



An Improved thermometer for intermediate-mass fragments

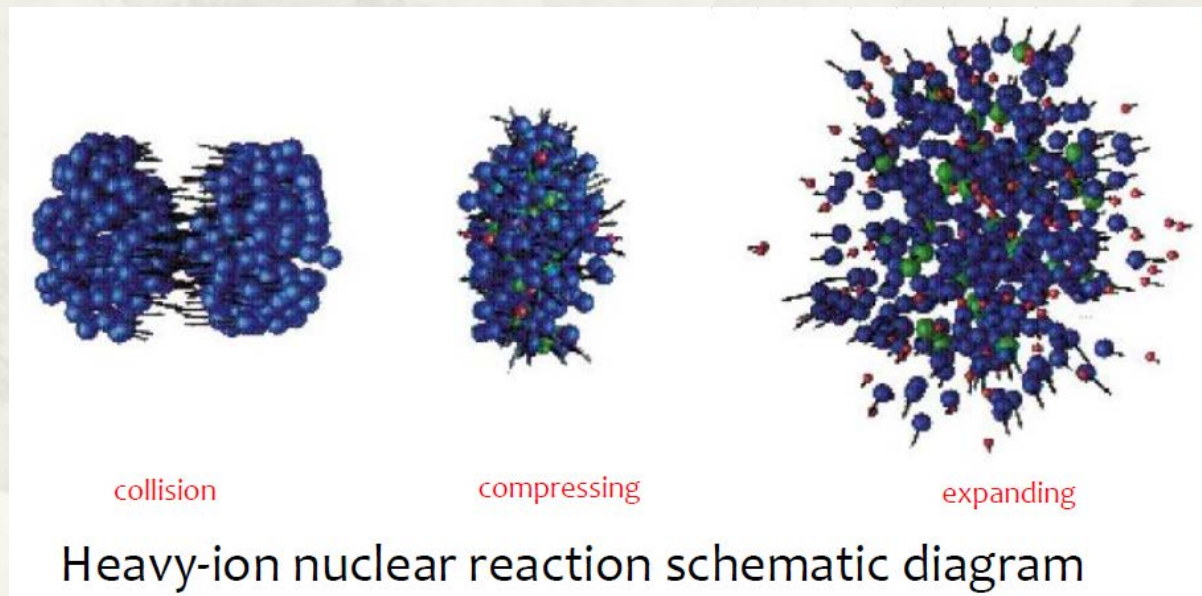
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1. Background

- * The temperature is one of the most important questions in the heavy-ion collision physics since it changes along the reaction process, which first increases in a very short time due to the compression of the system and then decrease with the expansion of the system in a long time.



1. Background

- * For the many probes used to study the nuclear symmetry energy, such as the isoscaling method, the isobaric ratio method, and the isobaric yield ratio difference (IBD) method, T is a part of the probe and cannot be separated easily.

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1. Background

- A thermometer based on the isobaric yield ratio (IYR) has been proposed.

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Temperature determined by isobaric yield ratios in heavy-ion collisions

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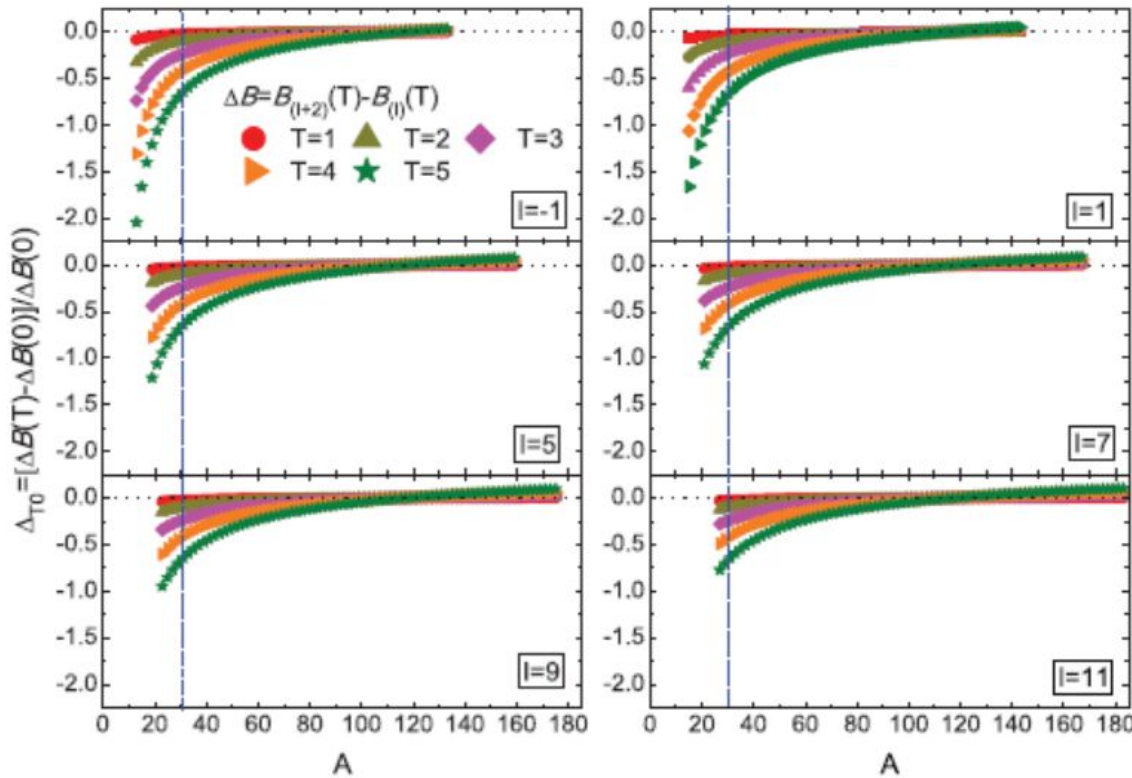
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- The thermometer based on IYR extracts T and the difference of chemical potential $\Delta\mu$ ($\Delta\mu = \mu_n - \mu_p$) by fitting the isobaric yield ratio of two isobars.

$$\ln R(I + 2, I, A) - \Delta S = (\Delta W + \Delta\mu)/T$$

1. Background



$$\Delta B(T) = B_{(I+2)}(T) - B_{(I)}(T)$$

$$\Delta_{T0} \equiv [\Delta B(T) - \Delta B(0)] / \Delta B(0)$$

- * Δ_{T0} decrease as the mass becomes larger and similarly as T decrease.
- * At $T = 1$ MeV, Δ_{T0} of the $I = -1 \sim 11$ isobars are very close to zero.
- * At $T \geq 3$ MeV, the $A < 50$ isobars show relatively large Δ_{T0} and the value of Δ_{T0} is less than -0.1.

1. Background

- In a word, it has proved that the residue free energy between two isobars can be replaced by that of binding energy in the IYR method. The fitting formula of extracting T can be written as,

$$\ln R(I + 2, I, A) - \Delta S = (\Delta B + \Delta \mu) / T$$

2. Method

The new thermometer is developed by using the canonical ensemble theory. With the grand-canonical limitation, the cross section of a fragment $\sigma(A, I)$ has a form of

$$\sigma(A, I) = CA^\tau \exp\{[-F(A, I) + \mu_n N + \mu_p Z]/T\}$$

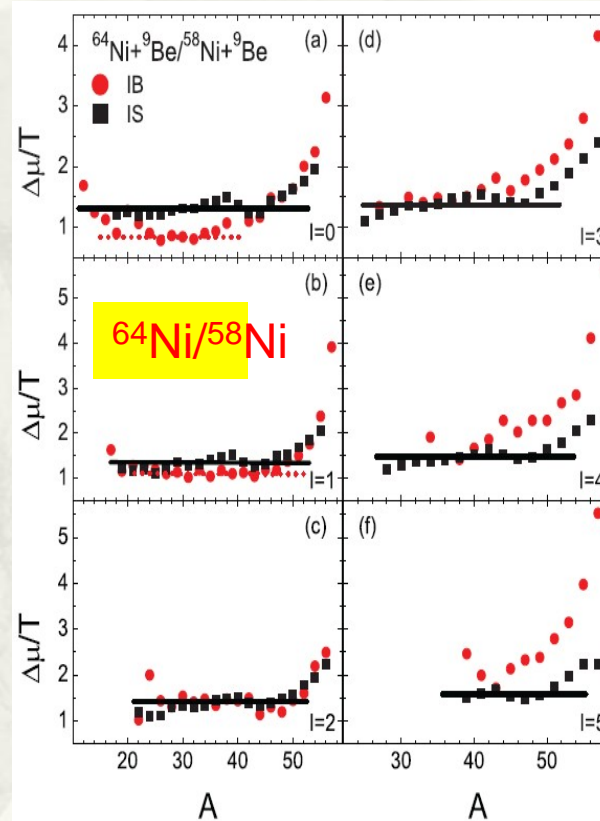
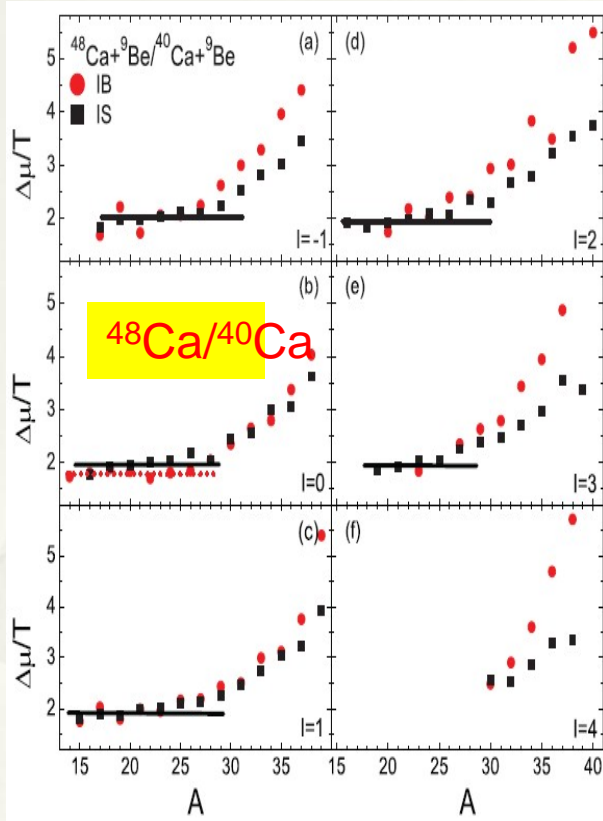
The isobaric yield ratio of isobars with $I+2$ and I is,

$$\begin{aligned} \ln R(A, I + 2, I) &= \ln[\sigma(A, I + 2) / \sigma(A, I)] \\ &= [F(A, I) - F(A, I + 2) + \Delta\mu] / T \end{aligned}$$

Similarly, for isobars with I and $I-2$, one has,

$$\begin{aligned} \ln R(A, I, I - 2) &= \ln[\sigma(A, I) / \sigma(A, I - 2)] \\ &= [F(A, I - 2) - F(A, I) + \Delta\mu] / T \end{aligned}$$

2. Method



- * In the isobaric ratio difference (IBD) analysis, $\Delta\mu/T$ from the small A fragment changes very little, which means $\Delta\mu/T$ can be cancelled out in the difference between the IYRs.

Ma CW et al., PRC87(2013)034618.

2. Method

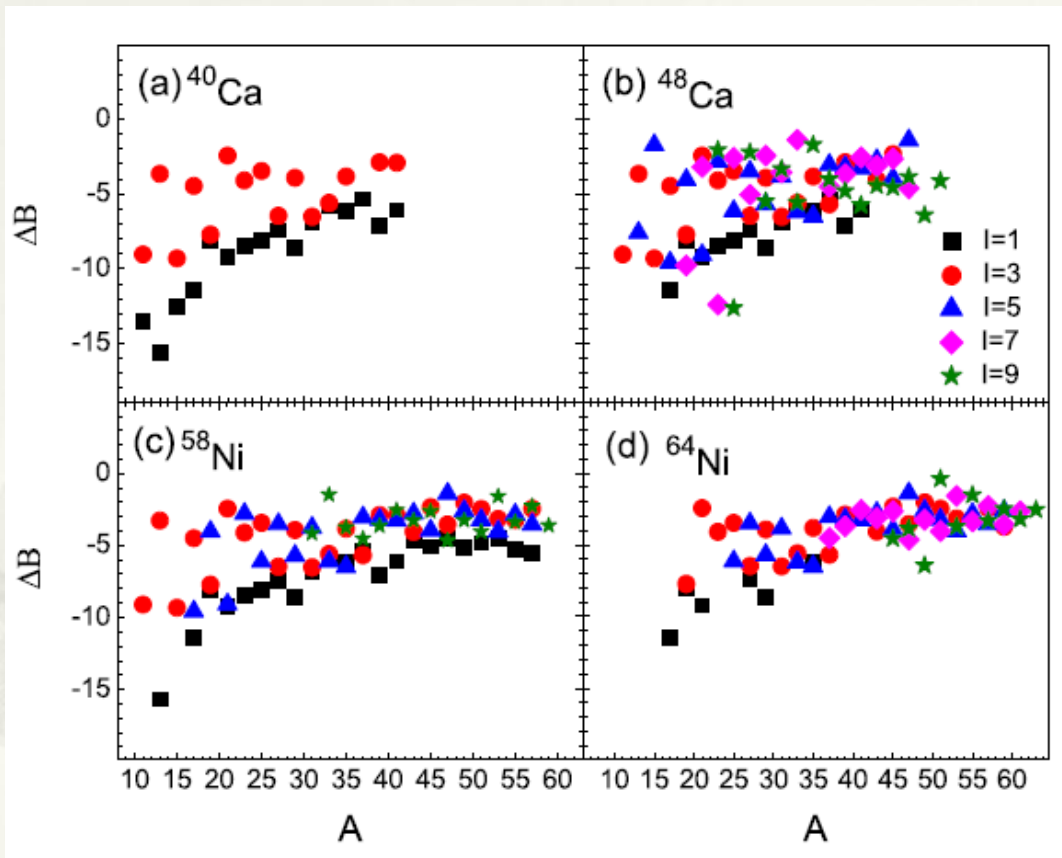
- * The difference of IYRs can be written as,

$$\begin{aligned} & \ln R(A, I + 2, I) - \ln R(A, I, I - 2) \\ & = [2F(A, I) - F(A, I + 2) - F(A, I - 2)]/T \end{aligned}$$

- * For fragments having finite temperatures, it is proven that the residue free energy between two isobars can be replaced by that of binding energy $B(A, I)$. The improved method to obtain T from the difference between IYRs (labelled as T_{IB}) can be written as,

$$T_{IB} = \frac{2B(A, I) - B(A, I + 2) - B(A, I - 2)}{\ln R(A, I + 2, I) - \ln R(A, I, I - 2)} = \frac{\Delta B}{\Delta \ln R}$$

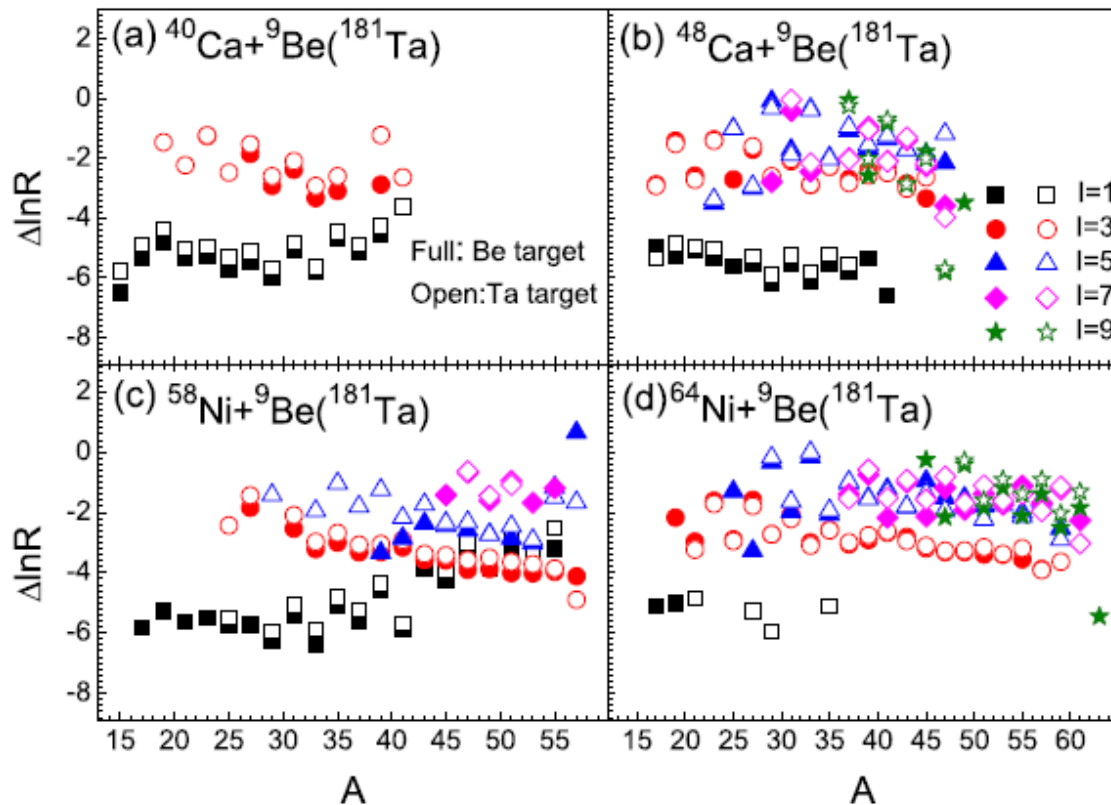
3. Results and Discussion



- * ΔB for the $I = 1$ fragments almost changes monotonically with A .
- * Staggering is shown in the ΔB for $I = 3, 5, \text{ and } 7$ fragments on the relative small A side.
- * The staggering in ΔB becomes smaller for the $A > 35$ fragments.

$\Delta B(\text{MeV})$ for the related isobars in the $140\text{A MeV } ^{40,48}\text{Ca} + ^9\text{Be}$ and $^{58,64}\text{Ni} + ^9\text{Be}$ reactions.

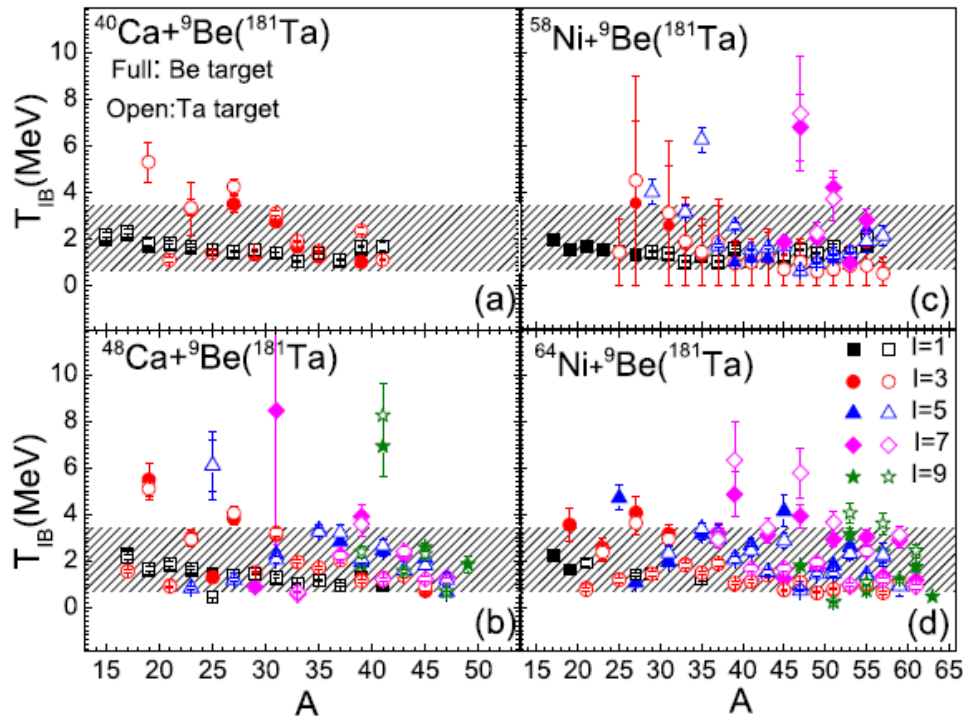
3. Results and Discussion



$\Delta \ln R$ for the related isobars in the $140\text{MeV } ^{40,48}\text{Ca} + ^9\text{Be} (^{181}\text{Ta})$ reactions

- * For the $I = 1$ fragments, $\Delta \ln R$ is almost constant on the small A side, but it increases with A when $A > 40$ and some staggering is shown when $A > 30$.
- * For the $I = 3, 5,$ and 7 fragments, an obvious staggering appears in $\Delta \ln R$ on the small A side, but this staggering becomes very small when A is relative large.
- * The target shows very little influence on the results of $\Delta \ln R$.

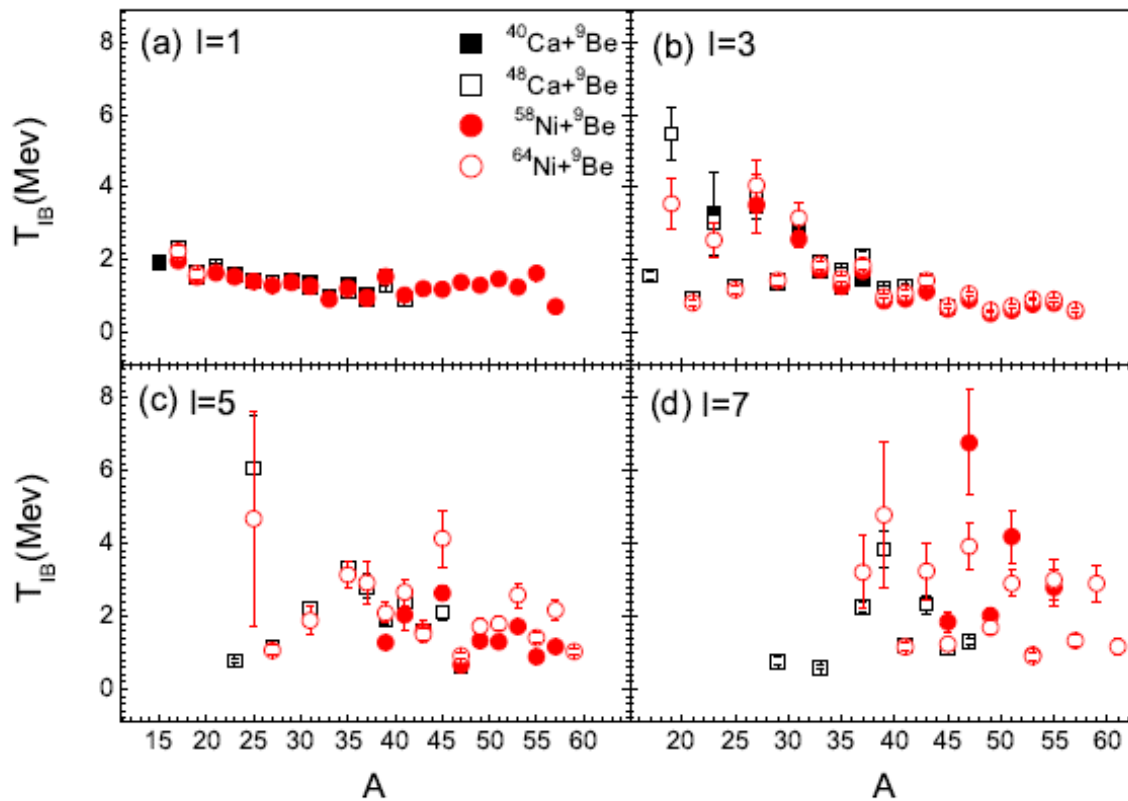
3. Results and Discussion



- * T_{IB} from the $I = 1$ fragments is almost constant around 1.5 MeV in all the reactions.
- * T_{IB} from the $I = 3$ fragments shows a relatively large staggering for the small A fragments.
- * T_{IB} from the $I = 5$ fragments shows a small staggering. But the staggering phenomenon again appears in T_{IB} for $I = 7$ and 9 fragments.

T_{IB} of the measured 140 A MeV $^{40,48}\text{Ca}+^9\text{Be}(^{181}\text{Ta})$ and $^{58,64}\text{Ca}+^9\text{Be}(^{181}\text{Ta})$ reactions, and the shadowed area is $0.6\text{MeV} < T_{IB} < 3.5\text{MeV}$.

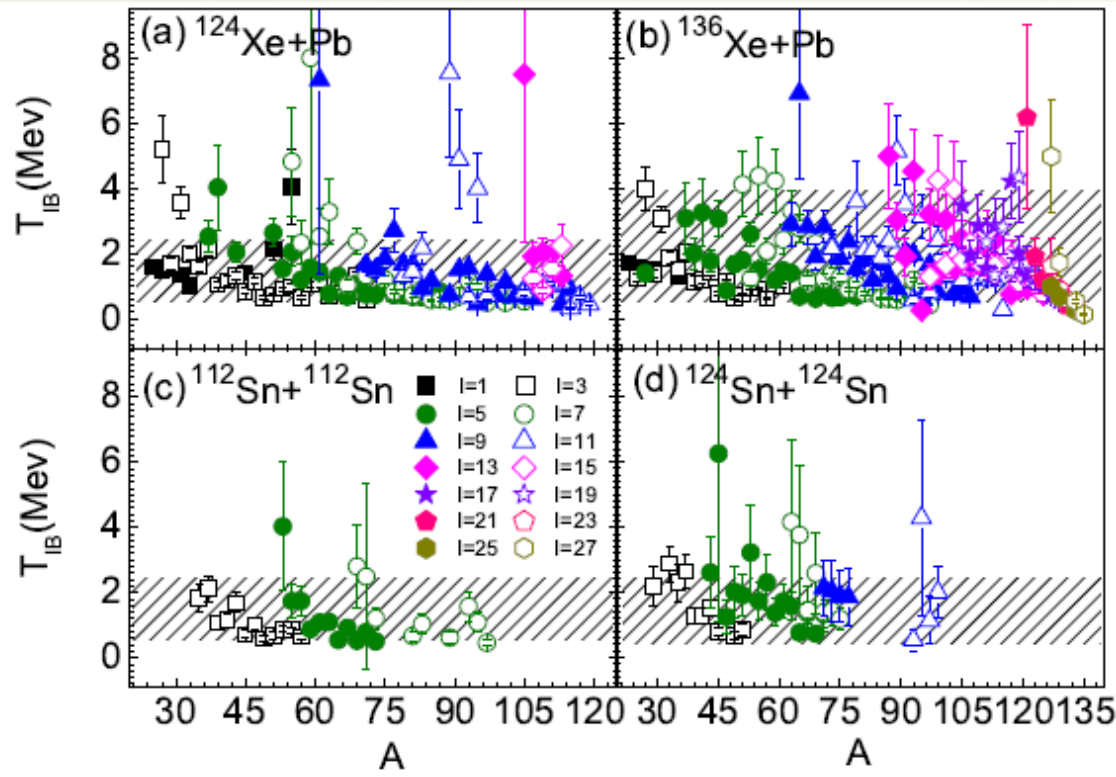
3. Results and Discussion



- * T_{IB} is almost same for the $I=1$ fragments, and is also almost same for the $I=3$ fragments except the fragments having relative small A .
- * Some obvious difference appears in T_{IB} of the $I=5$ fragments, and the difference becomes even larger in the $I=7$ fragments.

T_{IB} of the measured 140 AMeV $^{40,48}\text{Ca}+^9\text{Be}(^{181}\text{Ta})$ and $^{58,64}\text{Ca}+^9\text{Be}(^{181}\text{Ta})$ reactions are plotted according to I

3. Results and Discussion

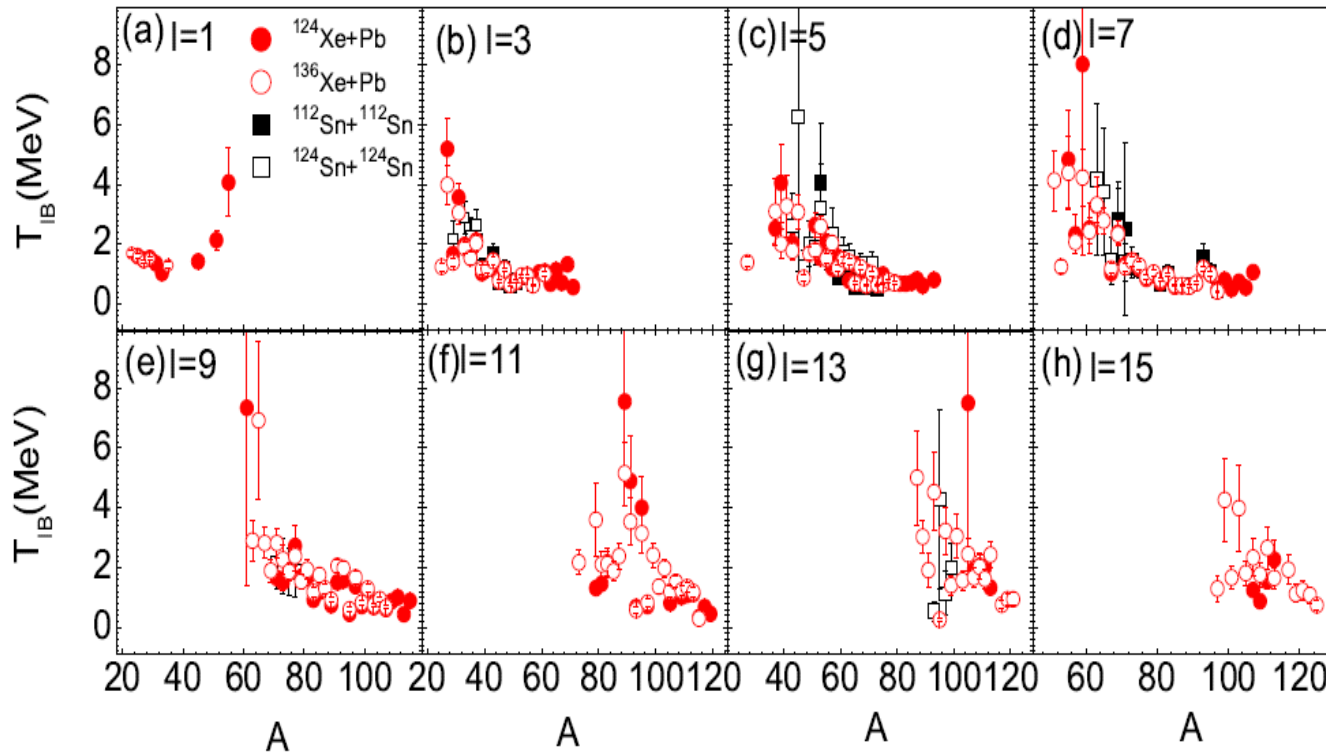


T_{IB} for fragments in the 1A GeV $^{124,136}\text{Xe} + \text{Pb}$ and $^{112,124}\text{Sn} + ^{112,124}\text{Sn}$ reactions.

T_{IB} from the fragments in the $^{112,124}\text{Sn}$ have the similar trend to those in the $^{124,136}\text{Xe}$ reactions, most of which are in the range $0.5\text{MeV} < T_{IB} < 2.5\text{MeV}$.

- * For most of the fragments in the ^{124}Xe reactions, T_{IB} falls in a range of $0.5\text{ MeV} < T_{IB} < 2.5\text{ MeV}$ comparing to that of $0.5\text{ MeV} < T_{IB} < 4\text{ MeV}$ for most of the fragments in the ^{136}Xe reactions, as shown by the shadowed areas.
- * Staggering is shown in T_{IB} for the small A fragments with $I = 3, 5,$ and 7 in both of the reactions, and in the fragments with $I = 13$ and 15 in the ^{136}Xe reaction.
- * For fragment with the same I , T_{IB} decreases with A , while T_{IB} for the relative large A fragment tend to be constant.

3. Results and Discussion



For the fragments with the same A , T_{IB} is very similar, which indicates that in the isoscaling and IBD methods, it is reasonable to assume that the temperature of a specific fragment in two reactions are the same.

Comparison of T_{IB} for fragments with same I in the measured 1A GeV $^{124,136}\text{Xe}+\text{Pb}$ and $^{112,124}\text{Sn} + ^{112,124}\text{Sn}$ reactions.

4. Summary

- An improved isobaric ratio thermometer (T_{IB}) for IMFs has been developed based on the difference between IYRs, in which the residual binding energy is used instead of the residue free energy.
- In contrast to the IYR thermometer, T_{IB} is obtained directly from fragments and avoids the fitting procedure in the IYR method, which makes T_{IB} become a direct probe to temperature.
- The values of T_{IB} for most considered intermediate-mass fragments are low.



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Thank you for your attention!