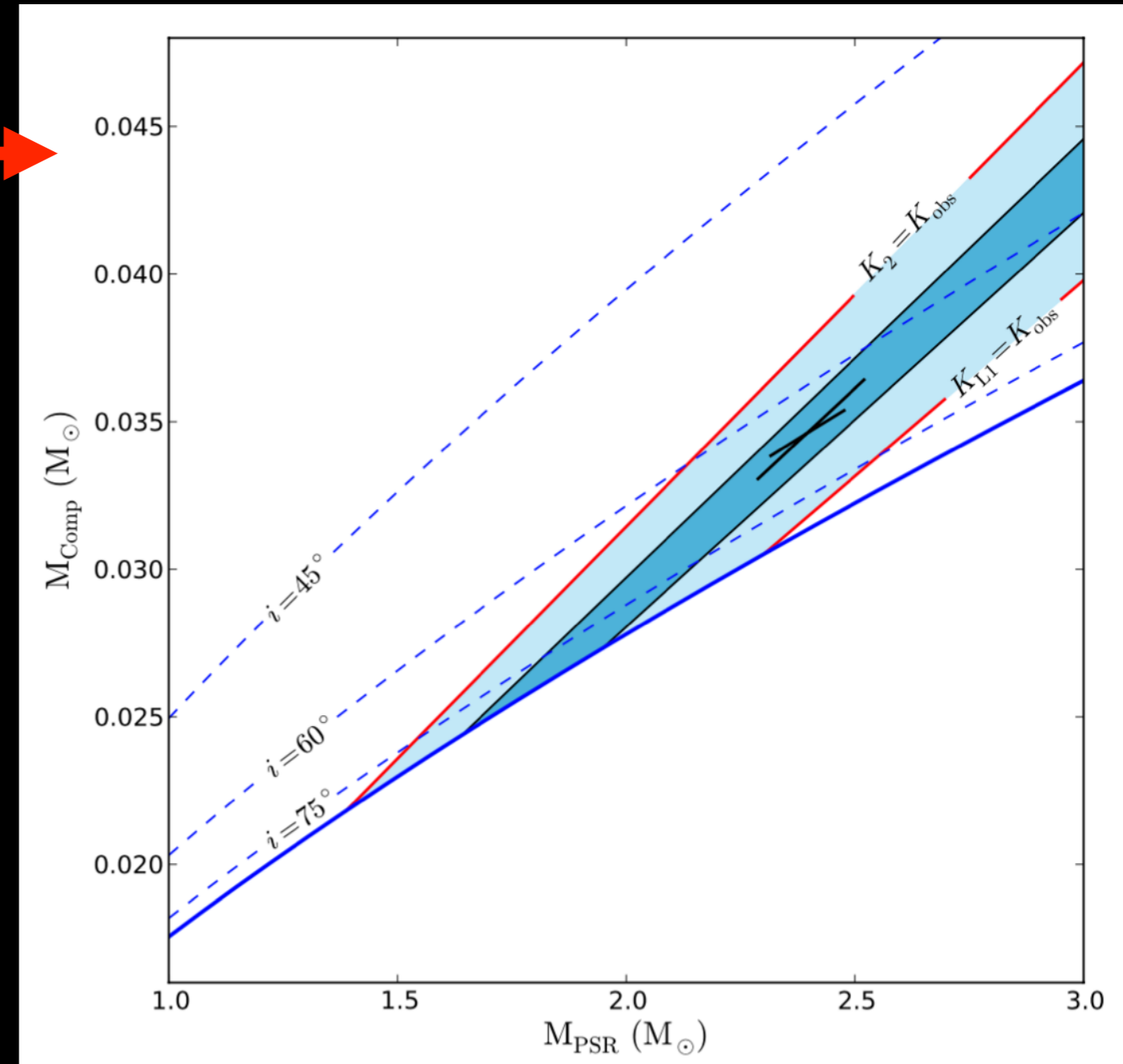
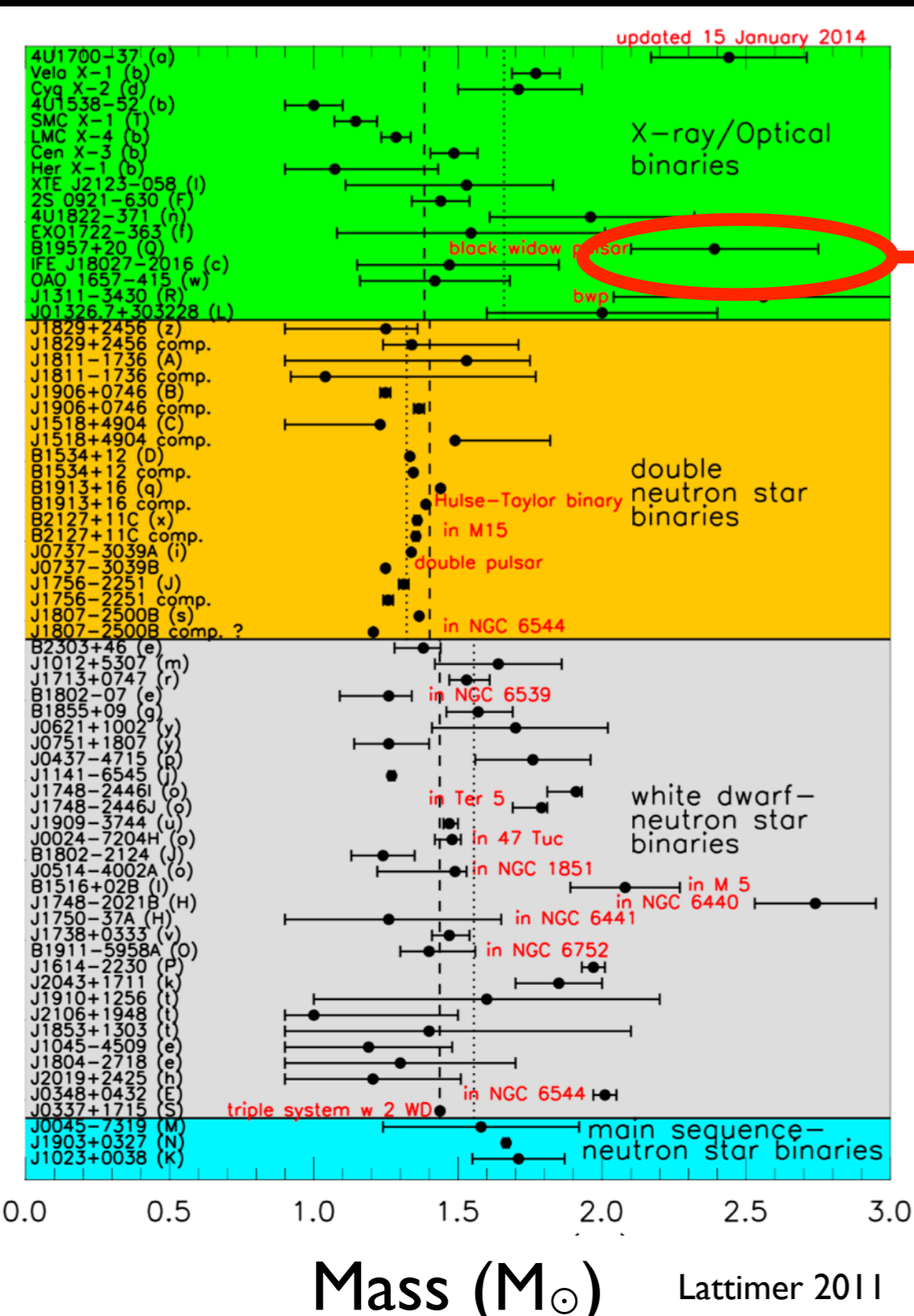


Other measurements with masses over $2 M_{\odot}$ suffer from systematics.



Freire et al. 2008

Other measurements with masses over $2 M_{\odot}$ suffer from systematics.



van Kerkwijk et al 2011

The Five hundred meters Aperture Spherical Telescope (FAST) will provide a leap in sensitivity for pulsar timing.



in the
Guizhou Province
贵州省

Summary

Quiescent LMXBs are stable objects from which the surface thermal emission allows us to measure the radius.

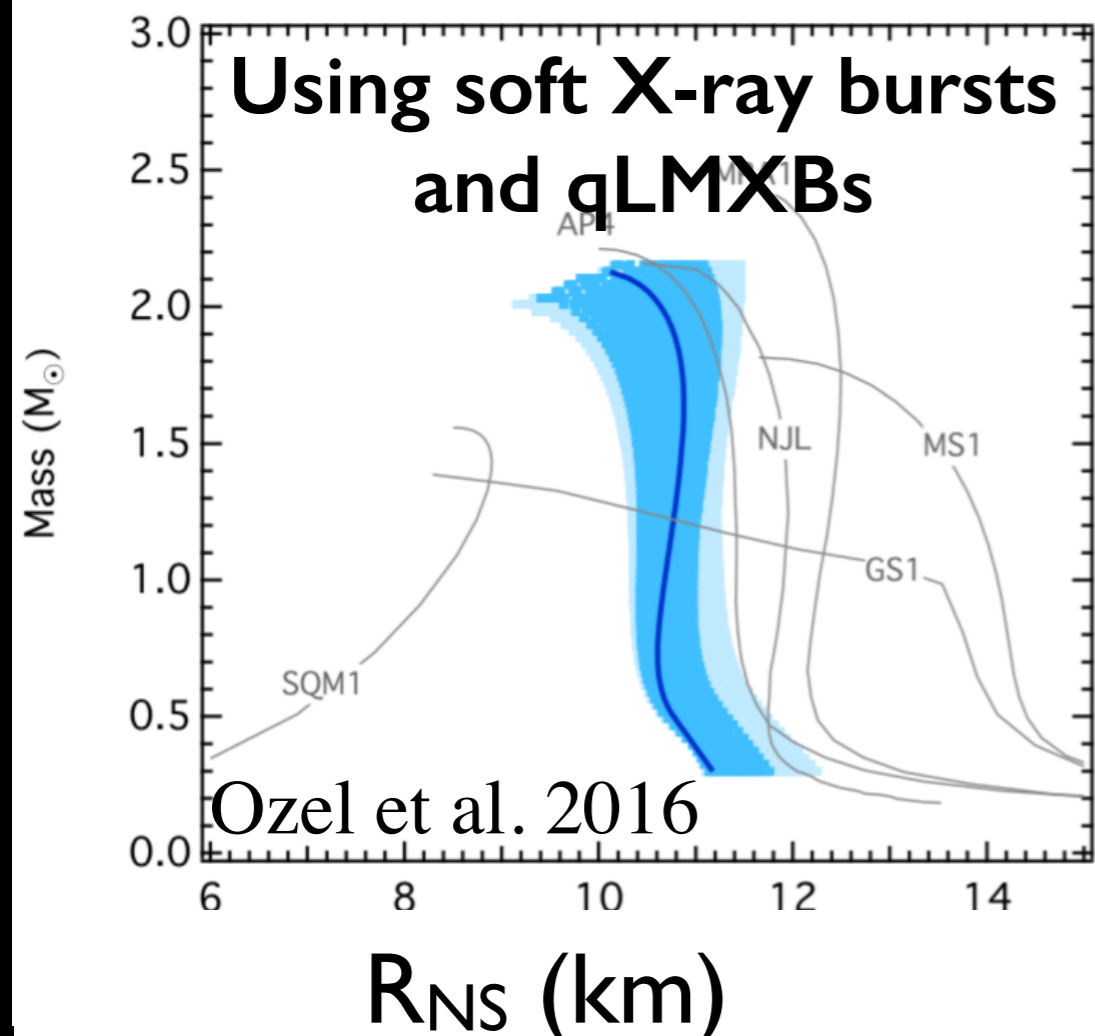
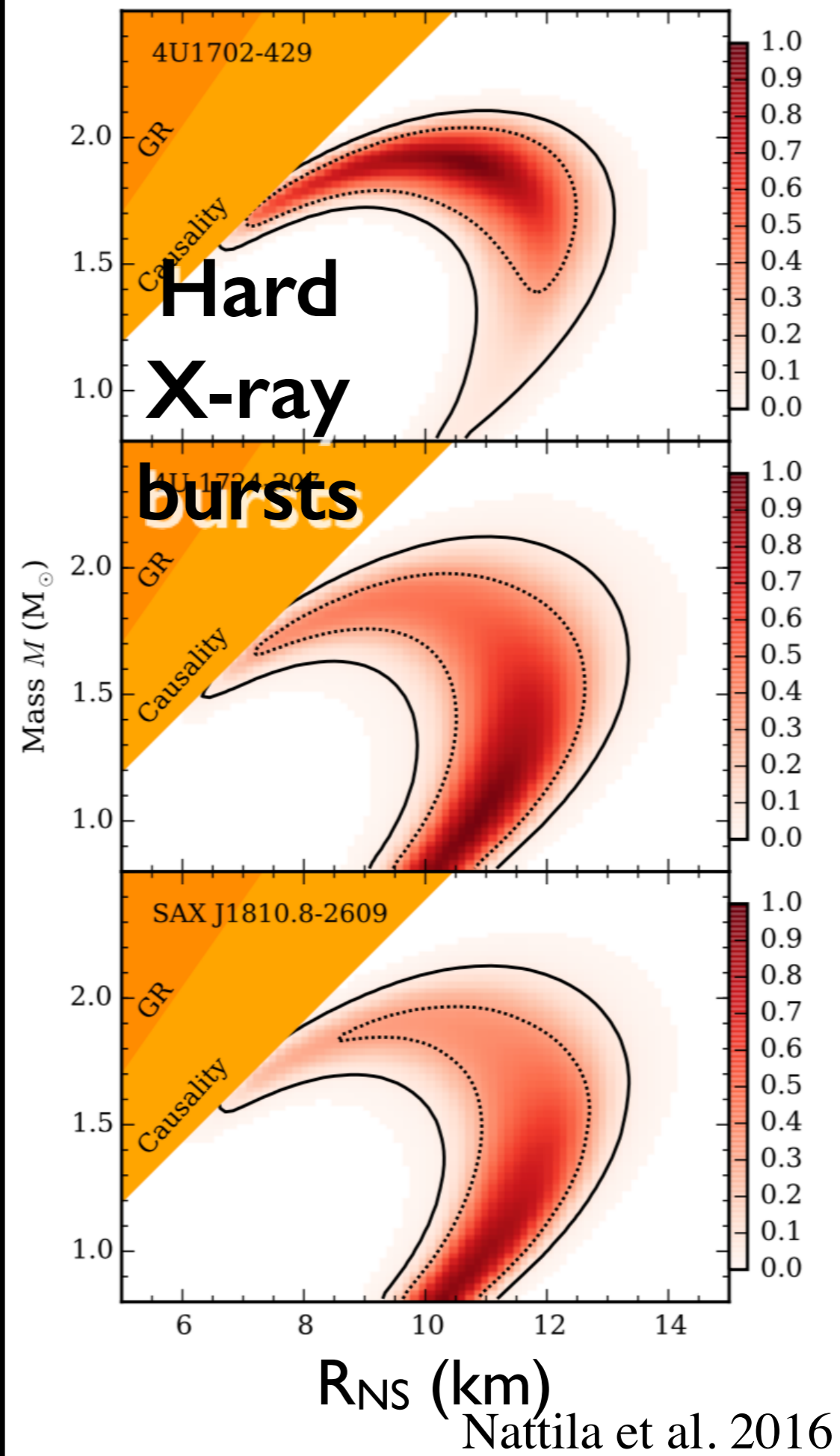
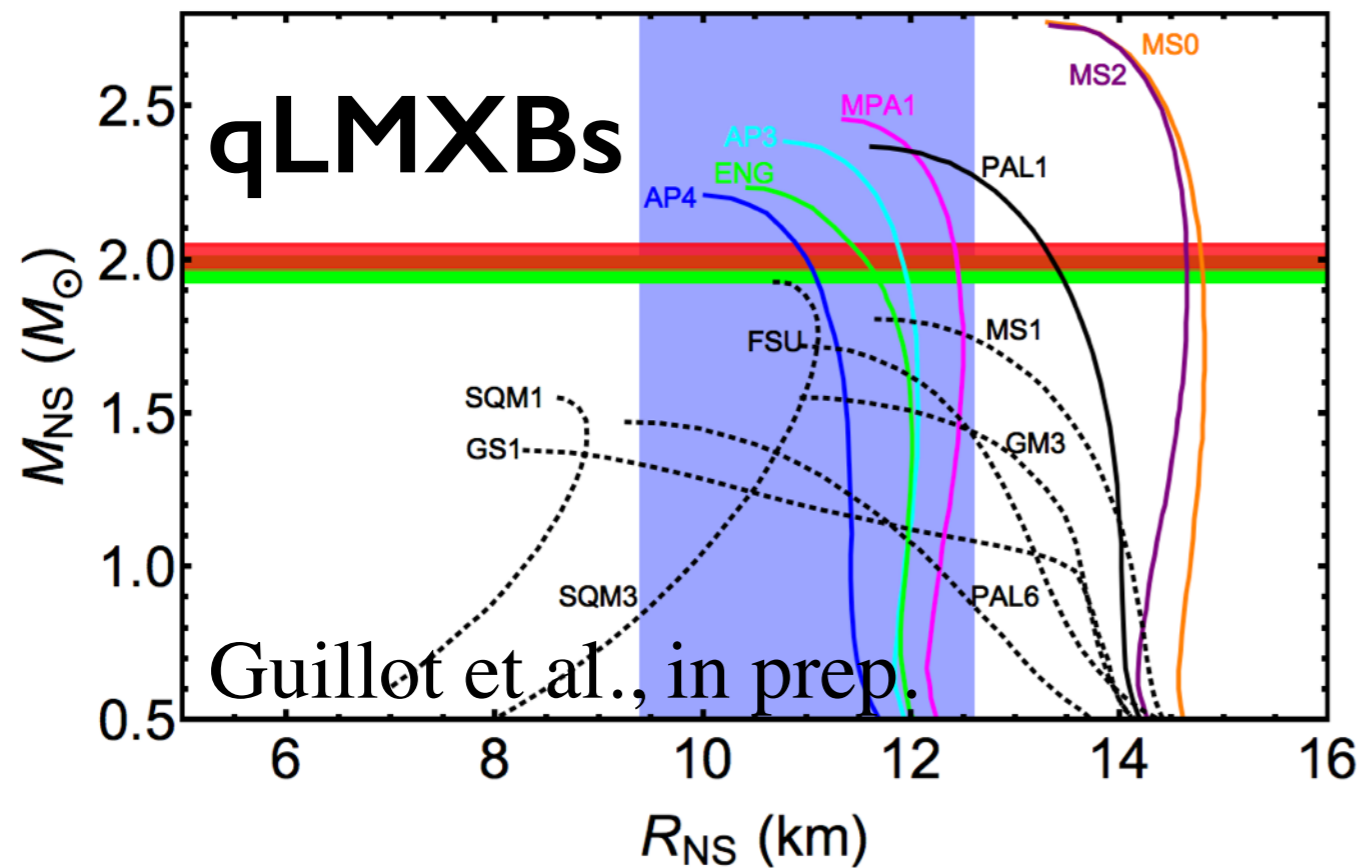
Because we actually measure R_∞ , constraints on the EoS from an individual qLMXB are limited.

But they can be combined, with some simple or more complicated parameterization of the EoS to extract constraints

There are systematics affecting the measurements, but more observations can help us understand them.

Recent progress led to higher radii which relaxes the tension with nuclear physics and other astrophysical measurements

$$R_{\text{NS}} = 10.8^{+1.8}_{-1.4} \text{ km}$$



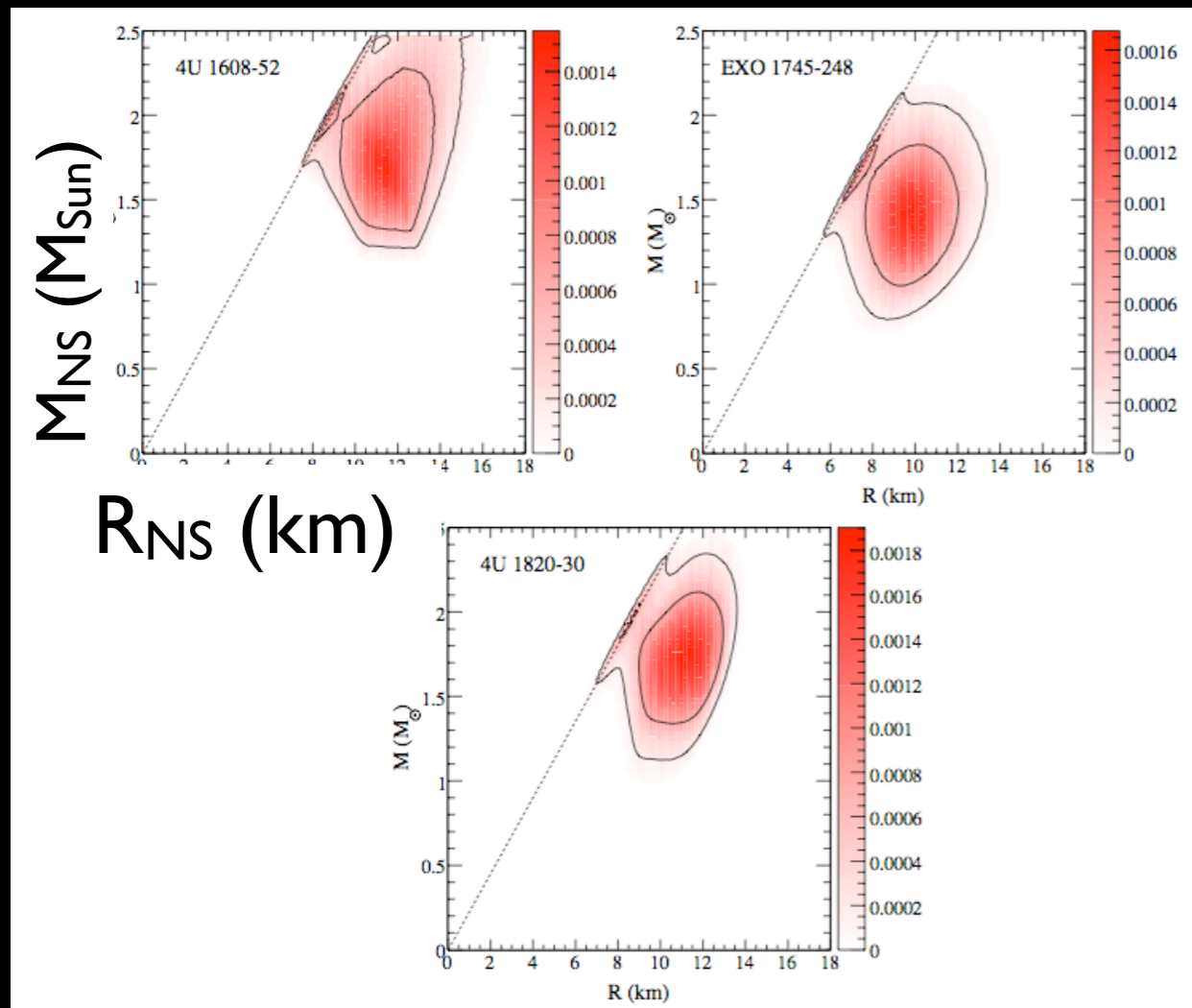
$M_{\text{NS}}-R_{\text{NS}}$ contours can be combined to parametrize the EoS.

Lattimer & Steiner 2014

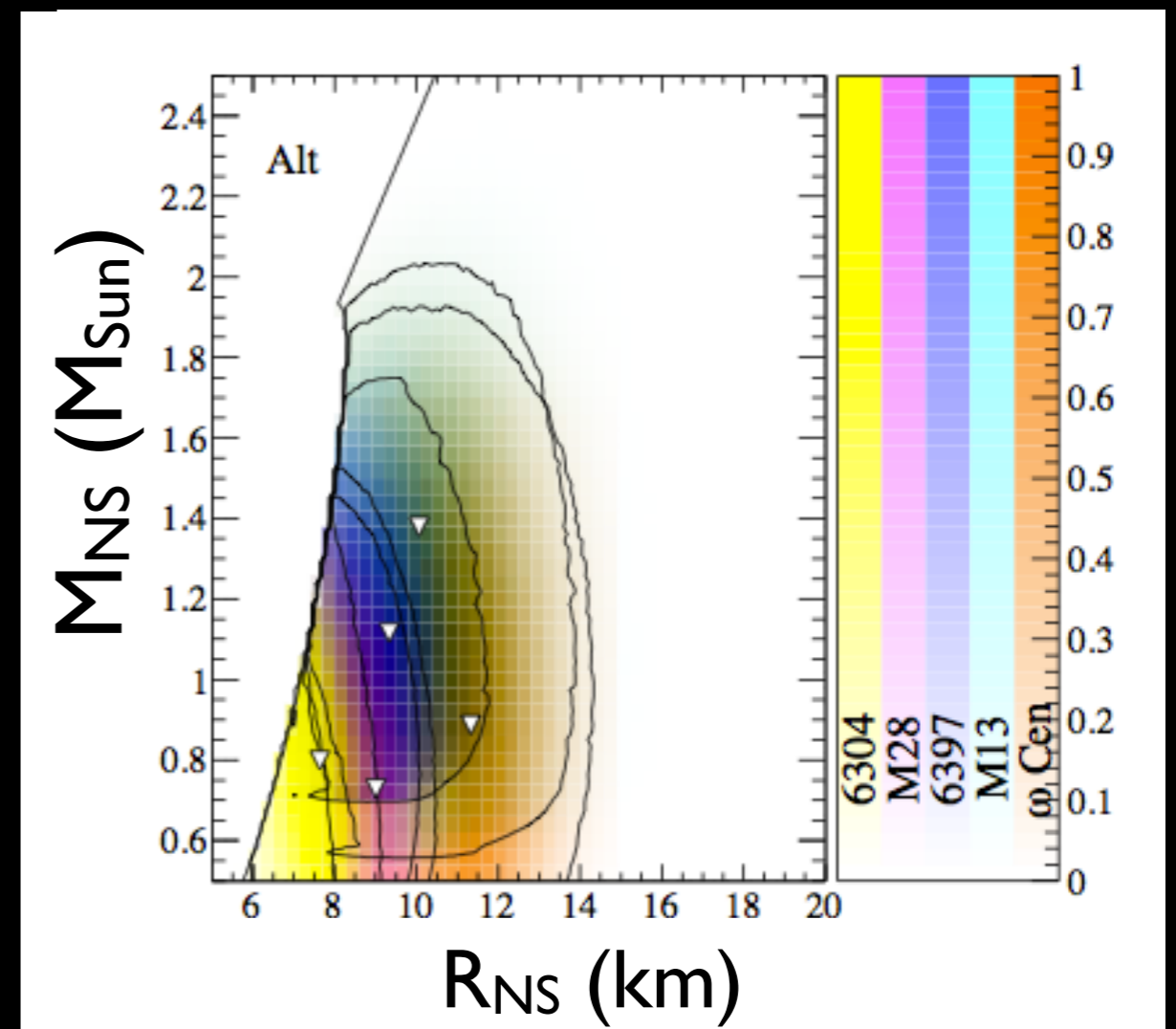
method demonstrated in Steiner et al 2010

Type I X-ray bursts

Quiescent LMXBs



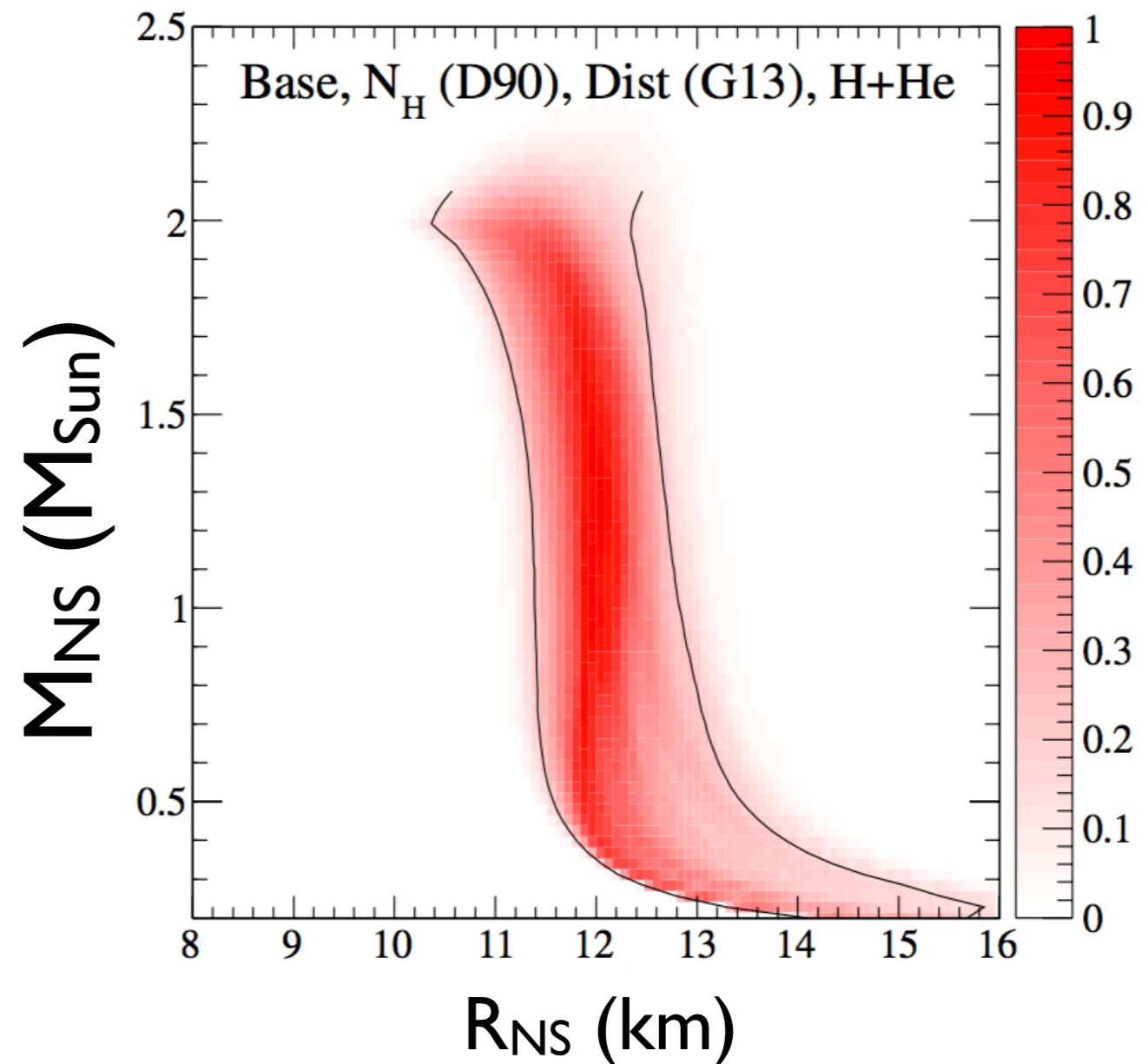
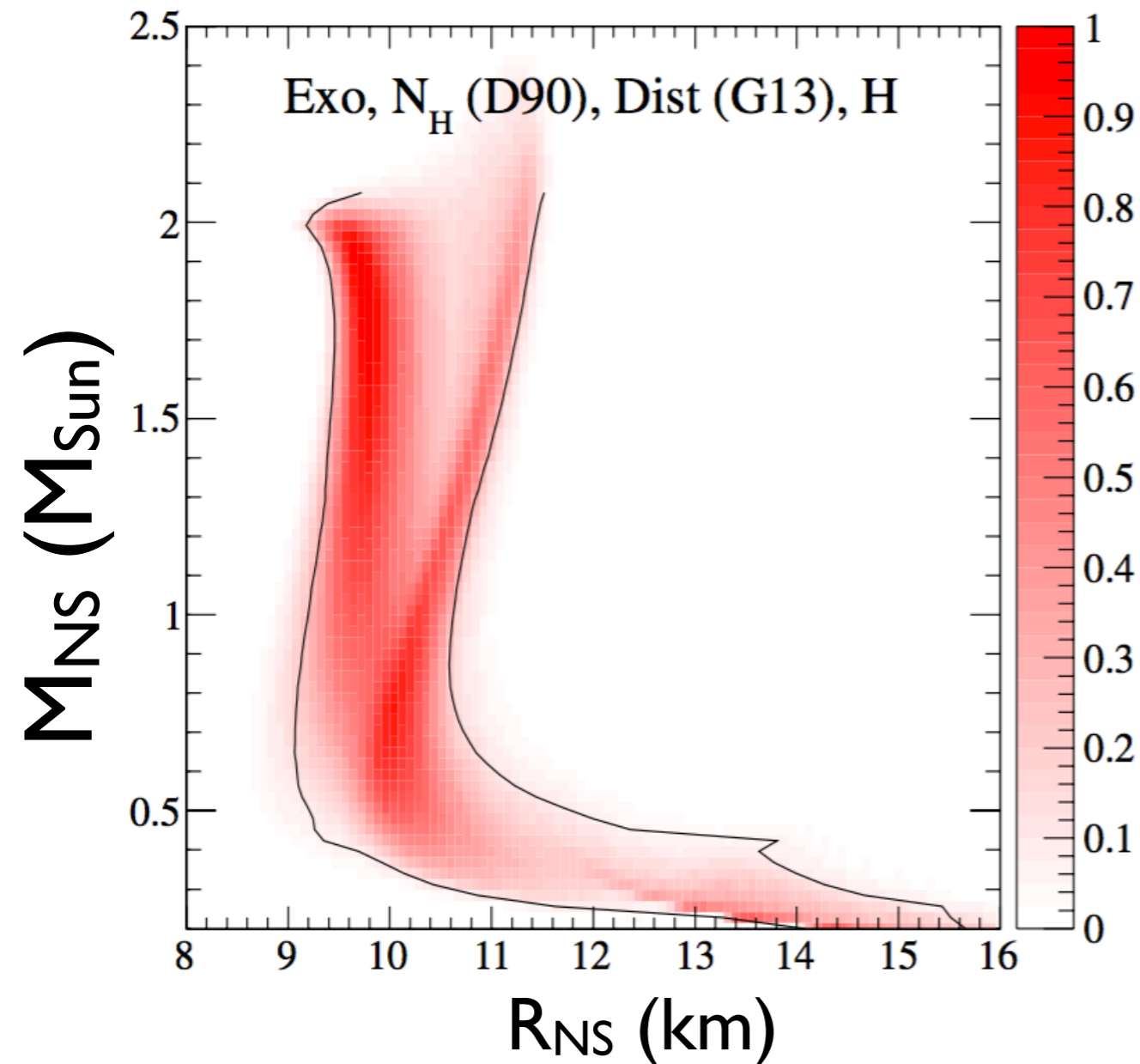
+



Rescaled M-R contour of qLMXBs from Guillot et al. 2013

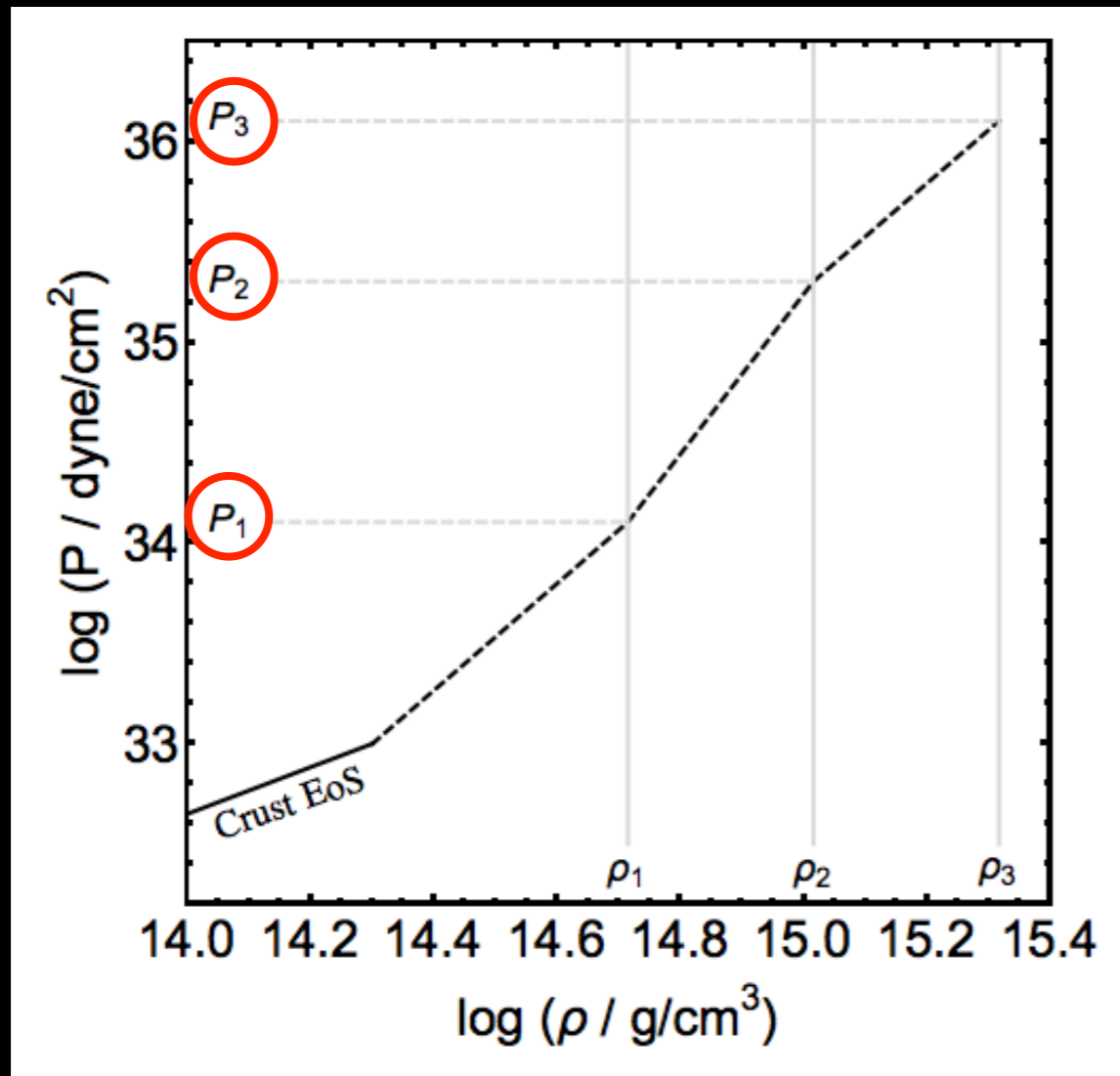
$M_{\text{NS}}-R_{\text{NS}}$ contours can be combined to parametrize the EoS.

Lattimer & Steiner 2014

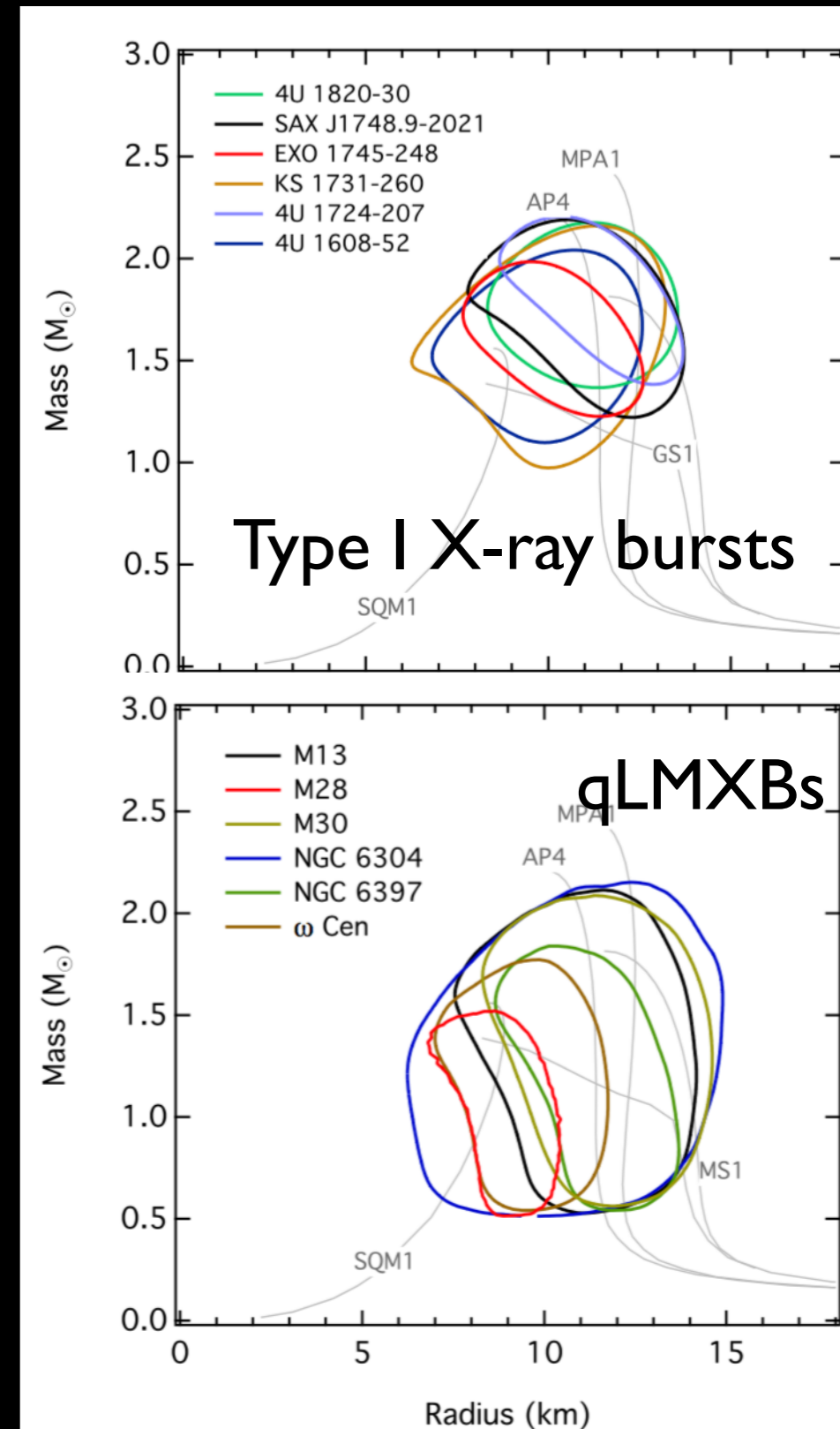


We combined $M_{\text{NS}}-R_{\text{NS}}$ measurements from qLMXBs and type I X-ray bursts to place constraints on the pressure at three fiducial densities.

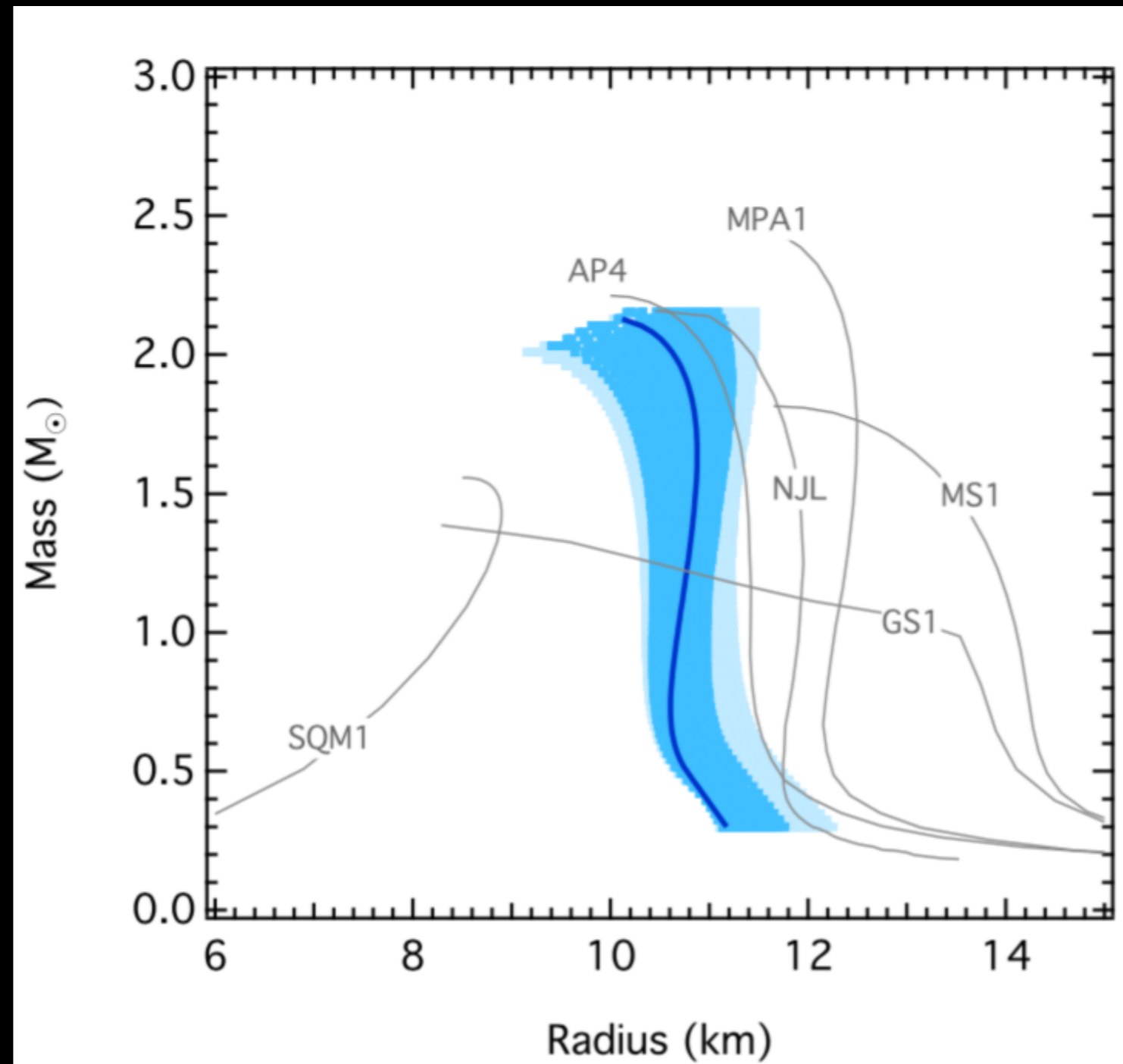
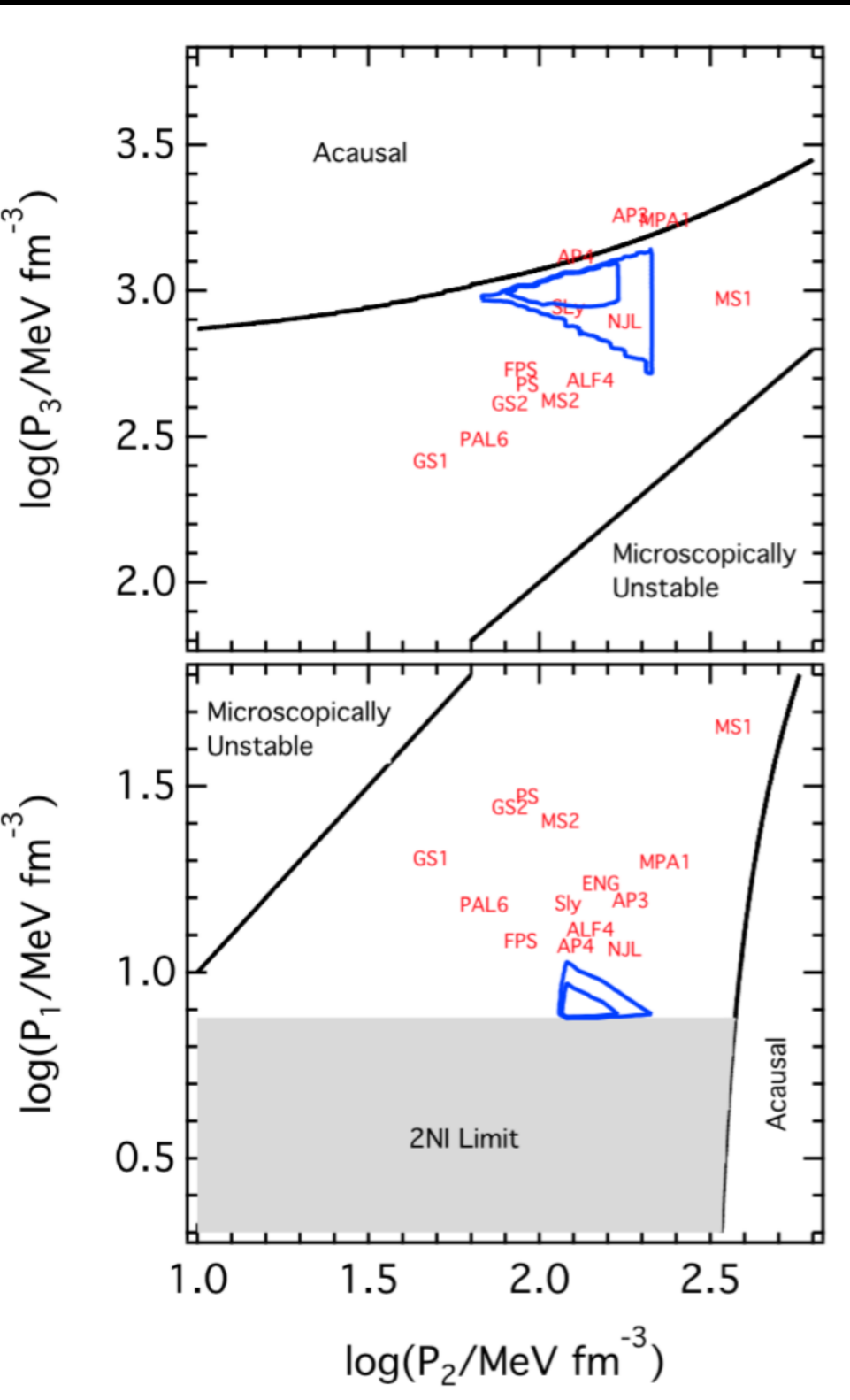
Ozel et al. 2016



P_1 , P_2 and P_3 measured at $1.85\rho_0$, $3.7\rho_0$ and $7.4\rho_0$



We combined $M_{\text{NS}}-R_{\text{NS}}$ measurements from qLMXBs and type I X-ray bursts to place constraints on the pressure at three fiducial densities, leading to a unique equation of state.

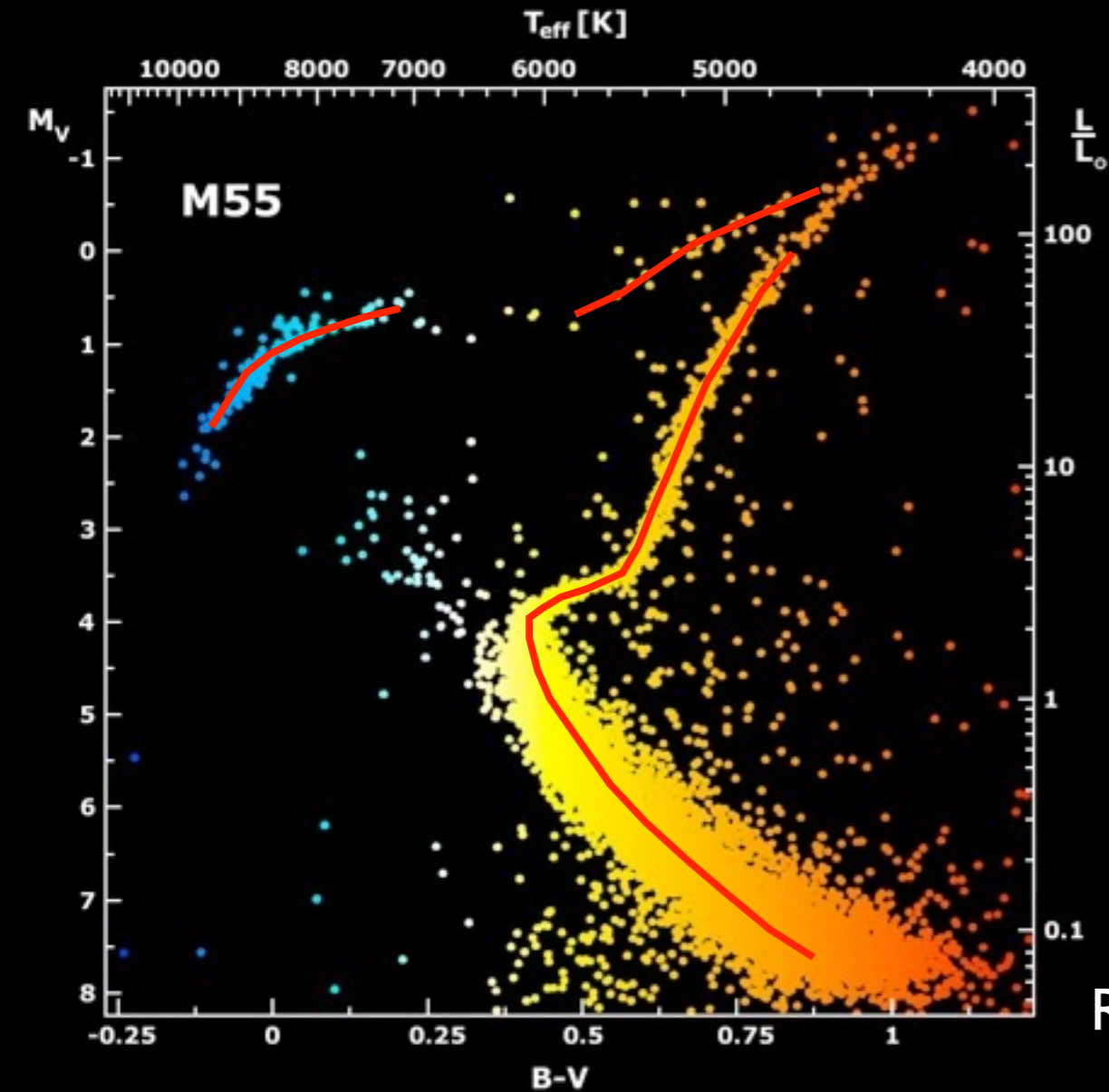


Aside

Distance to globular clusters are not trivial to obtain and can be severely affected by systematics.

Photometric distances

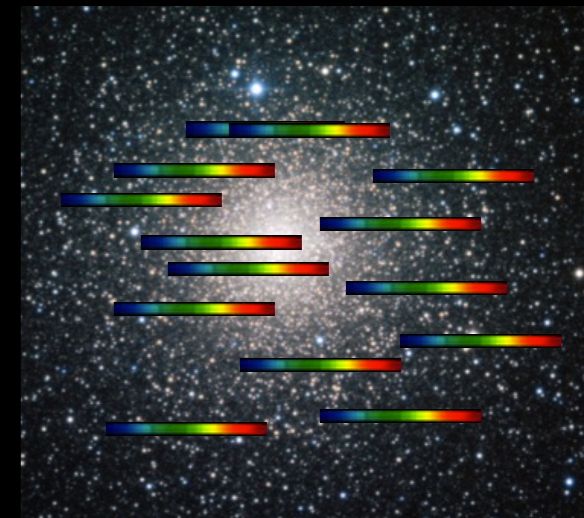
Dynamical distances



Relating apparent magnitude to absolute magnitude

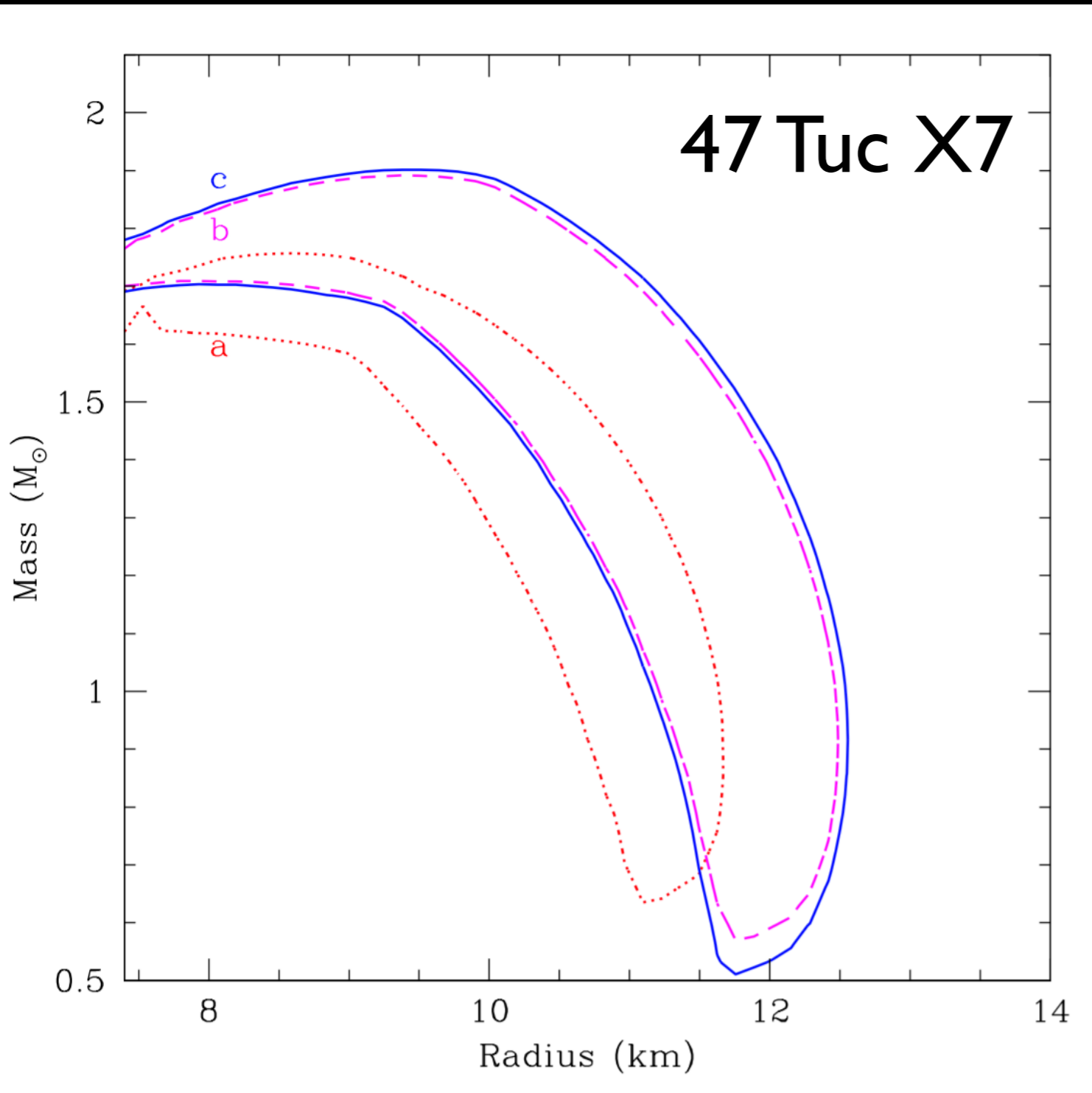


projected velocity dispersion in arcsec/year



radial velocity dispersion in km/sec

For some qLMXBs, instrumental effects may also bias the radius measurements.



Pile-up of photons on Chandra's CCD shifts the peak of the thermal spectrum, and affects the measured R_{∞} by about 10%

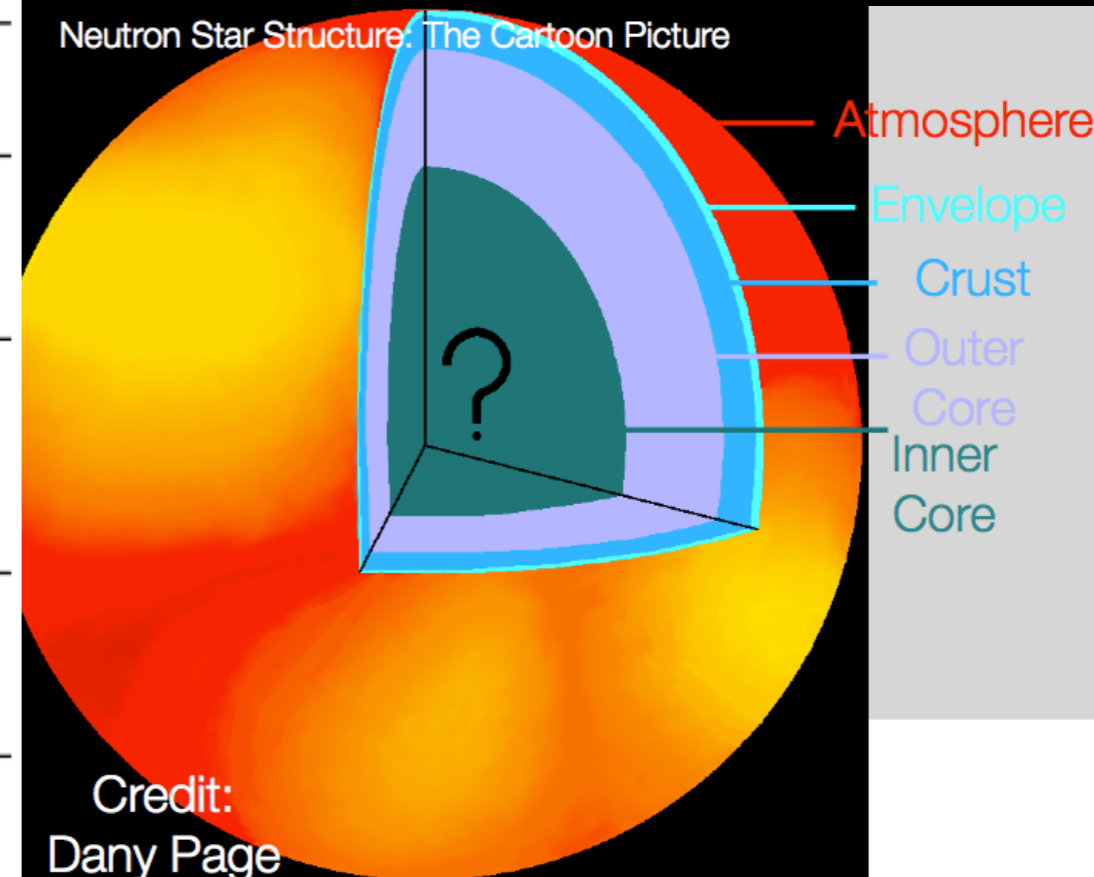
Bogdanov et al. 2016

**Non-Equilibrium Processes in the Outer Crust
Beginning with ^{56}Fe (Haensel & Zdunik 1990, 2003, 2008)**

ρ^a (g cm^{-3})	Process	Type of reaction	X_n^b	Q^c (keV)
1.49×10^9	$^{56}\text{Fe} \rightarrow ^{56}\text{Cr} - 2e^- + 2\nu_e$	e^- capture	0.00	40.7
1.11×10^{10}	$^{56}\text{Cr} \rightarrow ^{56}\text{Ti} - 2e^- + 2\nu_e$	e^- capture	0.00	35.8
7.85×10^{10}	$^{56}\text{Ti} \rightarrow ^{56}\text{Ca} - 2e^- + 2\nu_e$	e^- capture	0.00	47.3
2.50×10^{11}	$^{56}\text{Ca} \rightarrow ^{56}\text{Ar} - 2e^- + 2\nu_e$	e^- capture	0.00	46.1
6.11×10^{11}	$^{56}\text{Ar} \rightarrow ^{52}\text{S} + 4n - 2e^- + 2\nu_e$	n emission	0.00	59.8
9.075×10^{11}	$^{52}\text{S} \rightarrow ^{46}\text{Si} + 6n - 2e^- + 2\nu_e$	n emission	0.07	128.0
1.131×10^{12}	$^{46}\text{Si} \rightarrow ^{40}\text{Mg} + 6n - 2e^- + 2\nu_e$	n emission	0.18	143.5
1.455×10^{12}	$^{40}\text{Mg} \rightarrow ^{34}\text{Ne} + 6n - 2e^- + 2\nu_e$ $^{34}\text{Ne} + ^{34}\text{Ne} \rightarrow ^{68}\text{Ca}$	n emission pynonuclear	0.39	507.9
1.766×10^{12}	$^{68}\text{Ca} \rightarrow ^{62}\text{Ar} + 6n - 2e^- + 2\nu_e$	n emission	0.45	65.8
2.134×10^{12}	$^{62}\text{Ar} \rightarrow ^{56}\text{S} + 6n - 2e^- + 2\nu_e$	n emission	0.45	71.6
2.634×10^{12}	$^{56}\text{S} \rightarrow ^{50}\text{Si} + 6n - 2e^- + 2\nu_e$	n emission	0.50	77.9
3.338×10^{12}	$^{50}\text{Si} \rightarrow ^{44}\text{Mg} + 6n - 2e^- + 2\nu_e$	n emission	0.55	84.6
4.379×10^{12}	$^{44}\text{Mg} \rightarrow ^{36}\text{Ne} + 8n - 2e^- + 2\nu_e$ $^{36}\text{Ne} + ^{36}\text{Ne} \rightarrow ^{72}\text{Ca}$ $^{72}\text{Ca} \rightarrow ^{66}\text{Ar} + 6n - 2e^- + 2\nu_e$	n emission pynonuclear n emission	0.61	308.8
5.839×10^{12}	$^{66}\text{Ar} \rightarrow ^{60}\text{S} + 6n - 2e^- + 2\nu_e$	n emission	0.70	29.5
7.041×10^{12}	$^{60}\text{S} \rightarrow ^{54}\text{Si} + 6n - 2e^- + 2\nu_e$	n emission	0.73	31.0
8.980×10^{12}	$^{54}\text{Si} \rightarrow ^{48}\text{Mg} + 6n - 2e^- + 2\nu_e$ $^{48}\text{Mg} + ^{48}\text{Mg} \rightarrow ^{96}\text{Cr}$ $^{96}\text{Cr} \rightarrow ^{94}\text{Cr} + 2n$	n emission pynonuclear n emission	0.80	135.1
1.057×10^{13}	$^{94}\text{Cr} \rightarrow ^{88}\text{Ti} + 6n - 2e^- + 2\nu_e$	n emission	0.81	11.5
1.254×10^{13}	$^{88}\text{Ti} \rightarrow ^{82}\text{Ca} + 6n - 2e^- + 2\nu_e$	n emission	0.82	11.3
1.506×10^{13}	$^{82}\text{Ca} \rightarrow ^{76}\text{Ar} + 6n - 2e^- + 2\nu_e$	n emission	0.84	10.9
1.838×10^{13}	$^{76}\text{Ar} \rightarrow ^{70}\text{S} + 6n - 2e^- + 2\nu_e$	n emission	0.85	10.0
2.287×10^{13}	$^{70}\text{S} \rightarrow ^{64}\text{Si} + 6n - 2e^- + 2\nu_e$ $^{64}\text{Si} + ^{64}\text{Si} \rightarrow ^{128}\text{Ni}$ $^{128}\text{Ni} \rightarrow ^{126}\text{Ni} + 2n$	n emission pynonuclear n emission	0.87	67.3
2.784×10^{13}	$^{126}\text{Ni} \rightarrow ^{124}\text{Fe} + 2n - 2e^- + 2\nu_e$	n emission	0.88	2.5
3.493×10^{13}	$^{124}\text{Fe} \rightarrow ^{122}\text{Cr} + 2n - 2e^- + 2\nu_e$	n emission	0.89	2.4

The thermal emission from qLMXB is powered by Deep Crustal Heating.

Brown et al. 1998



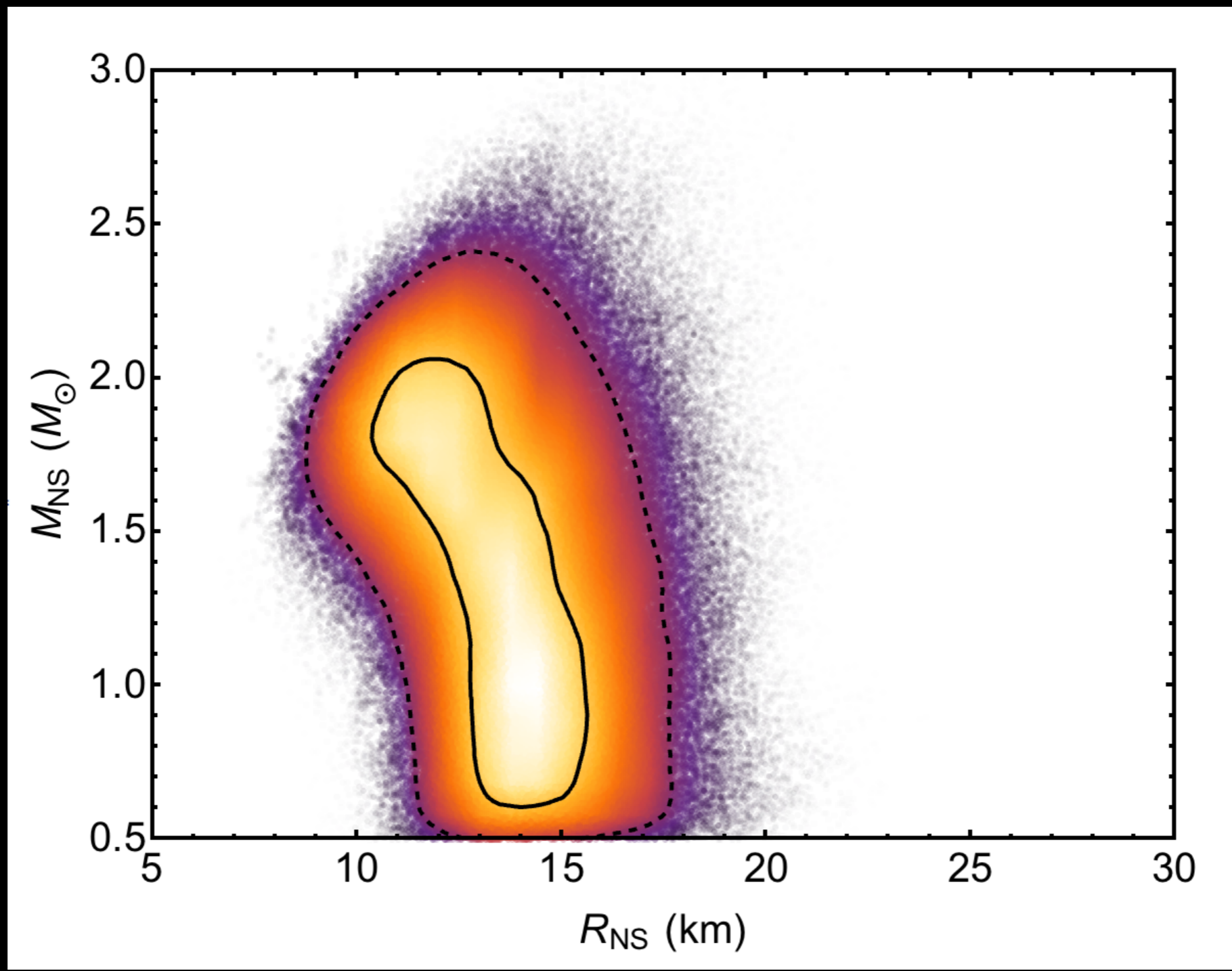
Not all globular cluster qLMXBs are useful. This is because of large distances and/or absorption.

Globular Cluster	Distance (kpc)	Absorption (N_H in 10^{22} cm^{-2})	qLMXB	"Useful"	Difficulties	Need Chandra
ω Cen	4.59	0.09	1	Green		NO
M13	7.1	0.01	1	Green		NO
M28	5.5	0.26	1	Green	Moderate pile-up	YES
NGC 6304	6.2	0.27	1	Green		YES
NGC 6397	2.3	0.14	1	Green		YES
47 Tuc	4.5	0.03	2 (+3?)	Green	Important pile-up	YES
M30	9	0.01	1	Green	Large distance	YES
NGC 6553	6	0.35	1	Green	<i>NEEDS TO BE CONFIRMED</i>	YES
M80	10.3	0.09	2	Orange	Large distance	YES
NGC 362	8.6	0.03	1	Orange	Large distance	YES
NGC 2808	9.6	0.82	1	Red	Large distance and N_H	YES
NGC 3201	5	1.17	1	Red	Very Large N_H	NO
NGC 6440	8.5	0.7	8	Red	Large distance and N_H	YES
Terzan 5	8.7	1.2	4	Red	Large distance and N_H	YES

Unconstrained R_∞ measurements

NGC 6397

with Helium and Pile-up



Straight line EoS: Radius at 1.4 Msun

